

Muon Colliders:

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Lake Geneva, Wisconsin

Why consider a Muon Collider?

The mass of the muon ($m_\mu/m_e = 207$) gives a \square collider some very desirable features:

- Less synchrotron ($\sim m^{-4}$), brem and initial state radiation \rightarrow muons don't radiate as readily as electrons:
- Larger couplings to Higgs-like particles - if $m_h < 2m_W$, possible to study Higgs boson production in the s-channel

This gives four compelling arguments for the muon collider versus other machines:

1. Possible low energy Higgs Factory
2. Narrower energy spread
3. Easier acceleration
4. Smaller machine footprint

From a Neutrino Factory to Muon Collider

Much of what has been learned from the neutrino factory feasibility studies can be applied to a muon collider:

- Targetry
- Capture and Decay
- Transverse Cooling
- Accelerating a Large Beam

A muon collider requires the muon beams to be cooled by several orders of magnitude compared with a neutrino factory.

All the muons must be in one bunch \rightarrow **6 dimensional cooling!**

Low Energy Higgs Factory

Muons are

- Only **massive** where s-channel resonance can be observed
- The Higgs width can be measured directly
- $h \rightarrow \mu\mu$ coupling is a direct test of the fermion mass generation mechanism. It can be measured to $\pm 4\%$ with $L = 0.2 \text{ fb}^{-1}$ if the beam energy resolution $R=0.003\%$

...also, you can get a narrow beam

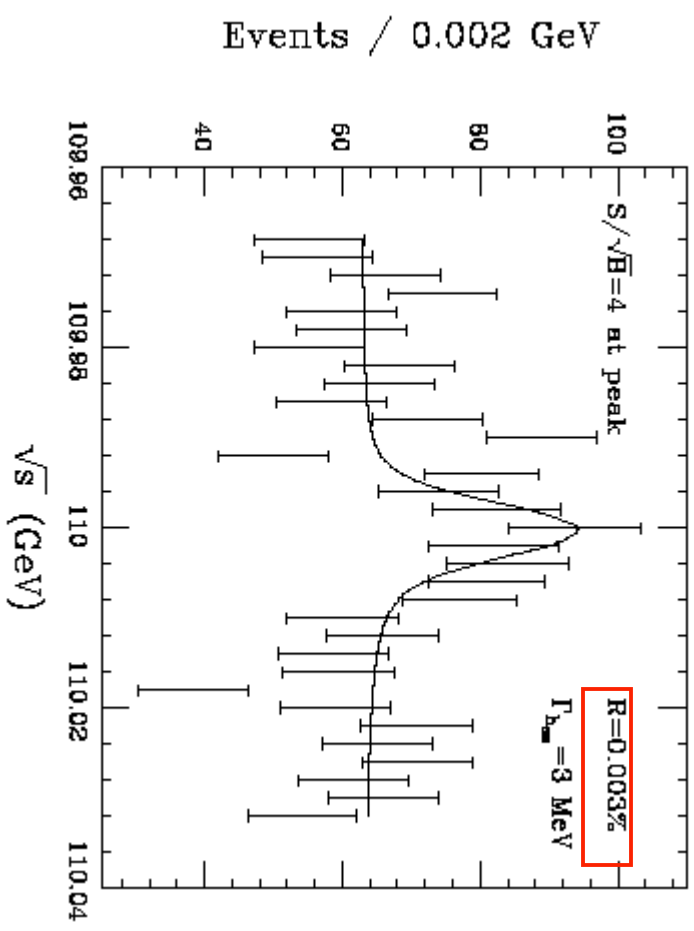
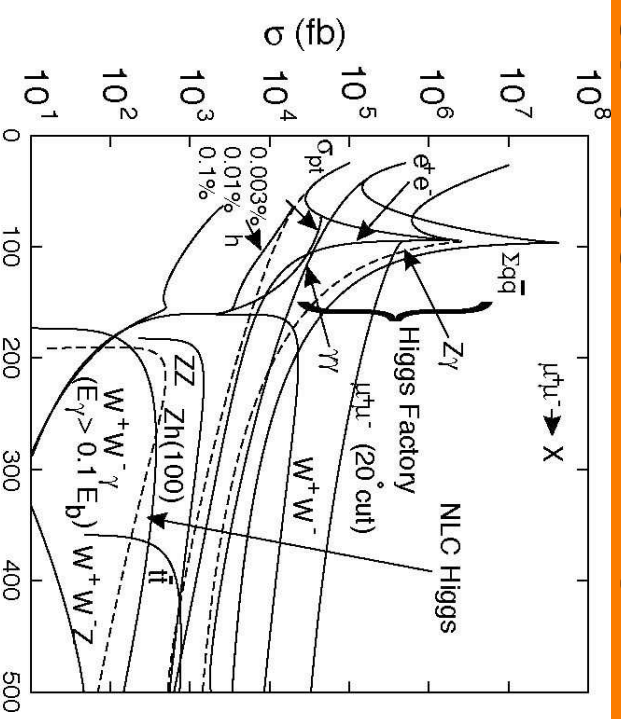
energy spread

$$\left(\frac{m_e}{m_\mu} \right)^2 = 6 \times 10^{-10}$$

Muon collider can provide the most precise measurement of the mass of a light Higgs using a beam energy scan of the resonance

	LHC	LC	$\mu^+\mu^-$
\mathcal{L}		500 fb ⁻¹	0.2 fb ⁻¹
m_h	9×10^{-4}	3×10^{-4}	3×10^{-6}
Γ_h^{tot}	> 0.3	0.17	0.2

Exceeds precision of theoretical predictions?



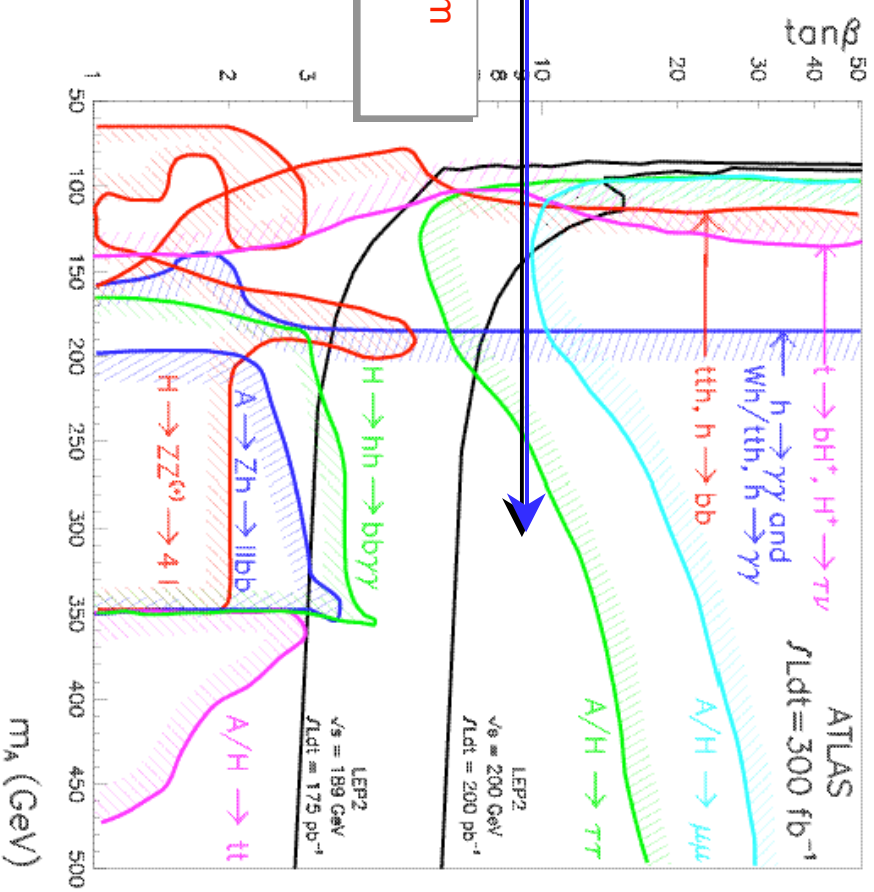
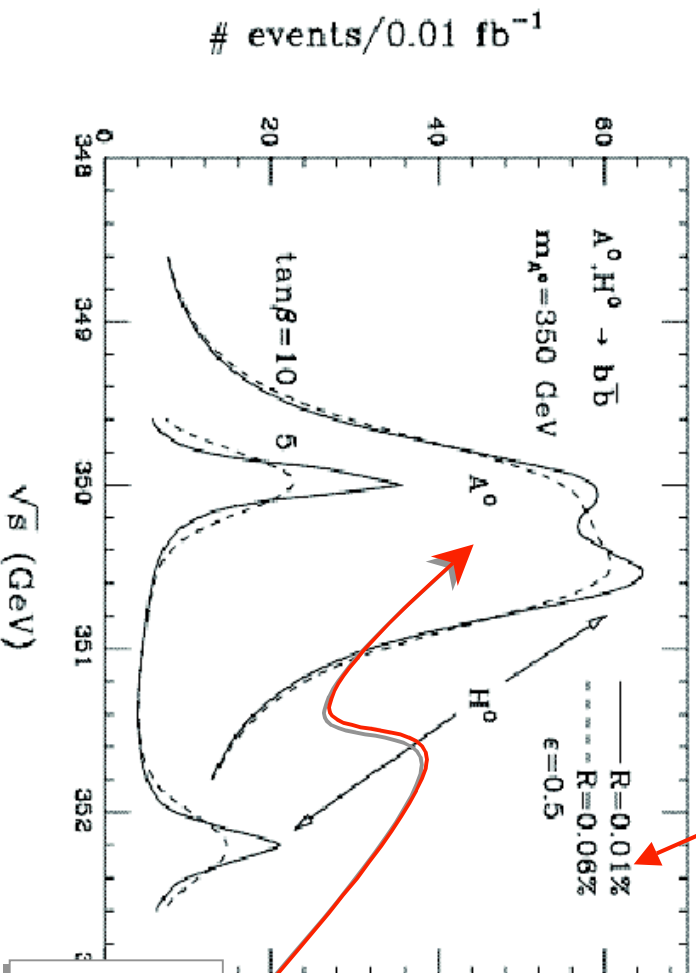
SUSY Higgs Factory

Regions of parameter space other machines just can't probe

...but must first raise \sqrt{s} !

A possible LHC and LC "blind spot"

Note dependence on beam energy resolution!



$$m_{A^0} \gtrsim \max \left\{ \frac{\sqrt{s}}{2} \text{ (LC)}, 250 \text{ GeV (LHC)} \right\}$$

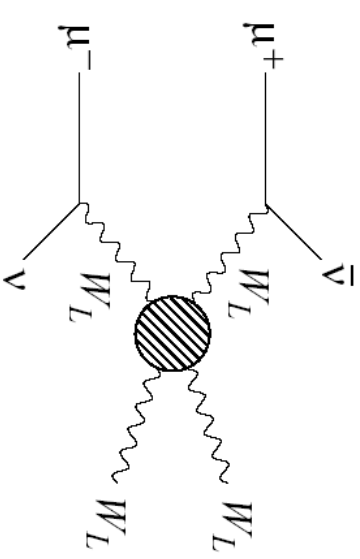
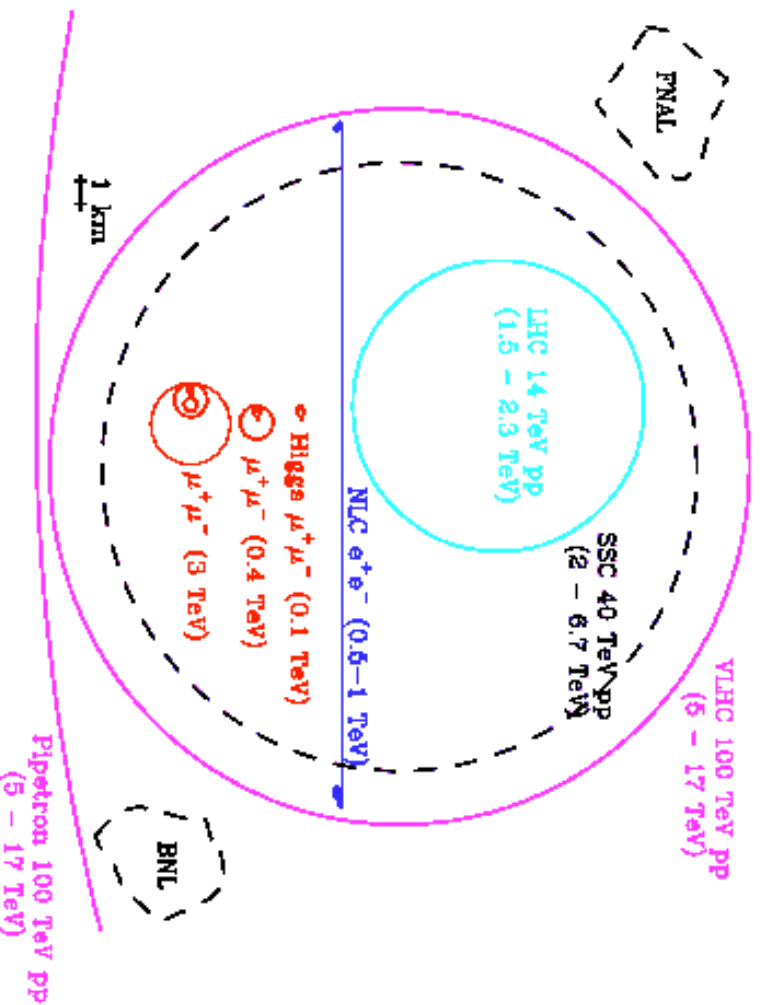
MH-MA: If masses are degenerate, they can only be resolved by exploiting the narrow beam energy spread at a muon collider using a scan.

Energy Frontier Machines

And, we don't know what lies beyond the

electroweak scale

The current story suggests that there “has” to be something at or approaching the **TeV energy scale**, but sooner or later we will want a multi-TeV lepton machine for precision measurements of SEWS (strongly interacting electroweak sector)



Muon colliders are smaller than other machines for a given energy
 ☐ Less real estate

The energy not radiated away is that much less for RF to accelerate

High energy muon colliders retain the possibility of narrow beam energy spread

High energy machine chosen will be the one that optimizes the cost/luminosity/energy equation

Other muon collider issues

- **R:** Gaussian spread in beam energy can be made very small, but at cost of Luminosity:
 - Some “conservative” calculations:
 - $L \sim (0.5, 1, 6) * 10^{31} \text{ cm}^{-2} \text{ s}^{-1}$ for $R = (0.003, 0.01, 0.1)\%$ and $\sqrt{s} \sim 100 \text{ GeV}$
 - $L \sim (1, 3, 7) * 10^{32} \text{ cm}^{-2} \text{ s}^{-1}$ for $\sqrt{s} = (200, 350, 400) \text{ GeV}$ and $R \sim 0.1\%$
 - So, $\square C$ best for: $h \quad \square + \square - \quad \sqrt{s} E_{\text{beam}} / E_{\text{beam}} = 0.01 R$
 - H_0 and A_0 peak separation, Higgs scan
 - CP of Higgs bosons
 - Good measurement of $h \quad \square + \square$ possible
- At FNAL unique opportunity for $\square p$ collisions:
 - 200 GeV \square beams in collision with 1 TeV p beam:
 - $L \sim 1.3 * 10^{23} \text{ cm}^{-2} \text{ s}^{-1}, \quad \square = 894 \text{ GeV}$
 - Neutrino Factory** a natural intermediate step!
- Luminosity can be improved by further R & D in emittance exchange, cooling, targetry.
 - May be the best for extreme energies
 - Can guarantee access to heavy SUSY particles, Z' and strong WW scattering if no Higgs Bosons and no SUSY
- If \square 's and e 's are fundamentally different, a $\square C$ is necessary!

The machine parameters...

Higgs Factory

CoM energy (TeV)	3	0.4		0.1	
p 's/bunch	2.5×10^{13}	2.5×10^{13}		5×10^{13}	
μ /bunch	2×10^{12}	2×10^{12}		4×10^{12}	
Rms $\Delta p/p$ %	0.16	0.14	0.12	0.01	0.003
6-D $\epsilon_{6,N}$ (πm) ³	1.7×10^{-10}	1.7×10^{-10}	1.7×10^{-10}	1.7×10^{-10}	1.7×10^{-10}
Rms ϵ_n (π mm-mrad)	50	50	85	195	290
β^* (cm)	0.3	2.6	4.1	9.4	14.1
σ_z (cm)	0.3	2.6	4.1	9.4	14.1
σ_r ,spot (μm)	3.2	26	86	196	294
σ_θ IP (mrad)	1.1	1.0	2.1	2.1	2.1
Luminosity $\text{cm}^{-2}\text{s}^{-1}$	7×10^{34}	10^{33}	1.2×10^{32}	2.2×10^{31}	10^{31}
Higgs/year			1.9×10^3	4×10^3	3.9×10^3

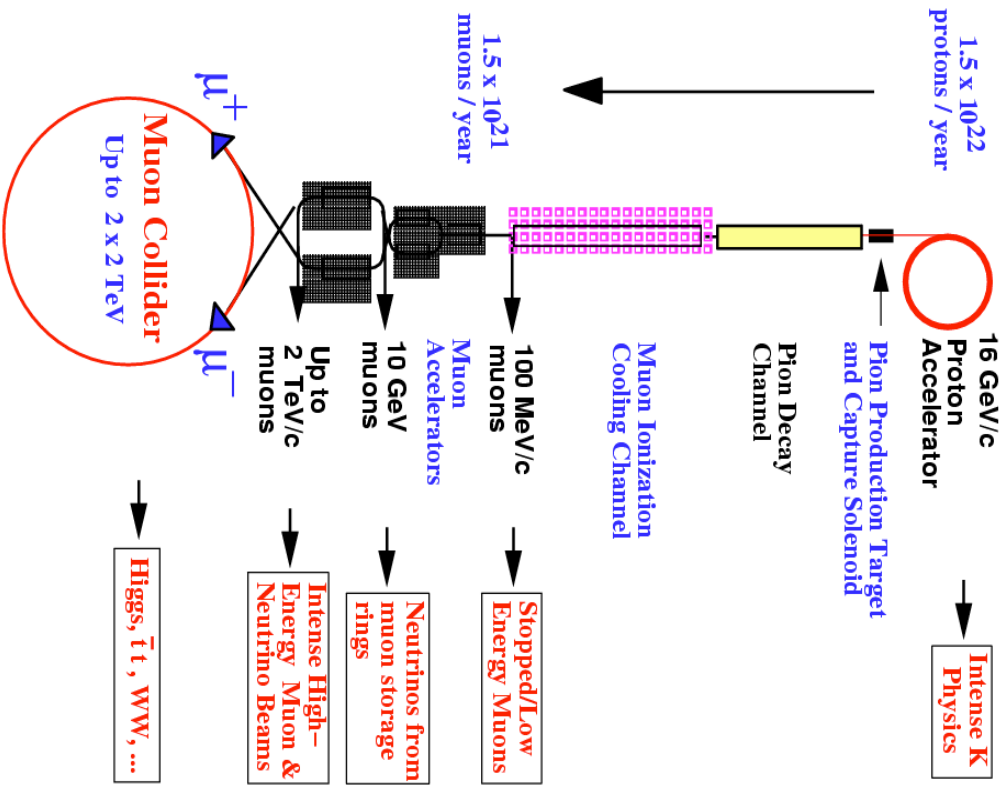
$$\boxed{\mathcal{L} = 5 \times 10^4 \text{ fb}}$$

orders of magnitude
more cooling than for
a v factory!

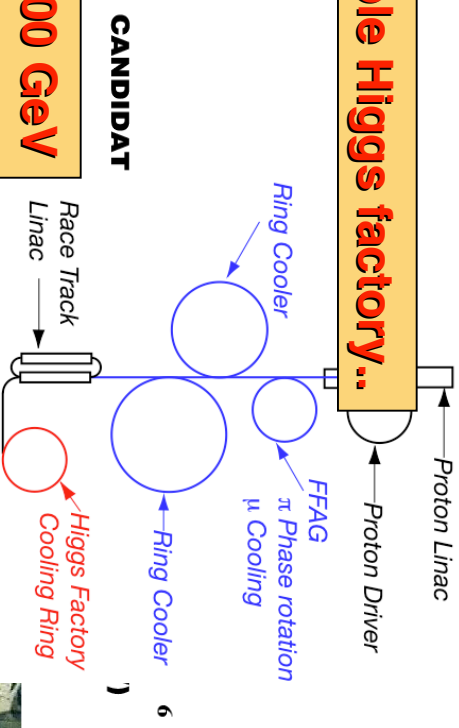
Also, high luminosity means fewer bunches!

Technical Staging and Physics

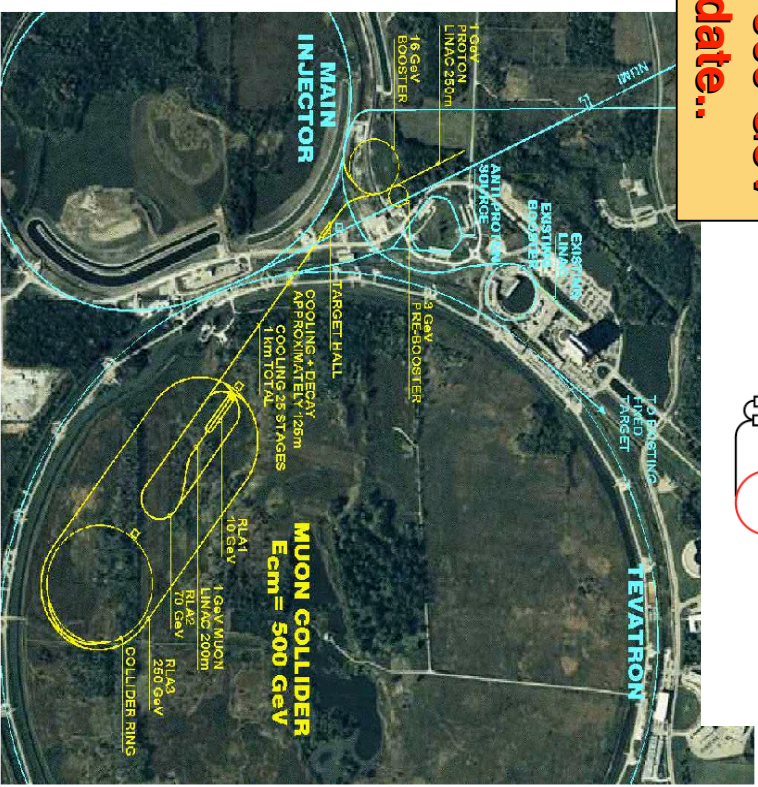
Muon Collider Schematic



Possible Higgs factory..

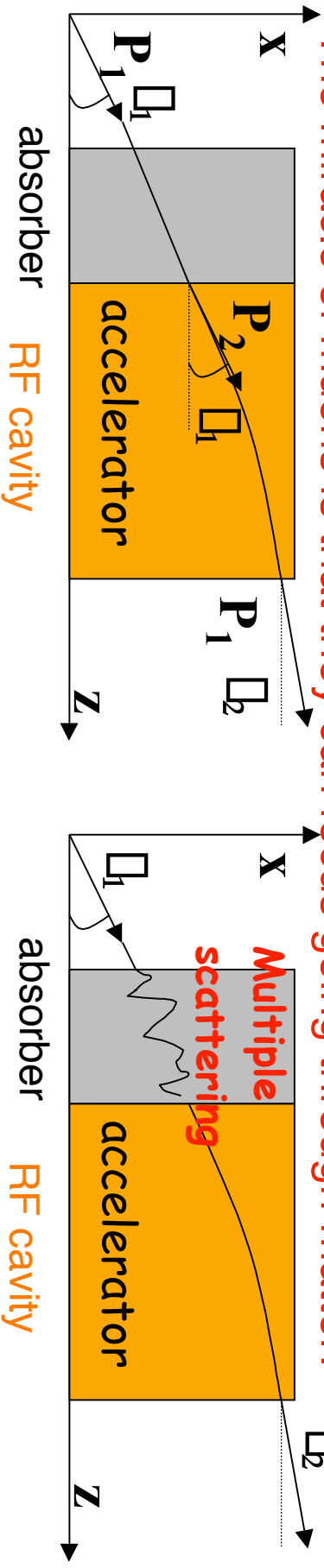


FNAL 500 GeV candidate..



Ionization Cooling

The miracle of muons is that they can focus going through matter!



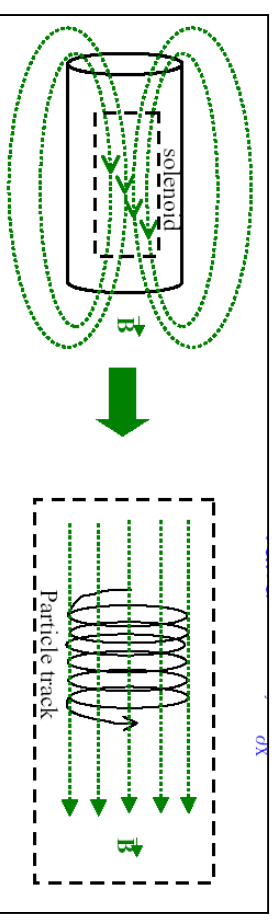
Liouville's Theorem states that phase space is invariant.. need to remove energy to increase particle density...

Phase space equation:

$$\frac{d\hat{a}_x}{dz} = \underbrace{\left[-\frac{\hat{a}_x}{L_{\text{trans}}} \right]}_{\text{Cooling term}} + \underbrace{f \hat{a}_x^3}_{\text{Heating term (mult. scatt.)}} E m_1 L_R$$

With transverse focussing (solenoid)

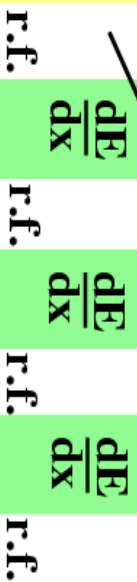
□ ~ beam envelope:



6 - Dimensional Cooling

Ioniz

1

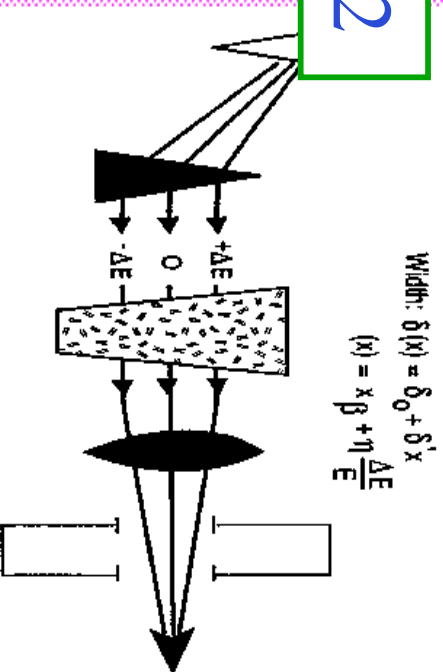


Muons lose energy by dE/dx and longitudinal momentum replaced by r.f.

To Minimize heating from Coulomb Scattering:

- Small β_{\perp} (strong focusing) : High-field solenoids or Lithium Lenses
- Large L_R (low-Z absorber) : Liquid H_2

2



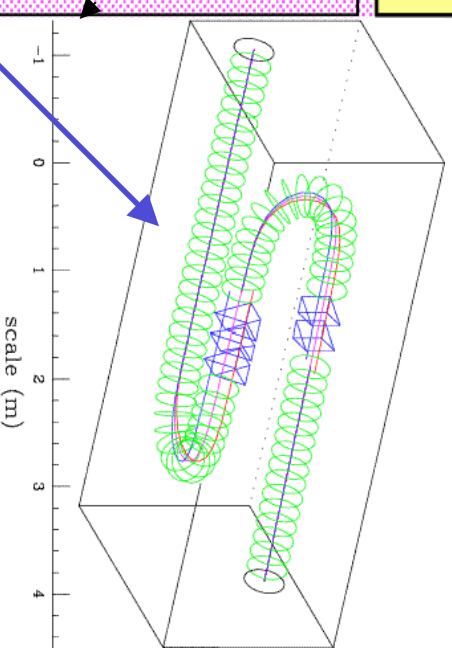
Energy "Cooling"

Ionization cooling using a wedge plus dispersion.

Exchanges emittance between transverse & longitudinal directions

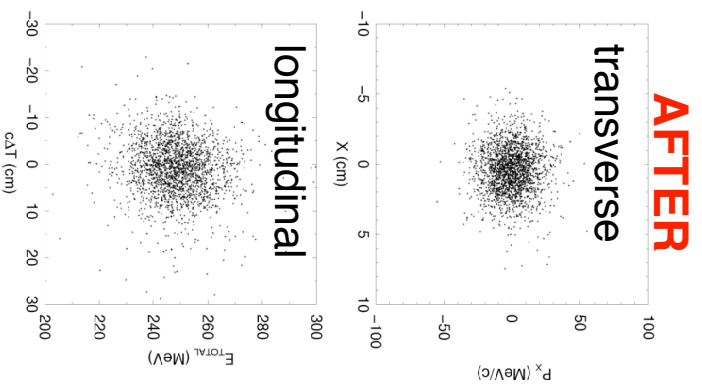
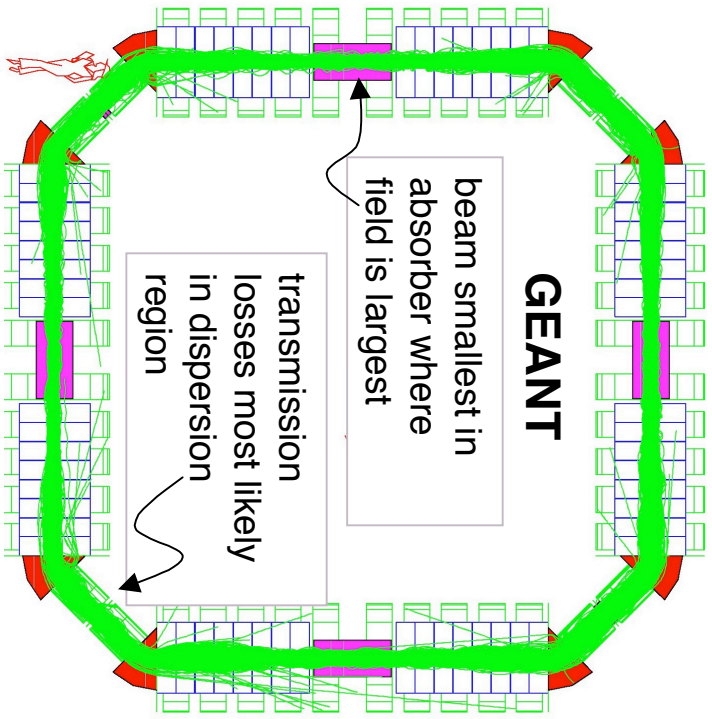
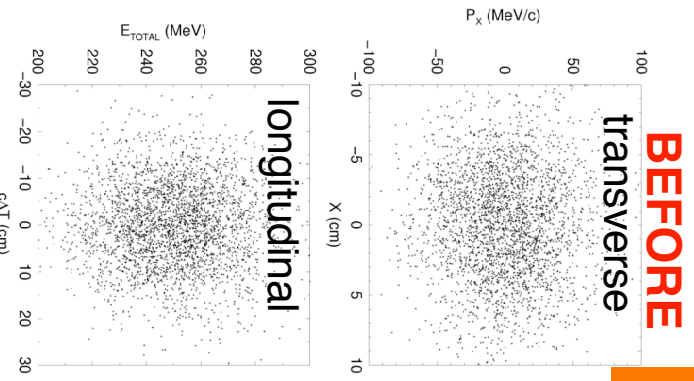
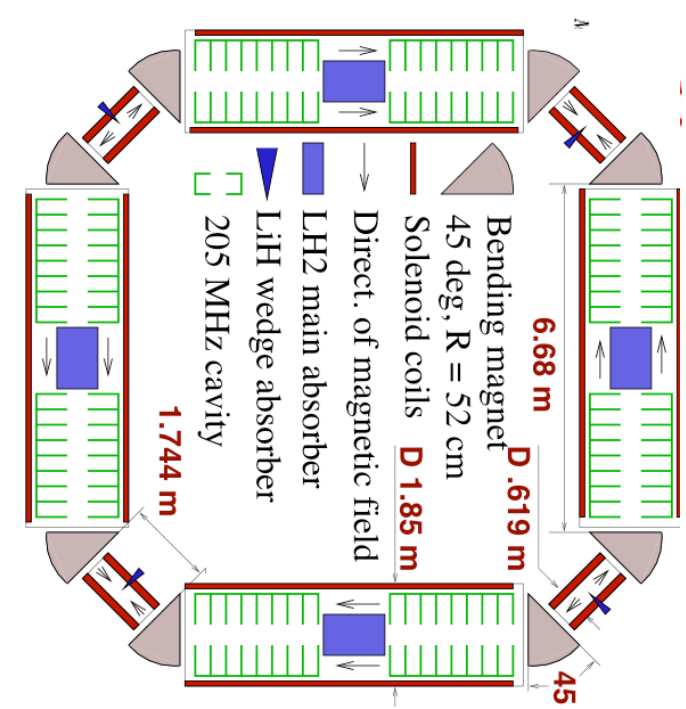
Cooling merit factor:
 $\epsilon_b(\text{init})/\epsilon_b(\text{final})$

1. Neutrino source: 4-dimensional cooling
2. Muon collider: 6-dimensional cooling

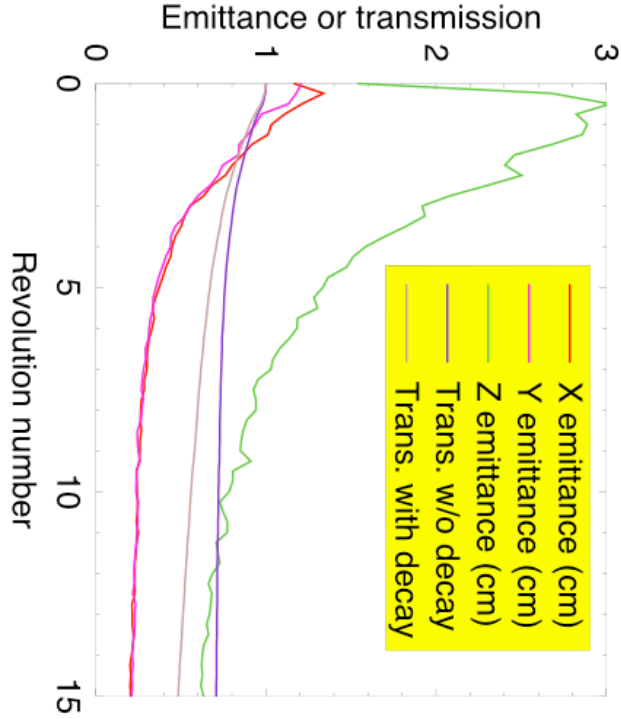


Bent Solenoid: drift proportional to particle's momentum, introduces dispersion, \square

Ring Coolers



- Provides same transverse cooling as sFOFO linear channel considered in neutrino factory Study II.
- Heat dissipation in absorber could be challenging
- Injection and extraction is difficult-no space

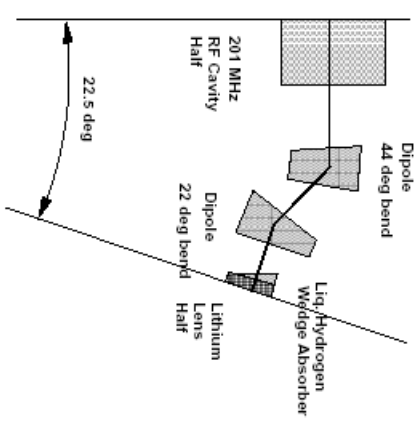
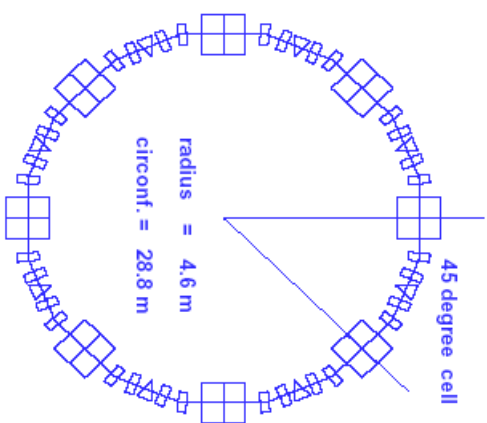


Merit Factor=38 after 15 turns

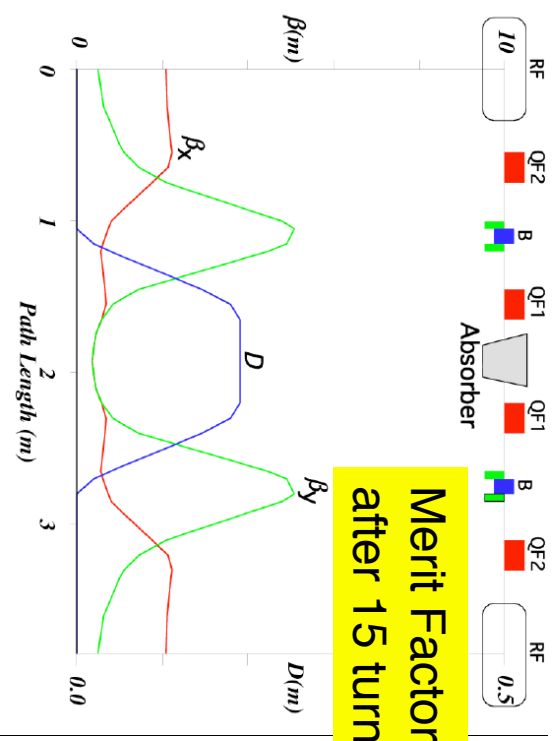
Lattice cooling rings

dipole only

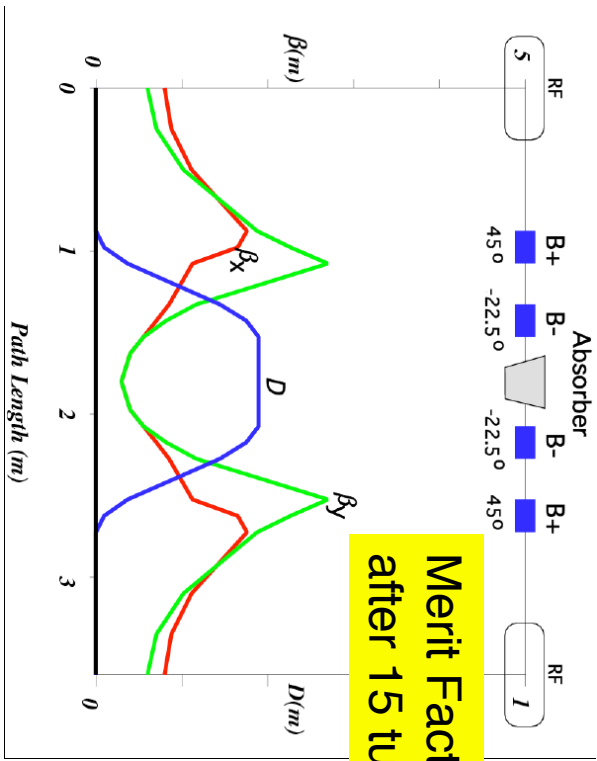
Use only convention quadrupole and/or dipole magnets to contain beam.



Quadrupole/dipole ring



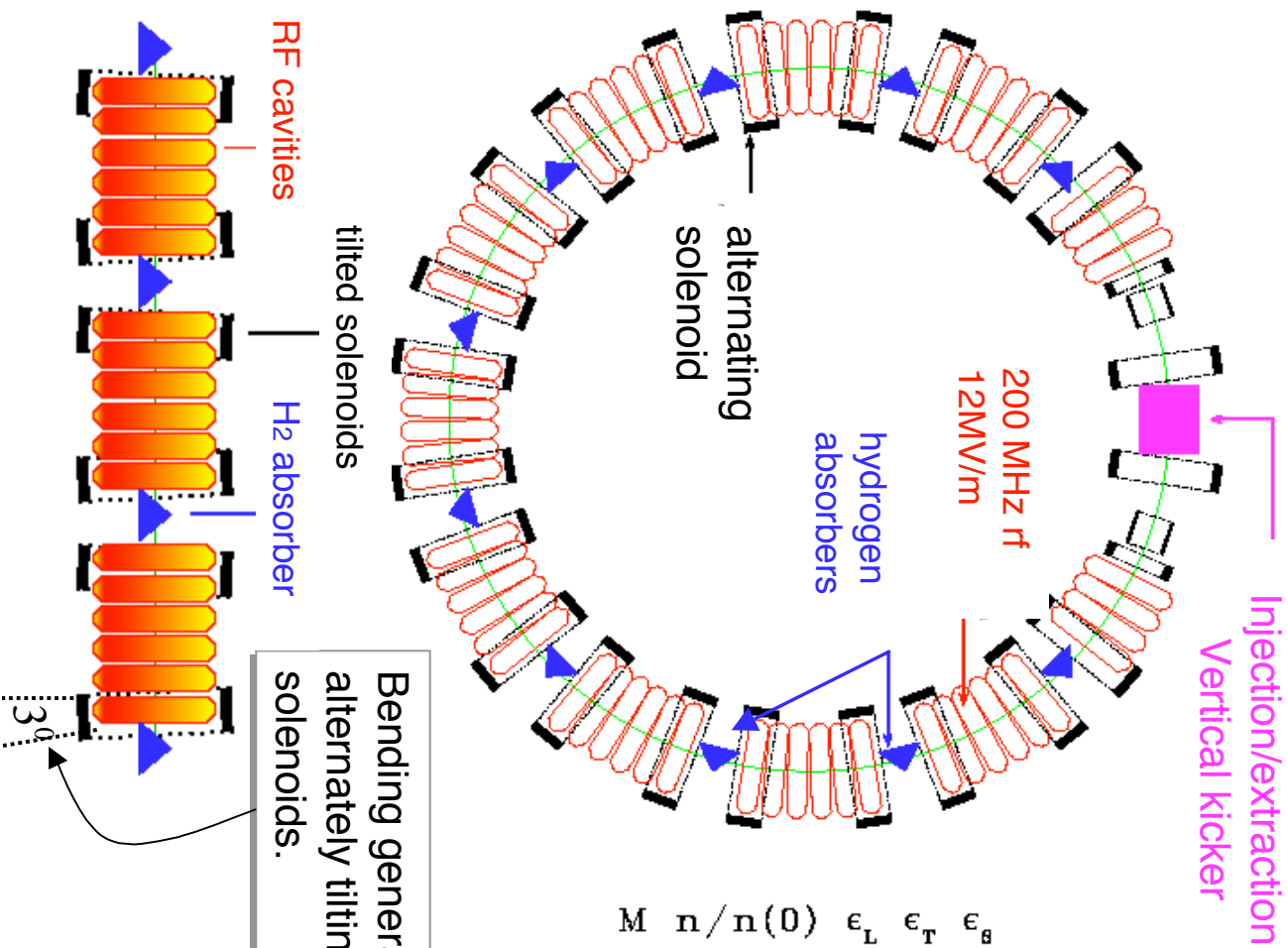
Merit Factor=15 after 15 turns



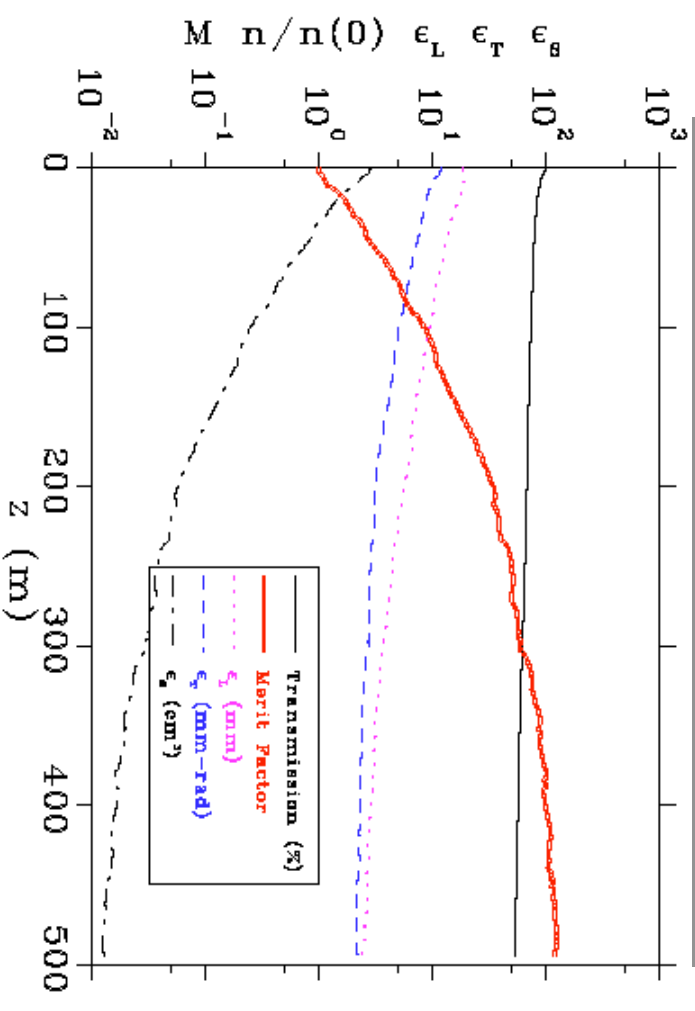
Merit Factor=80 after 15 turns

Performance improves for more compact lattices-could be a problem for injection/extraction

Alternating Solenoid Ring



Solenoids flip polarity at the center of a cell. All cells are identical.



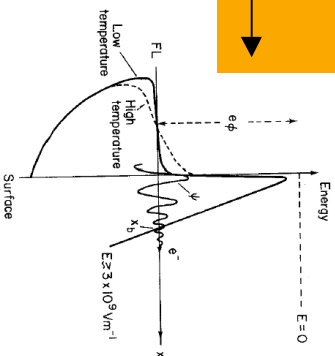
Merit factor decreases by ~30% after accounting for injection/extraction.

Dark matter dominates the universe
 Dark Energy controls its destiny ...
 Dark currents keep us from unveiling its secrets...

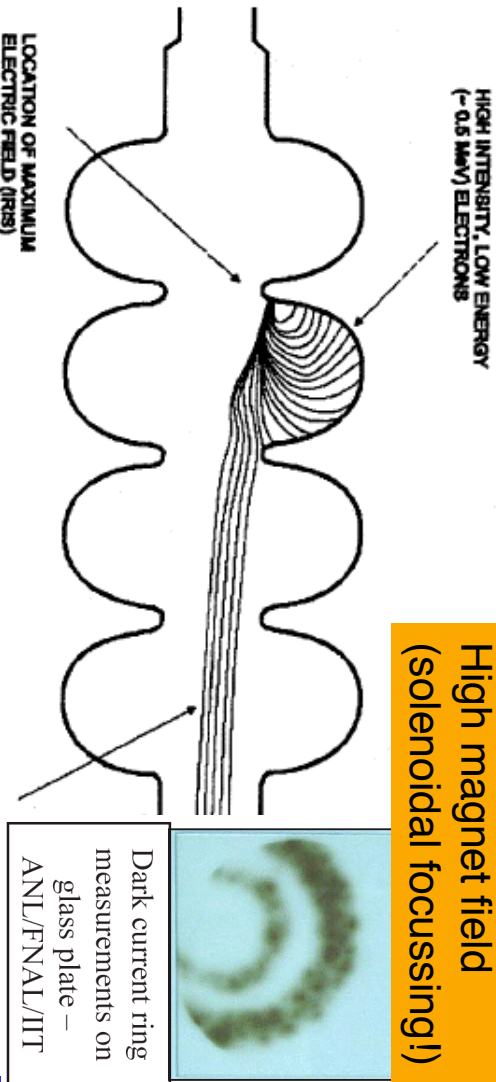
Dark currents

Fowler-Nordheim field emission
 (quantum tunnelling effect): \longrightarrow

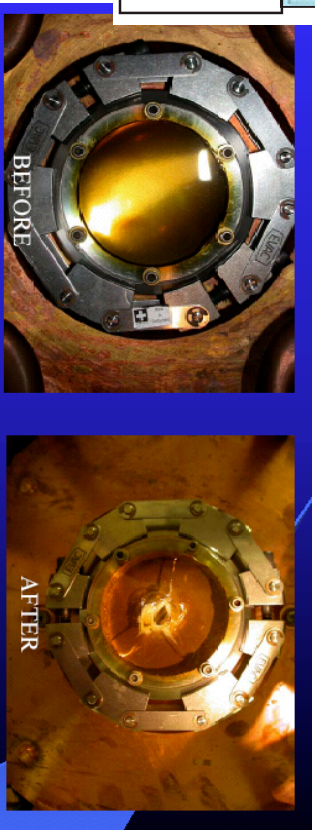
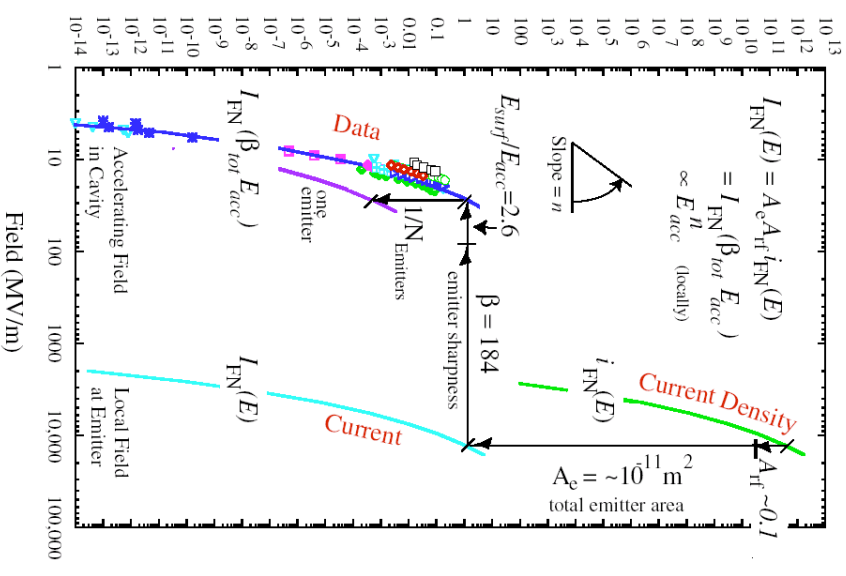
$$I(E) = \frac{A_{FN} A_e (\beta_{FN} E)^2}{\exp\left(\frac{B_{FN} \beta_{FN}^{3/2}}{E}\right)}$$



High magnet field
 (solenoidal focussing!)



Current, I (A), or current density, i (A/m^2)



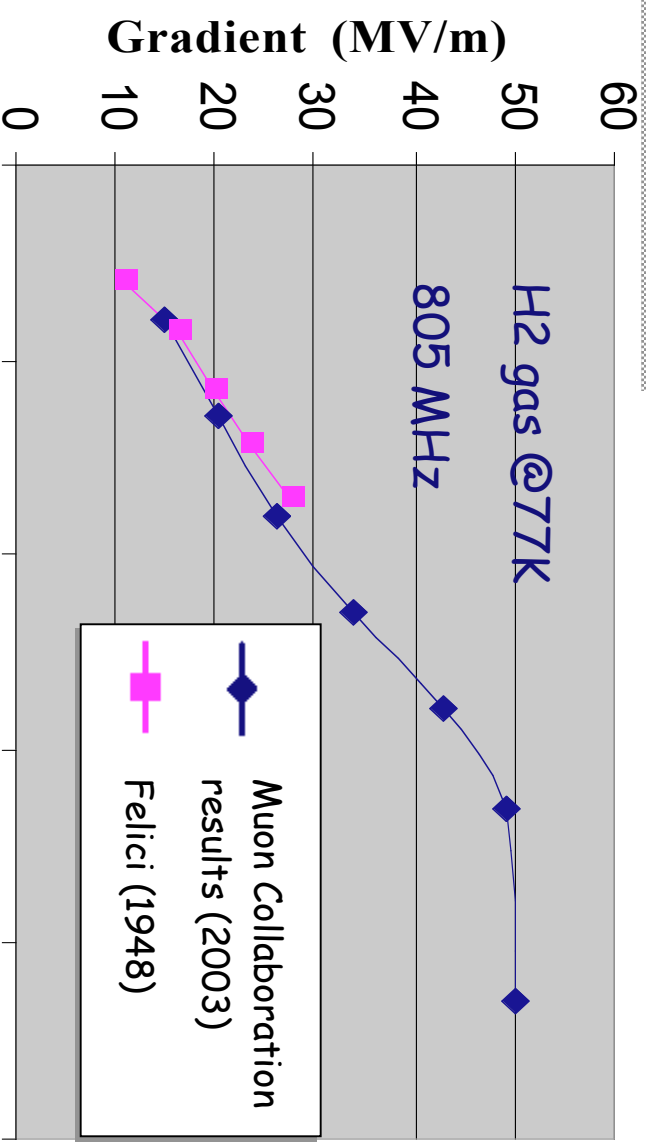
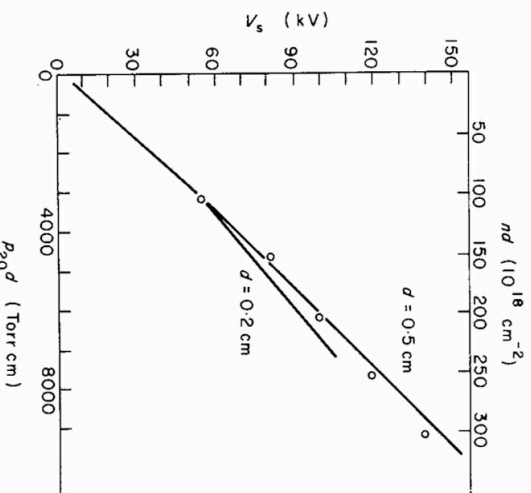
High Gradient Cavities: a gas filled approach

Paschen's Law (1889): breakdown voltage for discharge between electrodes in gases is a function of the product of pressure and distance.

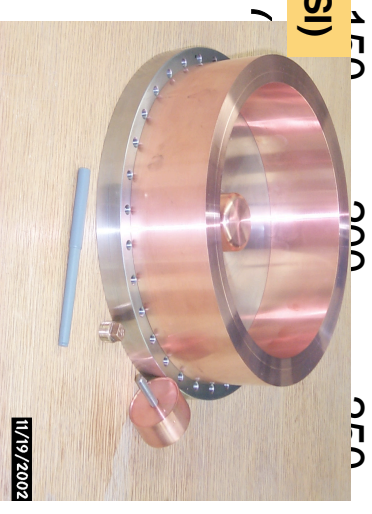
Gaseous hydrogen:

$$V_{breakdown} = 0.448nd + 0.6\sqrt{nd}$$

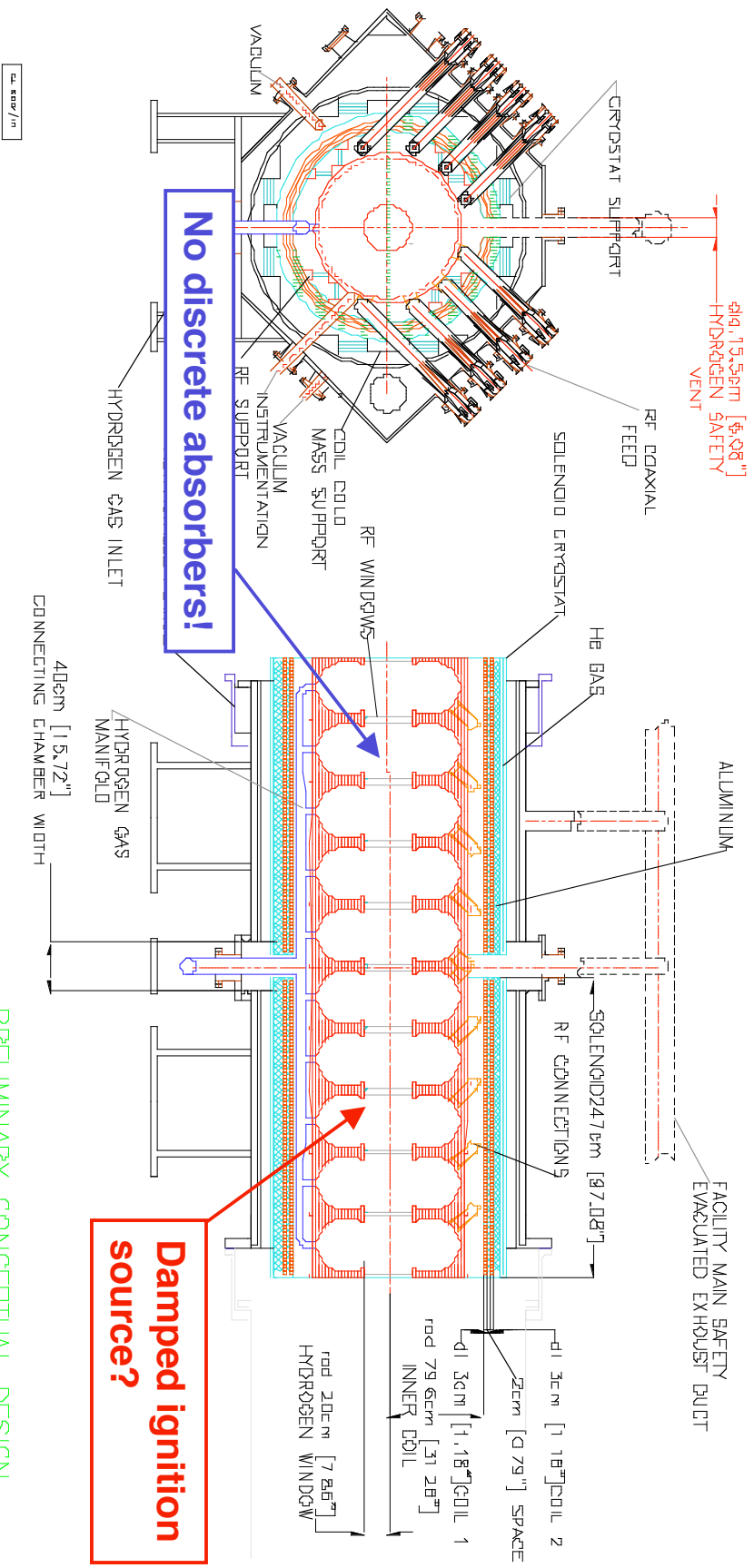
density n ; pressure required decreases with temperature



- Suppresses breakdown, allowing higher gradients
- Absorbs dark current radiation
- Gas with high heat capacity cools RF windows and increases electrical efficiency
- Gas can even act as a homogeneous absorber to provide ionization cooling!



Gaseous Hydrogen Cooling Channel

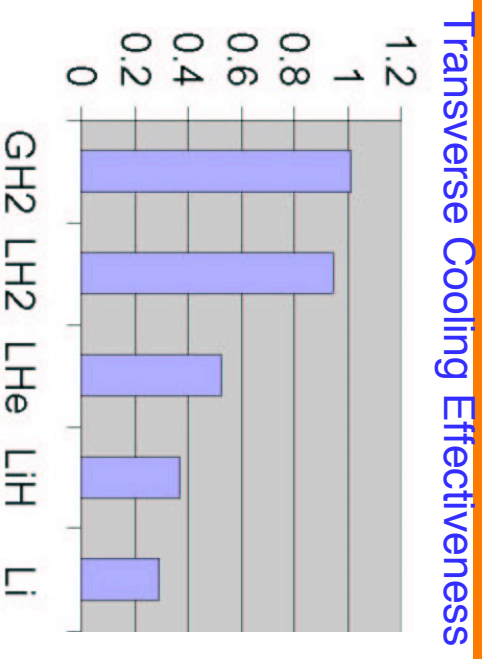


- Dense GH_2 suppresses high-voltage breakdown inhibits avalanches (**Paschen's Law**)
- No absorber windows necessary!
- Best for uniform solenoidal fields

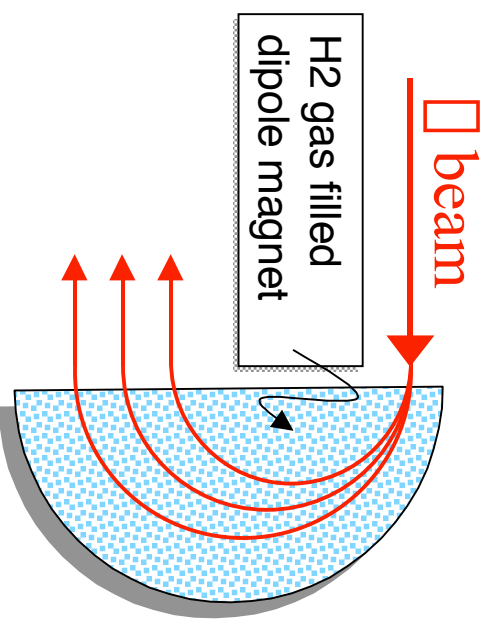
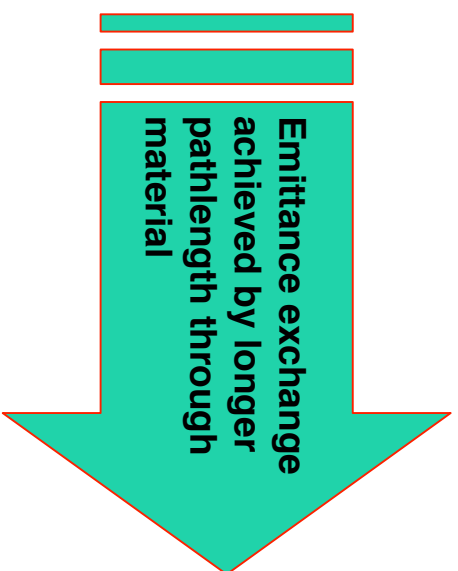
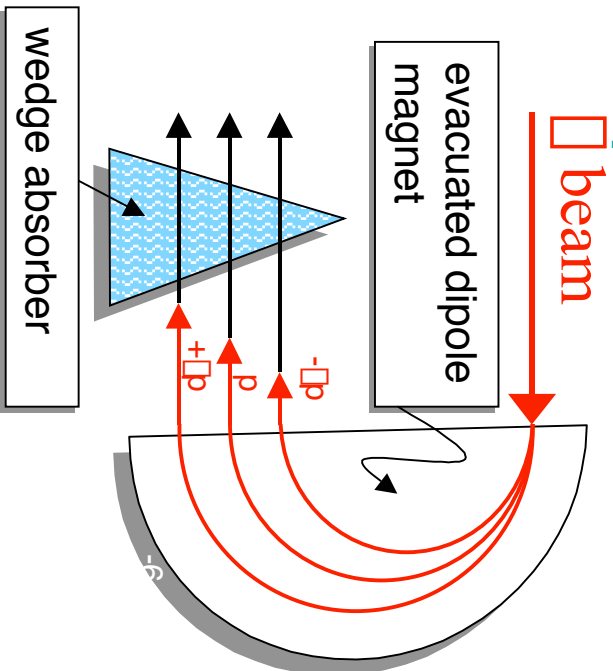
Major challenge to the prevailing safety culture!

6D Cooling in a gas filled RF cavity

To achieve the same cooling power : $(X_0 \cdot dE/dx)$
 for transverse cooling as in current LH2 cooling channels requires a GH2 pressure above that needed to suppress breakdown

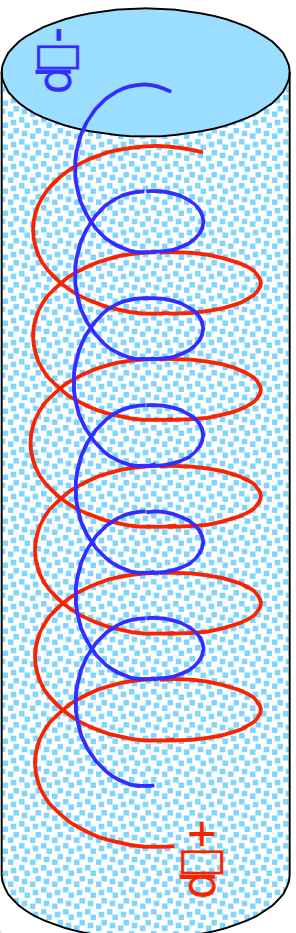


6D Cooling Channel: a gas-filled cavity in a solenoid plus transverse helical dipole fields



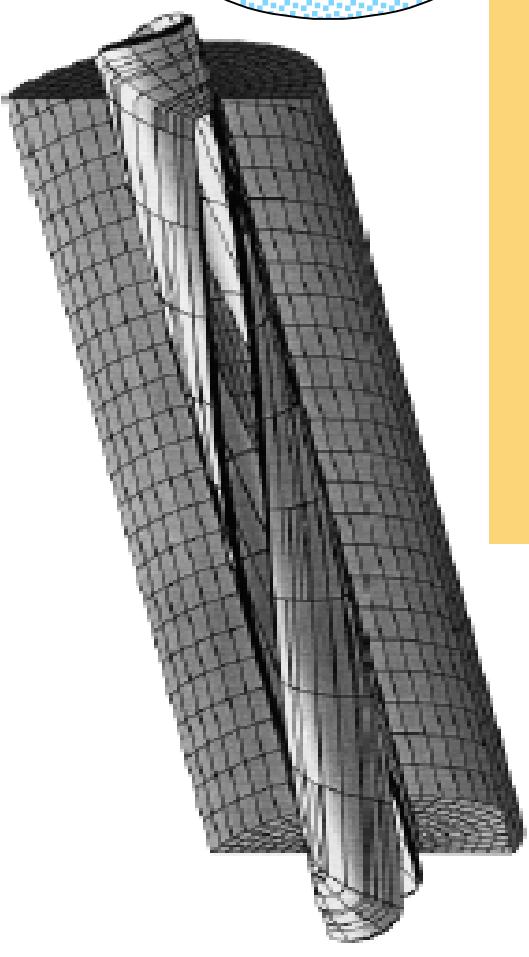
6D Cooling with GH2

- Derbenev channel: Solenoid plus transverse helical dipole fields
- Analytically see equal cooling decrements and 10^6 phase space reduction in ~ 150 m channel with energy loss of $1/3$
- Not a ring channel – avoids ring problems
 1. Injection and Extraction simpler
 2. No Multi-pass Beam loading or Absorber heating
 3. Can adjust channel parameters as beam cools



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Direct Wind Type

Paper contributed to COOL03 Meeting Hotel Fuji, Japan
http://members.aol.com/muonsinc/COOL03_6-d_rev1.pdf

Concluding remarks

- **Hadron colliders** have traditionally been the “discovery” machines, and the Tevatron and LHC **at this time**, may be no exception.
- We don’t have enough information to make a decision to commit to any ~ \$10G machine, and couldn’t build any if we did **at this time**.
- Accelerator and detector R & D is needed for all major proposed machines, and breakthroughs in any of them help all of them.
- Muon colliders are the farthest reaching machines, but recent developments suggest that it **NOT** necessarily the furthest away from being built **at this time**: both statements support a strong R & D program.
- Furthermore, an early stage of the μ C, the μ **factory**, is a machine that may be technically and financially feasible ~ next 10 years.
- Aggressive accelerator and detector R & D is the only way we move from a “**story**” **driven** field to become a **data driven** field – and the muon collaboration is doing just that: a strong group of accelerator and particle physicists, reversing a > 40 year trend.