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Exclusive Semileptonic B decays at BaBar

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BaBar Collaboration

Outline

CKM Matrix and unitarity relations

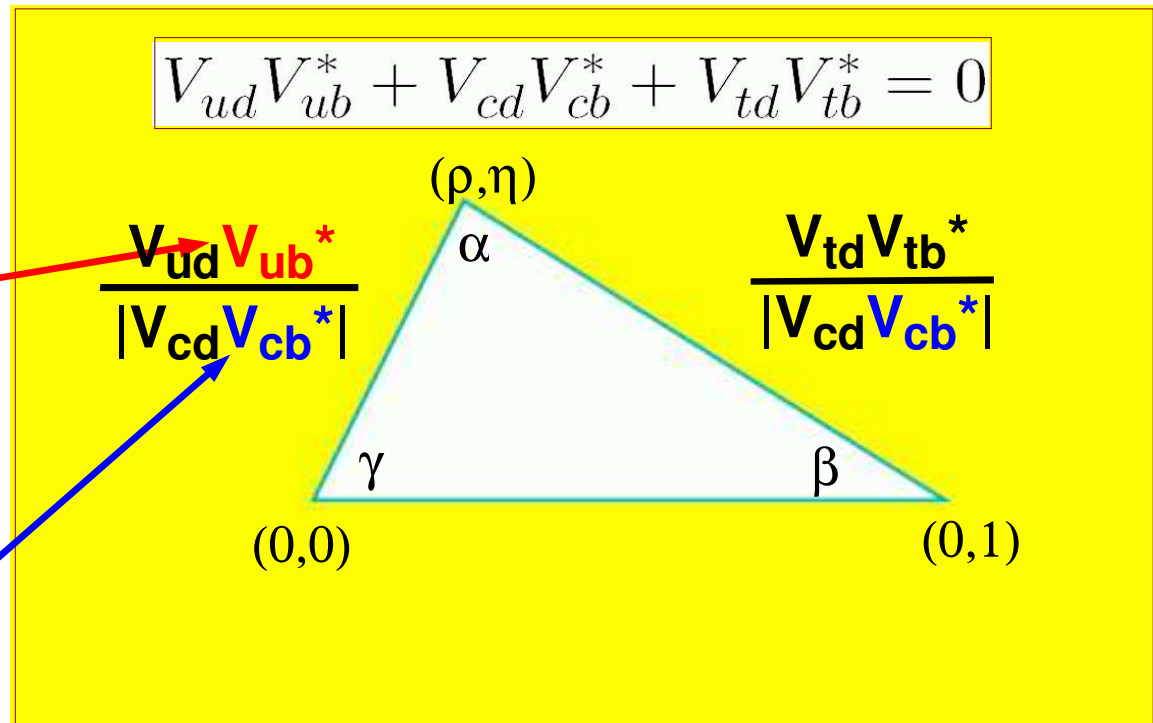
Semileptonic B decays
provide observables for V_{xb}
CKM elements extraction

Exclusive $B^0 \rightarrow \rho^- l \nu$
published on PRL
& $B^+ \rightarrow \pi^0, \rho^0, \omega l \nu$
preliminary result of Br

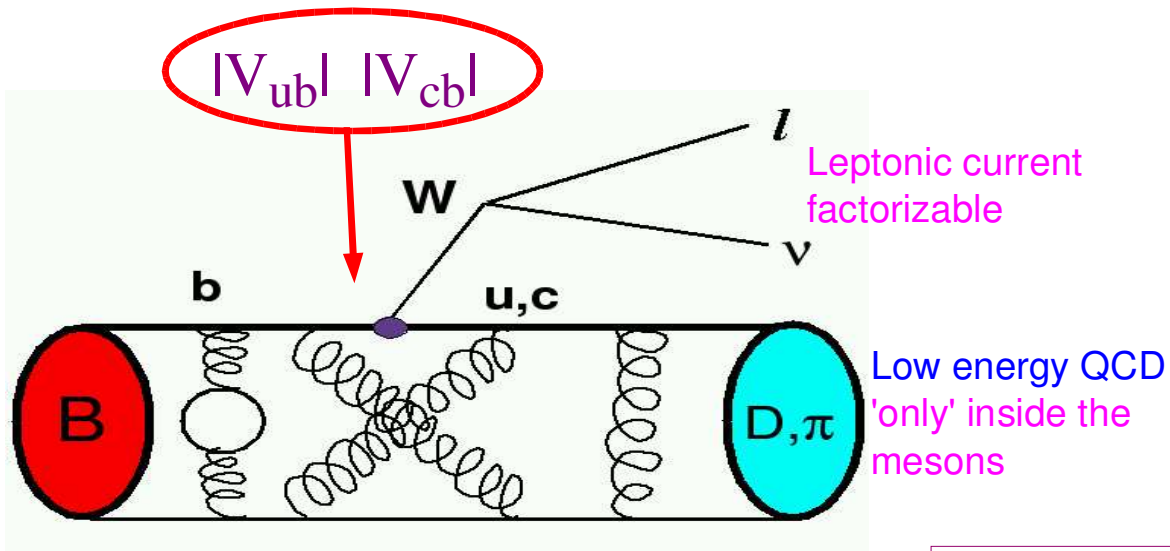
Exclusive $B^0 \rightarrow D^* l \nu$
preliminary result

Decays studied using
 $e^+e^- \rightarrow Y(4S)$ events

Measurements based on:
 $\sim 80 \text{ fb}^{-1}$ at the $Y(4S)$ mass
 $\sim 9 \text{ fb}^{-1}$ 40 MeV below



How to measure $|V_{cb}|$ & $|V_{ub}|$?



QCD corrections needed to extract the EW physics

Exclusive methods:

$B \rightarrow D, \pi, \rho, \omega$ **current** parameterized with Form Factors

$$\frac{d\Gamma}{dq^2} \propto |V_{xb}|^2 \mathcal{F}^2(q^2) \mathcal{G}(q^2)$$

pseudoscalar meson 1 FF
vector meson 3 FF

$B \rightarrow D, D^*$

HQS & HQET

$B \rightarrow \pi, \rho, \omega$

light quark in the final state!

Main source of uncertainties for the $|V_{xb}|$ extraction

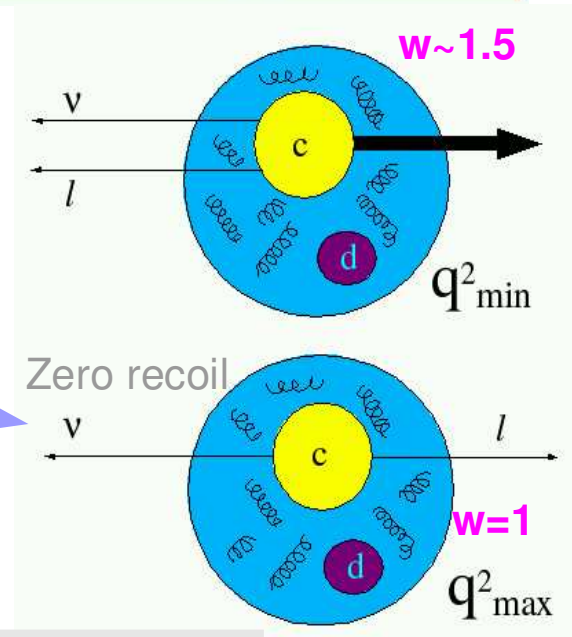
$|V_{cb}|$ with $B \rightarrow D^* l \nu$ decay

$$\frac{d\Gamma}{dw} \propto |V_{cb}|^2 \mathcal{F}^2(w) \mathcal{G}(w)$$

$$w = v_B \cdot v_{D^*} = \frac{m_B^2 + m_{D^*}^2 - q^2}{2m_B m_{D^*}}$$

$B \rightarrow D^*$ Form Factor (3 f.f.)

D^* boost in the B rest frame



- HQS:

$m_Q \rightarrow \infty$ limit at **zero recoil** $\mathcal{F}(1) \rightarrow \xi(1) = 1$
(Isgur-Wise)

- Zero recoil: rate $\rightarrow 0$

$B \rightarrow D^* l \nu$ helicity suppression $(w-1)^{1/2}$
at **Y(4S)** reconstruction efficiency $\rightarrow 0$ (charged soft pion)

Strategy:

Measure $d\Gamma/dw$, extrapolate to $w=1 \rightarrow \mathcal{F}(1)|V_{cb}|$

- HQET provide shapes $\mathcal{F}(w)$

- Lattice QCD correction to $\mathcal{F}(1)$

Exclusive $|V_{cb}|$: extrapolation to $w=1$

- $\mathcal{F}(w) = \mathcal{F}(1)(1 + \rho^2(w-1) + c(w-1)^2 + O(w-1)^3)$
- Dispersion relations: constraints to the shape [$c=f(\rho^2)$]

Boyd Grinstein Lellouch
Phys. Rev. D56
Caprini Lellouch Nebert
Nucl. Phys. B530

$$\frac{d\Gamma}{dw} \propto |V_{cb}|^2 A_1^2(w) \left\{ 2 \frac{1-2wr+r^2}{(1-r)^2} \left[1 + \frac{w-1}{w+1} R_1(w)^2 \right] + \left[1 + \frac{w-1}{1-r} (1-R_2(w)) \right]^2 \right\}$$

$$A_1(w) = A_1(1) \left[1 - 8\rho_{A_1}^2 z + (53\rho_{A_1}^2 - 15)z^2 - (231\rho_{A_1}^2 - 91)z^3 \right] \quad z = \frac{\sqrt{w+1} - \sqrt{2}}{\sqrt{w+1} + \sqrt{2}}$$

FIT: 2 free parameters $\mathcal{F}(1)|V_{cb}|$ & ρ_A^2 strongly correlated

QCD sum rules \rightarrow R1 & R2 shapes

$$R_1(w) \approx 1.27 - 0.12(w-1) + 0.05(w-1)^2 \quad R_2(w) \approx 0.80 + 0.11(w-1) - 0.06(w-1)^2$$

CLEO measurements at $w=1$

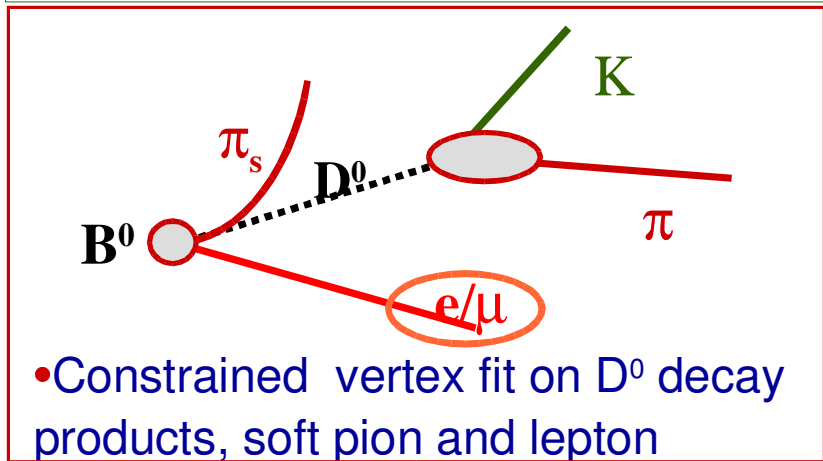
$$R_1(1) = 1.18 \pm 0.30 \pm 0.12 \quad R_2(1) = 0.71 \pm 0.22 \pm 0.07$$

Most important source of systematic error on ρ_A^2

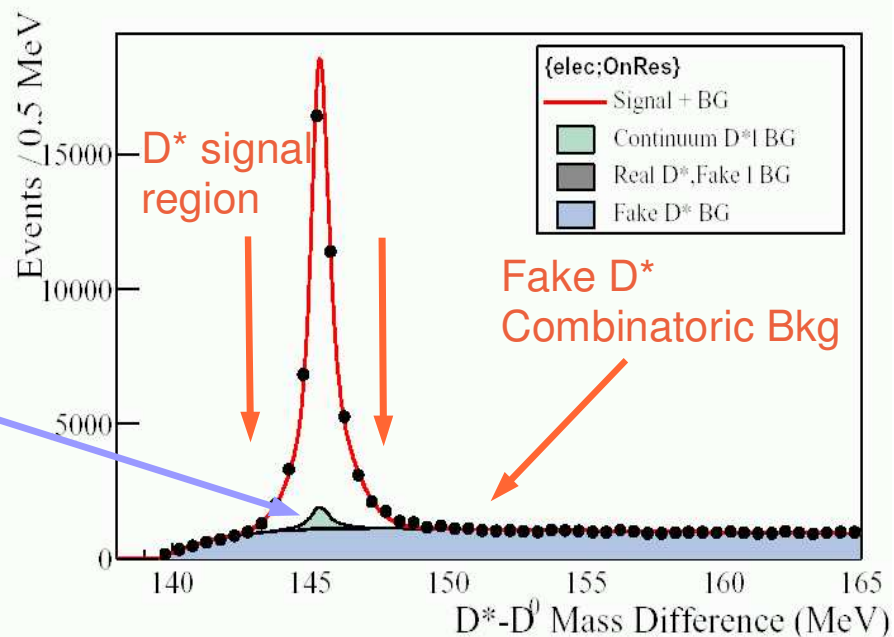
Exclusive $|V_{cb}|$: $B^0 \rightarrow D^{*-} l^+ \nu$ sample

$B^0 \rightarrow D^{*-} l^+ \nu$ reconstruction

- $D^{*-} \rightarrow D^0 \pi^-$ High energy lepton:
e & μ with $P_l > 1.2 \text{ GeV}/c$
- $D^0 \rightarrow K\pi, K3\pi, K\pi\pi^0$



Decay mode	BR (%)
$D^{*\pm} \rightarrow D^0 \pi^\pm$	67.7 ± 0.5
$D^0 \rightarrow K\pi$	3.80 ± 0.09
$D^0 \rightarrow K\pi\pi\pi$	7.46 ± 0.31
$D^0 \rightarrow K\pi\pi^0$	13.1 ± 0.9



Combinatoric: ΔM side band

Continuum $e^+e^- \rightarrow qq \rightarrow D^*X$: off peak data

Fake lepton: tracks failing lepton-ID

Correlated: $B^0 \rightarrow D^* X_c / \tau$

$B_1 \rightarrow D^* X, B_2 \rightarrow l Y$ (uncorrelated)

$B \rightarrow D^* X l \nu$ (D^{**} background)

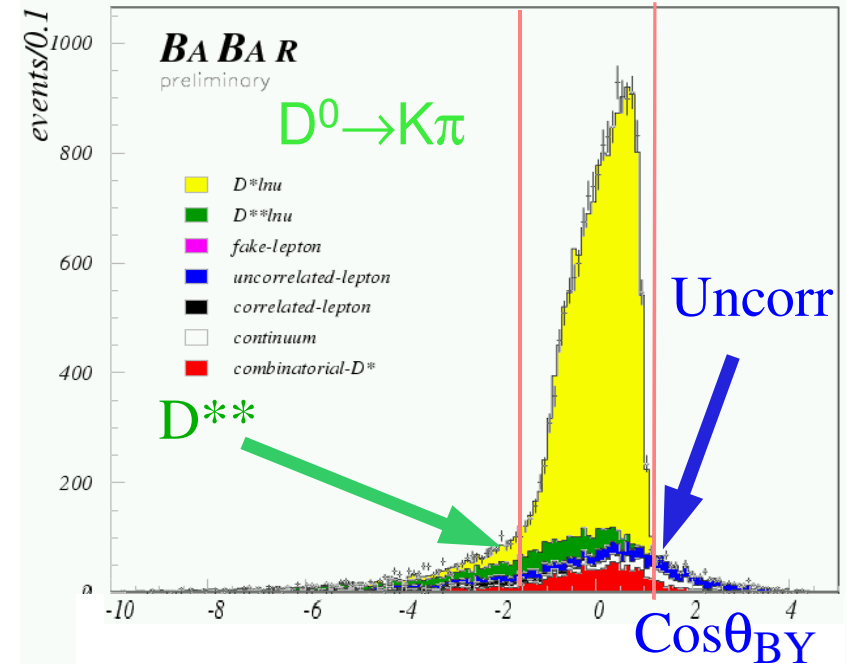
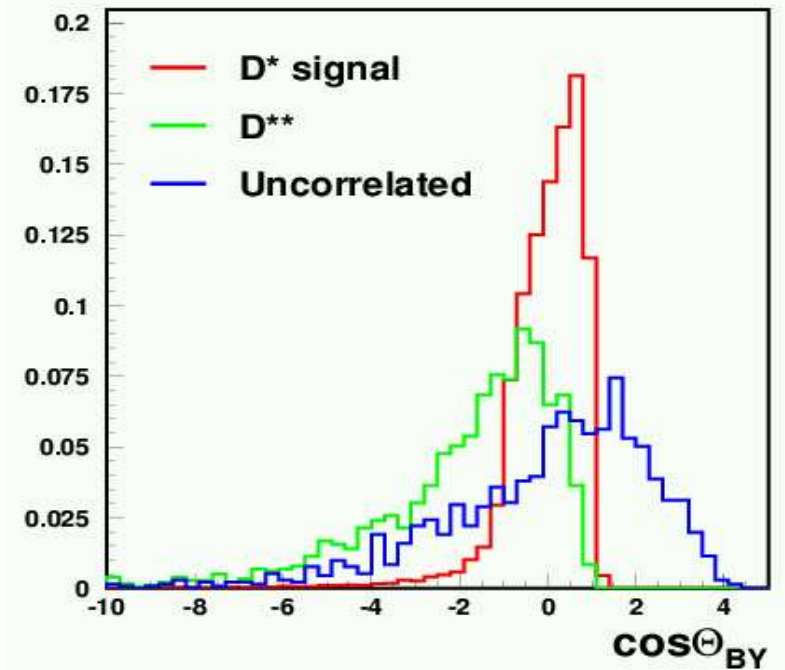
Next slide

55,000 events in the signal region!

Peaking background evaluation: D^{**} & Uncorr.

$$\cos \theta_{B^0, D^* \ell} = \frac{-(m_{B^0}^2 + m_{D^* \ell}^2 - 2 E_{B^0} E_{D^* \ell}) + m_{X\nu}^2}{2 |\vec{p}_{B^0}| |\vec{p}_{D^* \ell}|}$$

Fixed to 0 in the ν hypothesis



- determine the **fraction of D^{**} & uncorrelated** fitting $\cos \theta_{B, \gamma}$
- fit performed in **each w bin**
- constrain D^{**}/D^* and Uncorr/D^* ratios to be the same for each lepton and D^0 mode

Exclusive $|V_{cb}|$: dN/dw fit results

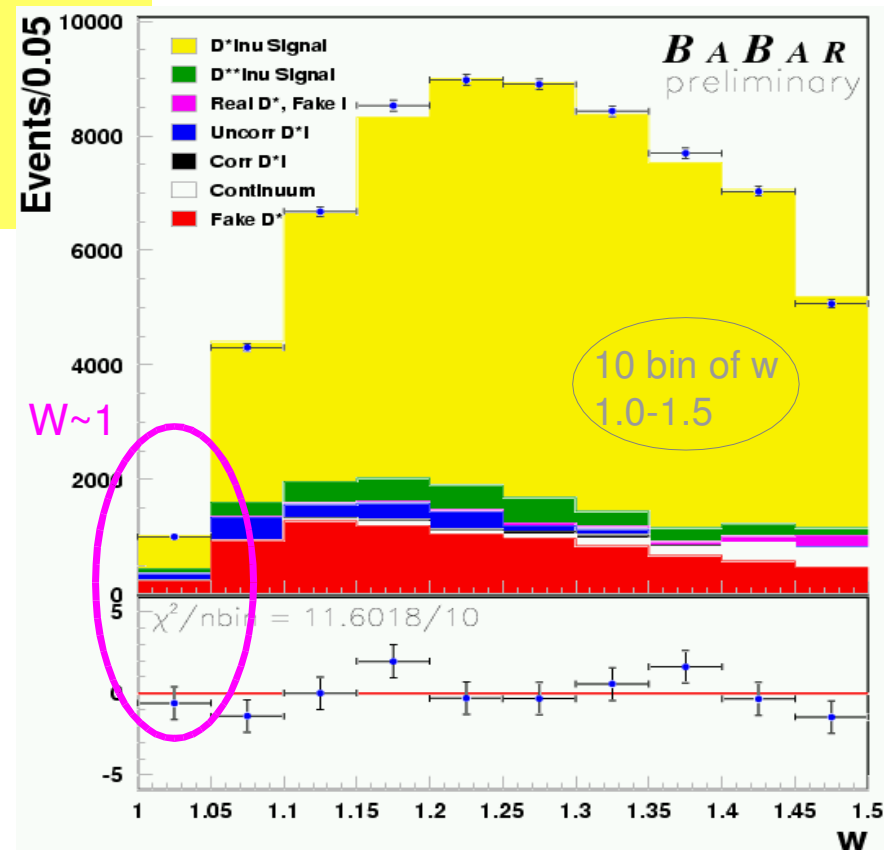
$$\frac{d\mathcal{N}}{dw} = 4 N_T f_{00} \mathcal{B}(D^{*+} \rightarrow D^0 \pi_{\text{slow}}^+) \mathcal{B}(D^0 \rightarrow K^- n\pi) \epsilon(w) \frac{d\mathcal{B}}{dw}$$

$$\mathcal{F}(1)|V_{cb}| = (34.03 \pm 0.24_{\text{stat}} \pm 1.31_{\text{syst}}) \times 10^{-3}$$

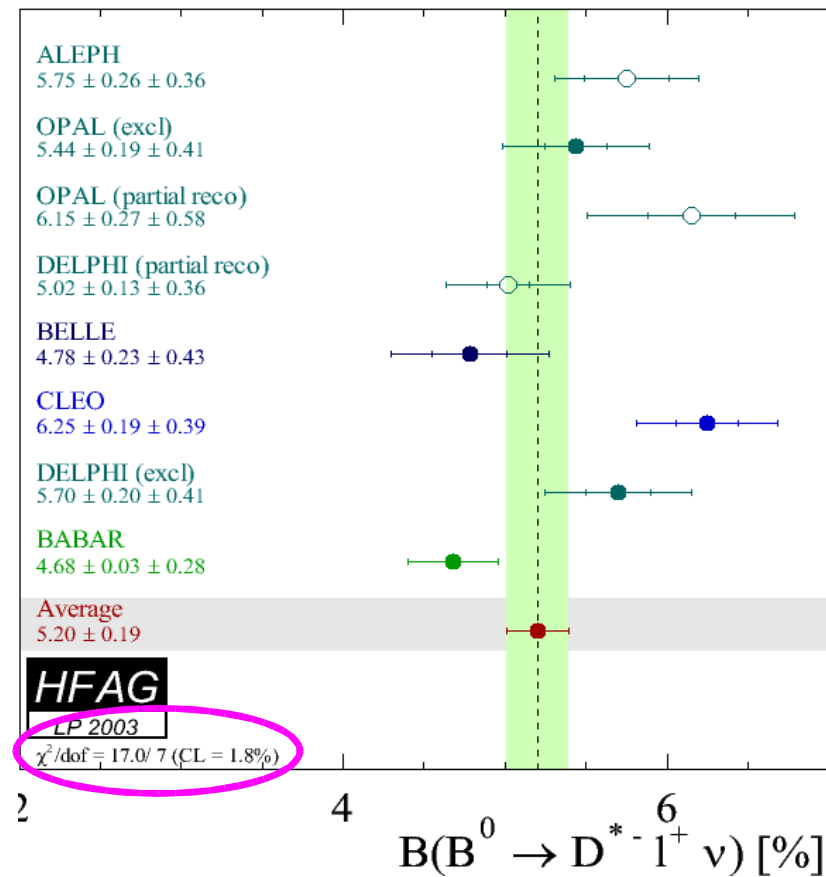
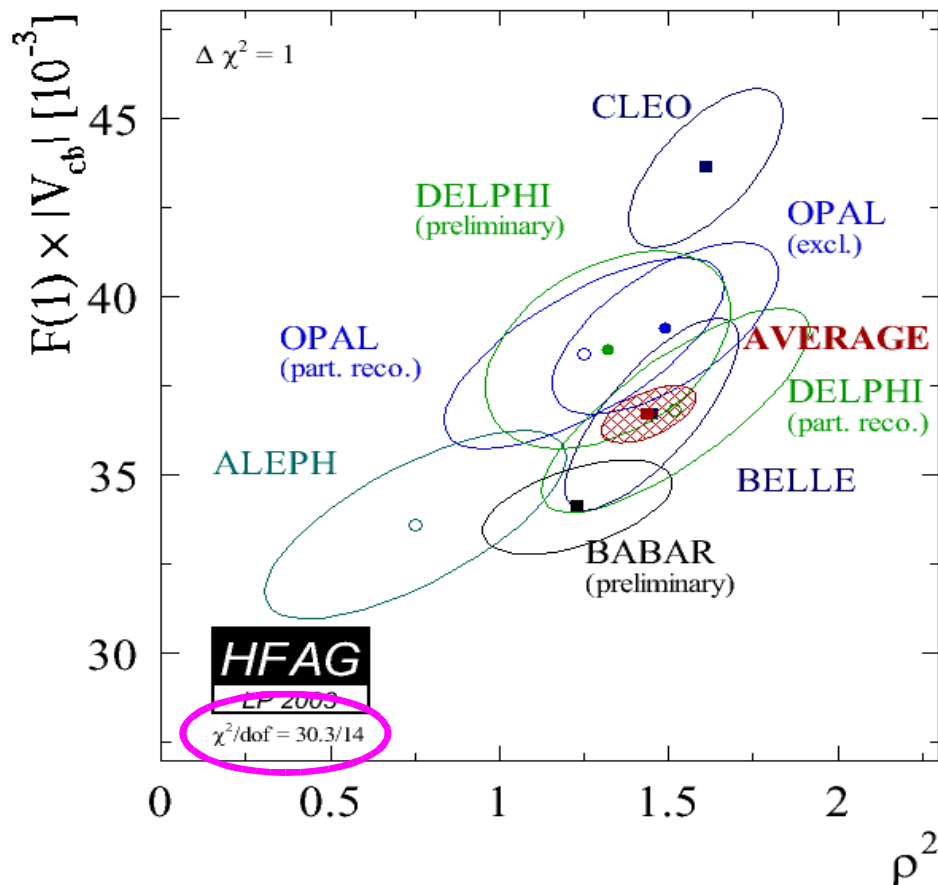
$$\rho_A^2 = 1.23 \pm 0.02_{\text{stat}} \pm 0.28_{\text{syst}}$$

$$\mathcal{B}(B^0 \rightarrow D^* l \nu) = (4.69 \pm 0.02 \pm 0.24)\%$$

error contribution	$\delta\mathcal{F}(1) V_{cb} /\mathcal{F}(1) V_{cb} * 10^{-3}$	$\delta\mathcal{B}/\mathcal{B}(\%)$
statistics	0.7	0.8
π_{slow} efficiency	1.3	1.9
tracking efficiency	1.3	2.7
D^* background composition	1.8	2.0
$R_1(1)$ and $R_2(1)$	1.8	1.8
.....
Total sys uncorrelated	3.4	5.0
$\mathcal{B}(Y(4S) \in B^0 B^0)$	1.3	2.7
.....
Total sys correlated	1.8	3.5



Exclusive $|V_{cb}|$: comparison of $F(1)|V_{cb}|$



$$\mathcal{F}(1)|V_{cb}| = (36.7 \pm 0.8) \times 10^{-3}$$

$$\rho_A^2 = 1.44 \pm 0.14$$

$$\text{Br} = (5.20 \pm 0.19)\%$$

Exclusive $B^{+0} \rightarrow \rho^{0/+} l \bar{\nu}$ decays: selection

- $B \rightarrow \rho^{\pm} l \bar{\nu}$, $B \rightarrow \rho^0 l \bar{\nu}$, $B \rightarrow \omega l \bar{\nu}$
- Neutrino reconstruction
 - Require **hermeticity**

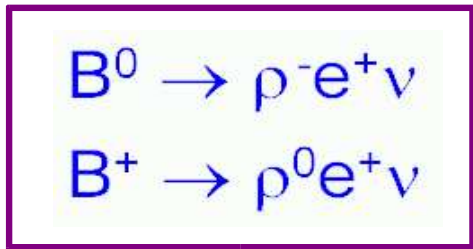
Analysis optimized for $\rho^{\pm} l \bar{\nu}$

$$\vec{p}_{\text{miss}} = - \sum_{\text{tracks}} \vec{p}_i - \sum_{\text{photons}} \vec{p}_i$$

- Extraction of the Yields:
 - Fit the $M_{\pi\pi(\pi)}$ vs ΔE ($=E_{\text{had}}+E_e+E_{\nu}-E_{\text{beam}}$) in **2 coarse bin of p_l**
 - High efficiency but **sensitivity in the region $p_l > 2.3 \text{ GeV}/c$**
- Isospin/quark-model constraints:

$$\begin{aligned} \Gamma(B^0 \rightarrow \rho^-) &= 2\Gamma(B^+ \rightarrow \rho^0) \\ &\sim 2\Gamma(B^+ \rightarrow \omega) \end{aligned}$$

Exclusive $B^{+0} \rightarrow \rho^{0/+} l \bar{\nu}$ decays

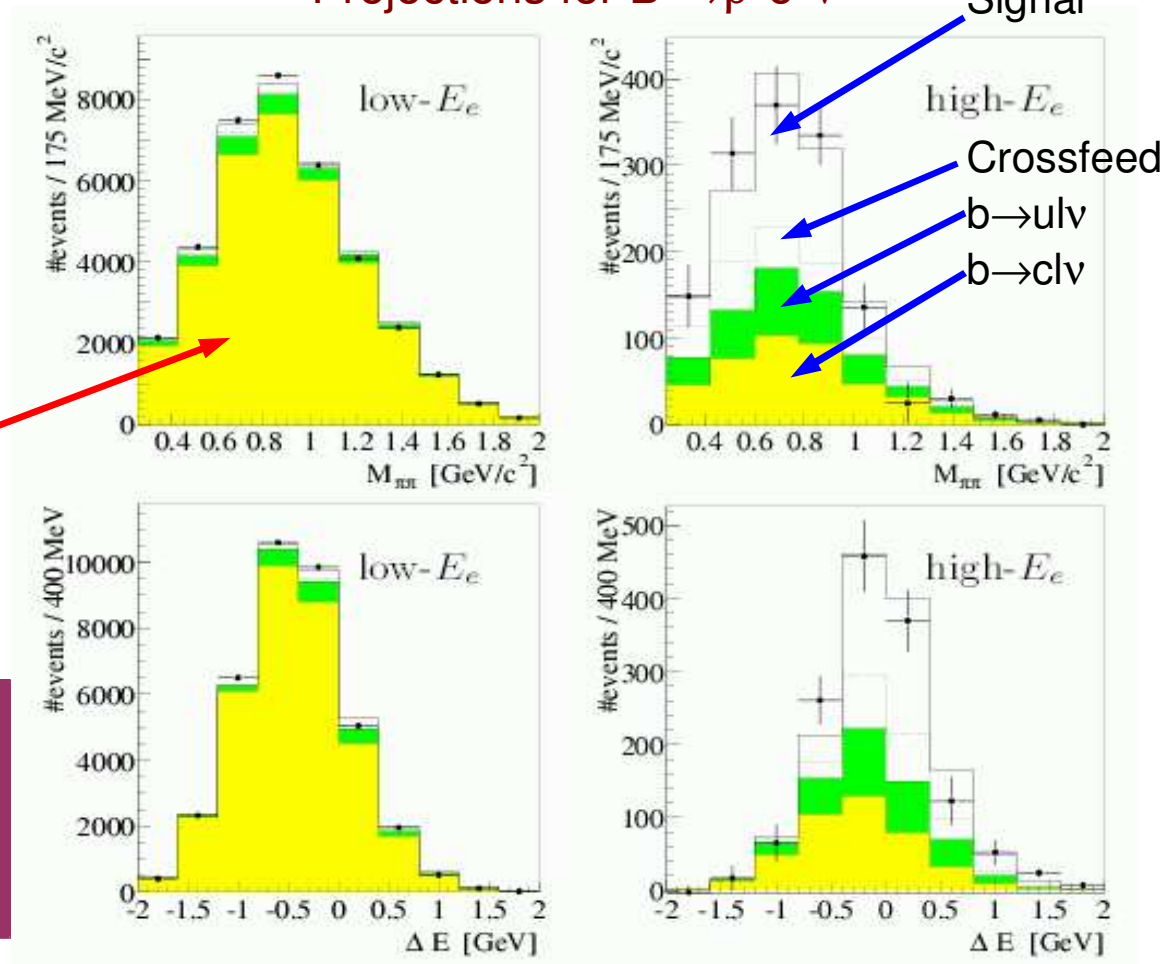


High E_l : 2.3-2.7 GeV
signal enriched

Low E_l : 2.0-2.3 GeV
background estimation

Yield in the High E_l region
 $B \rightarrow \rho^+ \rightarrow 505 \pm 63$
 $B \rightarrow \rho^0 \rightarrow 321 \pm 40$

Projections for $B^0 \rightarrow \rho^- e^+ \nu$



Continuum subtracted plots

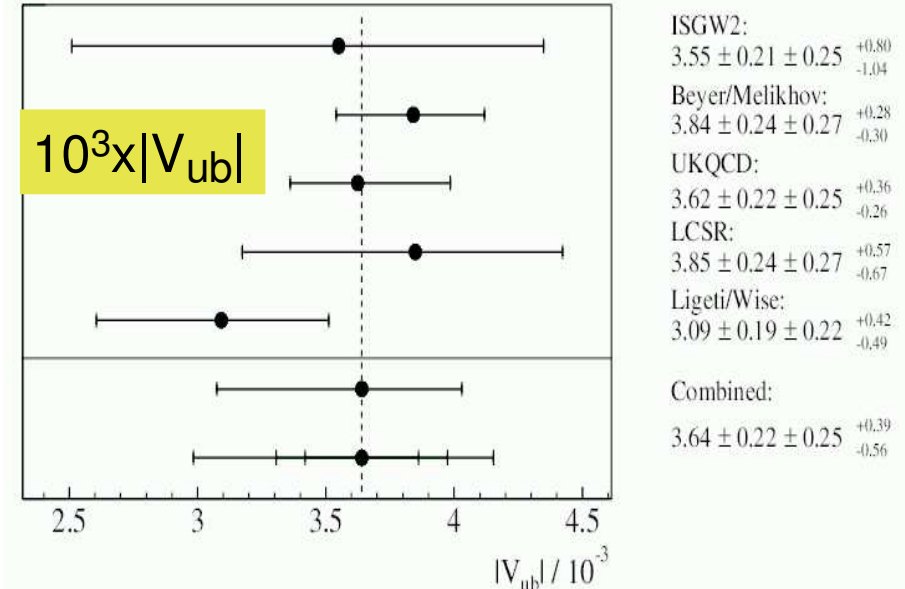
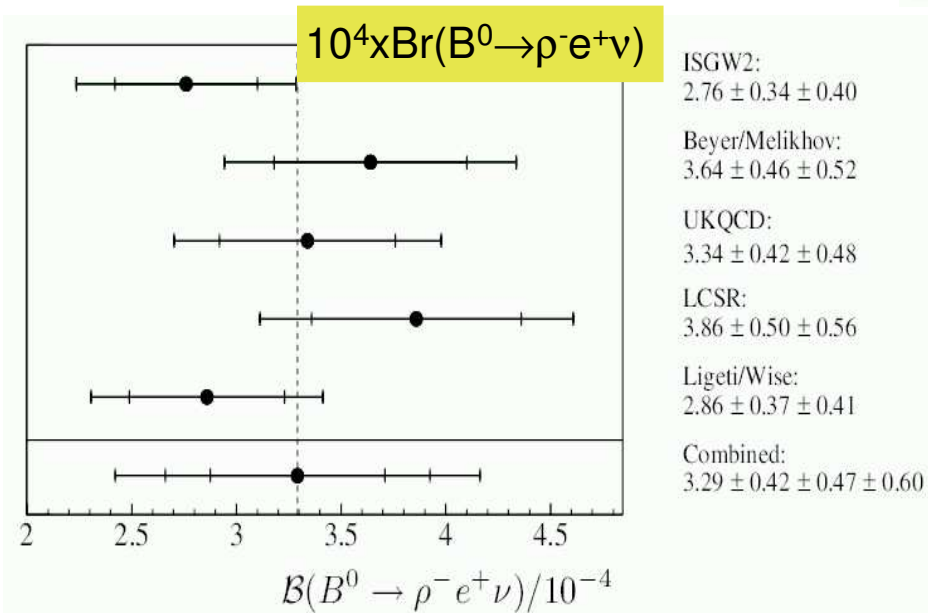
Continuum is the largest source of background

Exclusive $B^{+0} \rightarrow \rho^{0/+} l \bar{\nu}$: BR & $|V_{ub}|$

- [1] PRD52,2783
- [2] PLB436,344
- [3] PLB416,392
- [4] PRD58,094016
- [5] PRD53,4937

$$|V_{ub}| = \sqrt{\mathcal{B}(B^0 \rightarrow \rho^- e^+ \nu) / (\tilde{\Gamma}_{th} \tau_{B^0})}$$

Form factors	$\tilde{\Gamma}_{th}$ (ps ⁻¹)	Error (%)	Reference
ISGW2	14.2	±50	[1]
Beyer/Melikhov	16.0	±15	[2]
UKQCD	16.5	+21, -14	[3]
LCSR	16.9	±32	[4]
Ligeti/Wise	19.4	±29	[5]



$$|V_{ub}| = (3.64 \pm 0.22 \pm 0.25 \begin{matrix} +.39 \\ -.56 \end{matrix}) \times 10^{-3}$$

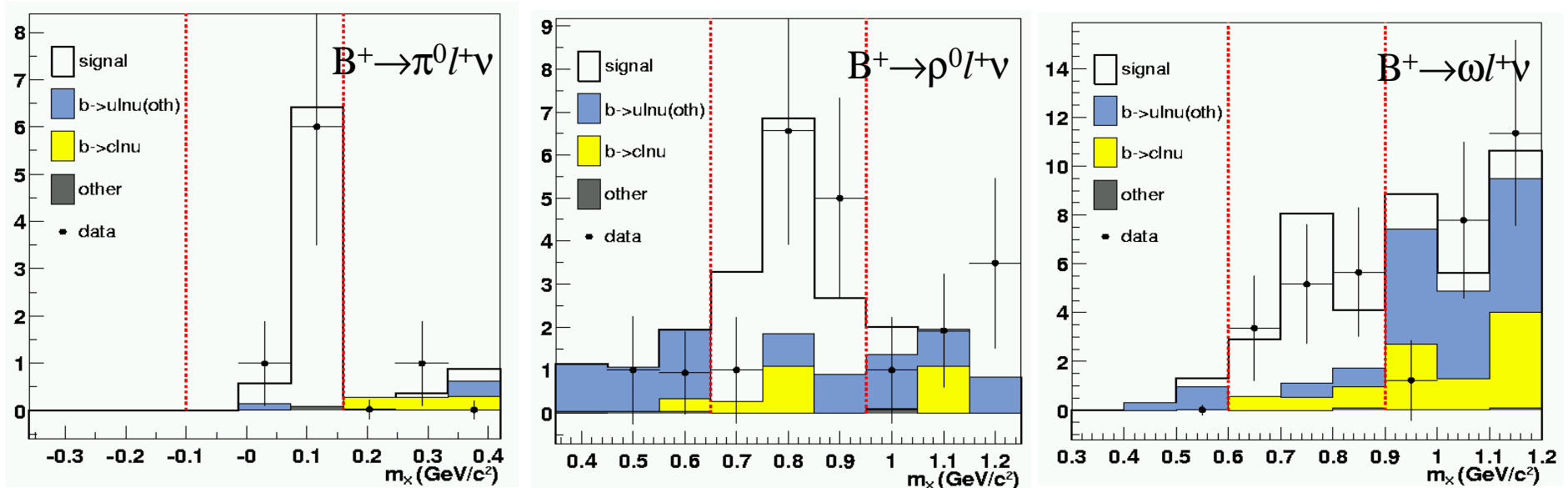
Exclusive $B^+ \rightarrow \pi^0, \rho^0, \omega l \nu$ decays

B recoil technique: as in inclusive V_{ub} analysis

- Small statistics
- Very high purity
- Loose cuts
 - small model dependence

$$\begin{cases} \mathcal{B}(B^+ \rightarrow \pi^0 l^+ \nu) = (0.78 \pm 0.32_{stat} \pm 0.13_{syst}) \cdot 10^{-4} \\ \mathcal{B}(B^+ \rightarrow \rho^0 l^+ \nu) = (0.99 \pm 0.37_{stat} \pm 0.19_{syst}) \cdot 10^{-4} \\ \mathcal{B}(B^+ \rightarrow \omega l^+ \nu) = (2.20 \pm 0.92_{stat} \pm 0.57_{syst}) \cdot 10^{-4} \end{cases}$$

Projection of the results on the m_x variable



Summary I: V_{cb}

- $|V_{cb}|$ via differential analysis with $B^0 \rightarrow D^* l \nu$

$$\text{BR}(B^0 \rightarrow D^* l \nu) = (4.69 \pm 0.02 \pm 0.24)\%$$

$$\mathcal{F}(1)|V_{cb}| = (34.03 \pm 0.24_{\text{stat}} \pm 1.31_{\text{syst}}) \times 10^{-3}$$

$$|V_{cb}| = (37.27 \pm 0.26_{\text{stat}} \pm 1.43_{\text{syst}} \pm 1.50_{-1.20}^{F(1)}) \times 10^{-3}$$

Preliminary result
hep-ex/0308027

$$\mathcal{F}(1) = 0.913^{+0.030}_{-0.035}$$

Lattice QCD

- **Experimental error O(4%)**
- **Very large sample**
 - Small statistical error
 - Background constrained from Data

Summary II: V_{ub}

- $|V_{ub}|$ analysis with $B \rightarrow \rho^\pm l \nu$ experimental error 9%

$$\text{BR}(B \rightarrow \rho^\pm l \nu) = (3.29 \pm 0.42 \pm 0.47 \pm 0.60) \times 10^{-4}$$

PR L.90:181801

$$|V_{ub}| = (3.64 \pm 0.22 \pm 0.25 \begin{matrix} +.39 \\ -.56 \end{matrix}) \times 10^{-3}$$

- BR of many charmless semileptonic B decays with **fully reconstructed events**

$$\begin{cases} \mathcal{B}(B^+ \rightarrow \pi^0 l^+ \nu) = (0.78 \pm 0.32_{stat} \pm 0.13_{syst}) \cdot 10^{-4} \\ \mathcal{B}(B^+ \rightarrow \rho^0 l^+ \nu) = (0.99 \pm 0.37_{stat} \pm 0.19_{syst}) \cdot 10^{-4} \\ \mathcal{B}(B^+ \rightarrow \omega l^+ \nu) = (2.20 \pm 0.92_{stat} \pm 0.57_{syst}) \cdot 10^{-4} \end{cases}$$

*Preliminary result
LP03*

- Working on converting BR in V_{ub}
- Promising with the increase of the luminosity

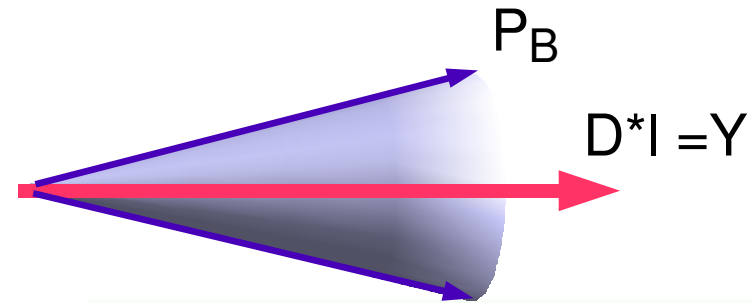
Backup slides

$B^0 \rightarrow D^* l^+ \nu$: reconstruction of w

$$w = v_B \cdot v_{D^*} = \frac{m_B^2 + m_{D^*}^2 - q^2}{2m_B m_{D^*}} \quad q^2 = (p_B - p_{D^*})^2 = (p_l + p_\nu)^2$$

Problem: we ignore the **B** direction (2 unknowns)
 one constraint: $m_\nu=0$

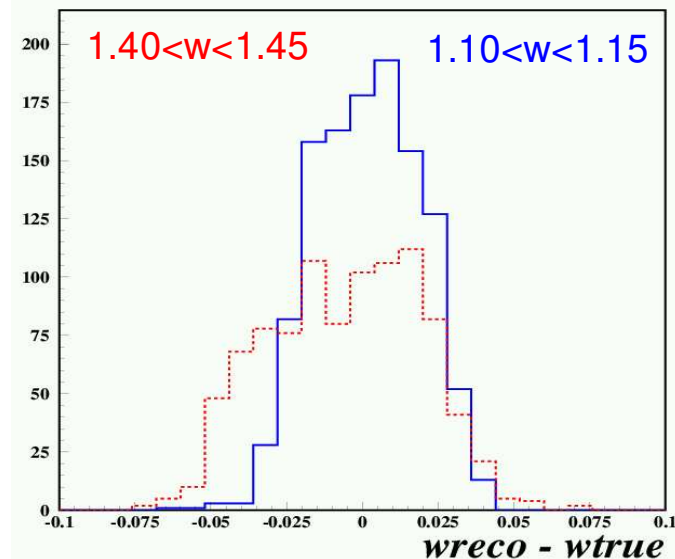
$$\cos(\theta_{B^0 Y}) = \frac{-(M_{B^0}^2 + M_Y^2 - 2E_{B^0} E_Y)}{2p_{B^0} p_Y}$$



Consider extreme solutions:

- **max** and **min** angle between **B** and **D***
- consistent with $\cos(BY)$ and $\cos(D^*Y)$

$$\tilde{w} = \frac{w_{min} + w_{max}}{2}$$



$B^0 \rightarrow D^{*-} l^+ \nu$: selection cuts

- Lepton Candidates from GoodTrackList
 - $P_{lep} > 1.2 \text{ GeV}/c$
 - PID: veryTight selector
- D^0 tracks from GoodTrackLoose: 12 hits in the DCH
 - Kaon: **not a Pion** for Kpi, **Tight** for Kpipi0 and K3pi
- Pi soft:
 - $p_{\pi \text{ soft}} < 450 \text{ MeV}$ and $p_{\pi \text{ soft}}^t > 50 \text{ MeV}$
- D^* candidate
 - Vertex fit $\chi^2 > 1\%$
 - $144 \text{ MeV} < \delta M < 147 \text{ MeV}$ (SVT+DCH)
 - $143 \text{ MeV} < \delta M < 148 \text{ MeV}$ (SVT only)
- $\cos \theta_{D^*l} < 0$ (Opposite Side sample)
- $|\cos \theta_{B,\gamma}| < 1.2$

$B^0 \rightarrow D^{*-} \ell^+ \nu$: D^{**} systematic errors

B decay mode	B $\times 10^{-2}$	Model	D^{**} decay	B	Overall BR $\times 10^{-4}$
$B^0 \rightarrow D^{*-} \pi^0 \ell^+ \nu_\ell$	0.10	GR	—	—	10.
$B^0 \rightarrow D_1^- \ell^+ \nu_\ell$	0.56	ISGW2	$D_1^- \rightarrow D^{*-} \pi^0$	0.33	18.5
$B^0 \rightarrow D_1^{*-} \ell^+ \nu_\ell$	0.37	ISGW2	$D_1^{*-} \rightarrow D^{*-} \pi^0$	0.33	12.2
$B^0 \rightarrow D_2^{*-} \ell^+ \nu_\ell$	0.37	ISGW2	$D_2^{*-} \rightarrow D^{*-} \pi^0$	0.103	3.81
$B^0 \rightarrow D'^- \ell^+ \nu_\ell$	0.02	ISGW2	$D'^- \rightarrow D^{*-} \pi^0$	0.33	0.67
$B^0 \rightarrow D^{*'} \ell^+ \nu_\ell$	0.22	ISGW2	$D^{*'} \rightarrow D^{*-} \pi^0$	0.17	3.74
$B^+ \rightarrow D^{*-} \pi^+ \ell^+ \nu_\ell$	0.20	GR	—	—	20.
$B^+ \rightarrow D_1^0 \ell^+ \nu_\ell$	0.56	ISGW2	$D_1^0 \rightarrow D^{*-} \pi^+$	0.67	37.5
$B^+ \rightarrow D_1^{*0} \ell^+ \nu_\ell$	0.37	ISGW2	$D_1^{*0} \rightarrow D^{*-} \pi^+$	0.67	24.8
$B^+ \rightarrow D_2^{*0} \ell^+ \nu_\ell$	0.37	ISGW2	$D_2^{*0} \rightarrow D^{*-} \pi^+$	0.21	7.78
$B^+ \rightarrow D'^0 \ell^+ \nu_\ell$	0.02	ISGW2	$D'^0 \rightarrow D^{*-} \pi^+$	0.67	1.32
$B^+ \rightarrow D^{*'} \ell^+ \nu_\ell$	0.22	ISGW2	$D^{*'} \rightarrow D^{*-} \pi^+$	0.33	7.26

Systematic error:

assuming only one mode a time;

repeat the cosBY and w fit: half the max and min values of the parameters

