

# B-tagging at the Tevatron

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- *Motivation*
- *Overview of b-tagging methods*
- *Measurement of b-tagging efficiency and mistagging rate*
- *b-tagging performance at the Tevatron*
- *Example of using b-tagging in top cross section measurement*
- *b-tagging at the LHC*
- *Conclusions*

# Motivation

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- B-tagging (b-jet identification) plays a crucial role for the high energy physics:
  - Top physics – all aspects ( $\text{Br}(t \rightarrow Wb) \sim 100\%$ )
  - Higgs physics – search for associated Higgs production
    - $(W/Z)H, H \rightarrow bb$
    - $Htt, H \rightarrow bb$
  - Searches for new physics
    - Stop, sbottom searches;
    - Technicolor searches
- Most of these applications require high b-tagging efficiency (probability to tag a b-jet)  $\sim 50$ — $60\%$  while keeping mistagging rate (probability to tag light jets originated from u/d/s-quarks and gluons) below 1%

# B-tagging algorithms (1)

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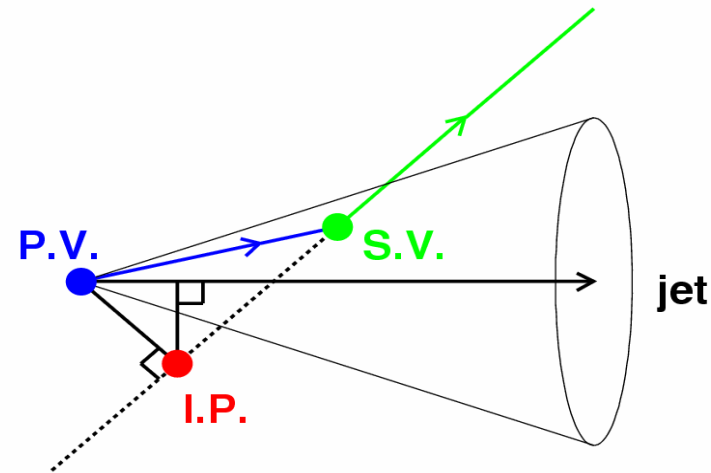
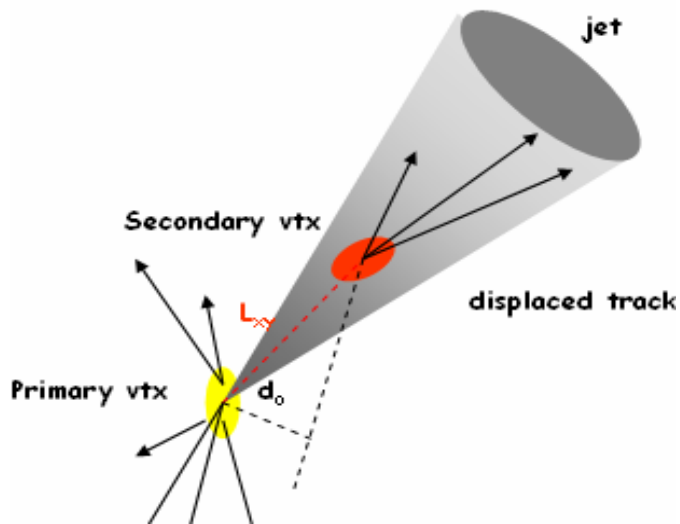
## ➤ Soft lepton tagging (SLT)

- Based on the fact that  $\sim 20\%$  of  $b$ -hadrons decay semileptonically (either  $e$  or  $\mu$  in the final state)
- Usually do not use electrons – big challenge;
- Once having preselected jets with muons, SLT has high efficiency, but high mistag rate as well
- Purity of this tagger can be improved using kinematic variables of muon, for example, using  $p_{\text{Trel}} - p_{\text{T}}$  of muon with respect to jet axis (muons from  $b$ -decays tend to have larger  $p_{\text{Trel}}$ )

# B-tagging algorithms (2)

## ► Lifetime tagging

- Make use of relatively big lifetime of B-hadrons
- Two different techniques
  - Explicit reconstruction of secondary vertices in jets
  - Looking at tracks in jets which are significantly displaced from primary vertex (counting method or probabilistic approach)



# Lifetime b-tagging methods

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## Secondary Vertex Tag

- Look for displaced vertices
- Jet is tagged as a *b* jet if signed decay length significance > some value (depends on “acceptable” mistag rate)

## Counting Signed Impact Parameter tag (CSIP)

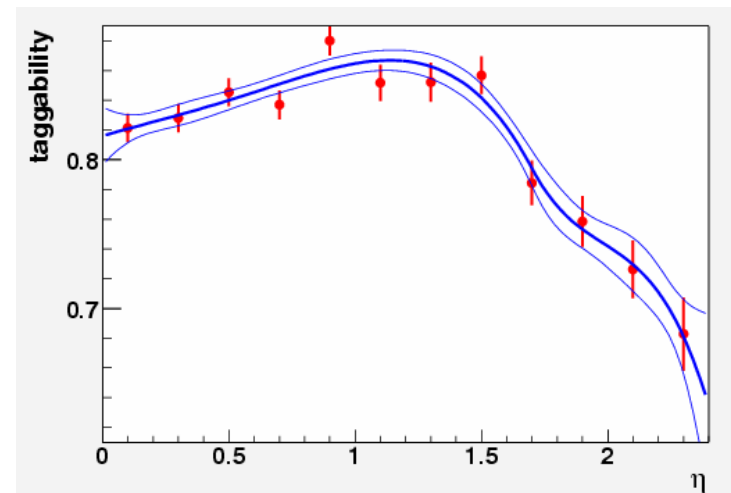
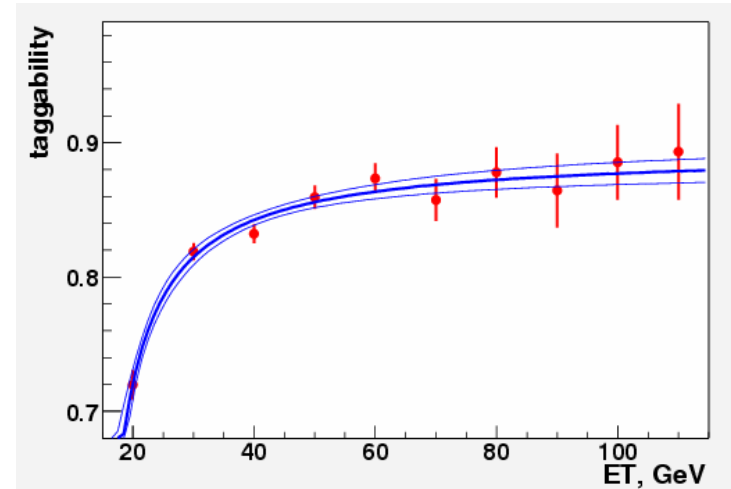
- $S = IP/\sigma(IP)$
- Jet is positively tagged if it has
  - at least two tracks with  $S > 3$  or
  - at least three tracks with  $S > 2$

## Jet Lifetime Probability

- For each track in the jet calculate a probability to come from primary vertex based on the IP significance;
- Combine probabilities for individual tracks into jet probability;
- Jet is tagged if its probability to be a light jet is less than some value (depends on “acceptable” mistag rate)

# Taggability

- The idea is to largely decouple the tagging efficiency from issues related to tracking inefficiencies and/or calorimeter noise;
- Is used by both experiments;
- Taggability is the probability for a jet to pass some quality criteria ( $D\phi$ ):
  - At least two tracks in track-jet associated with calorimeter jet
  - Certain criteria on  $p_T$  of tracks and on the number of hits per track
- Found that it depends on event sample and is not fully modeled by Monte Carlo



# How to measure b-tagging efficiency on data?

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- Ideal case (or Monte Carlo) : tag a sample of b-jets, so efficiency is the ratio of tagged jets to the total number of taggable jets
  - Data: mixture of light (dominant), c- and b-jets
    - Both numerator and denominator are affected by presence of non-b jets
  - Need separation between b and non-b jets
  - Requirement of soft lepton increases probability for a jet to be heavy flavor
- CDF: e-in-jets
    - $p_T(e) > 8$  GeV
    - Di-jet events
  - DØ:  $\mu$ -in-jets
    - $p_T(\mu) > 8$  GeV
    - Di-jet events

# Double tag method (CDF)

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- Enrich the di-jet sample with heavy flavor by tagging away jet;
- Subtract the number of mistags (tagged light jets) assuming it equal to the number of negative tags;
- The result is corrected for the fraction of non-QQbar events
  - Tagged away jet is a mistagged light jet or it comes from gluon splitting
  - Electron is fake or part of a conversion
- The correction factor involves
  - Efficiency to reconstruct conversions – measured on data
  - b/c ratio – measured on data, from  $D^0$  meson invariant mass fit or looking at  $\mu$  from cascade c-decays in e-jet.

- *b*-tagging efficiency:

$$\mathcal{E} = \frac{(N_{a+}^{e+} - N_{a+}^{e-}) - (N_{a-}^{e+} - N_{a-}^{e-})}{N_{a+} - N_{a-}} \cdot F_B^a$$



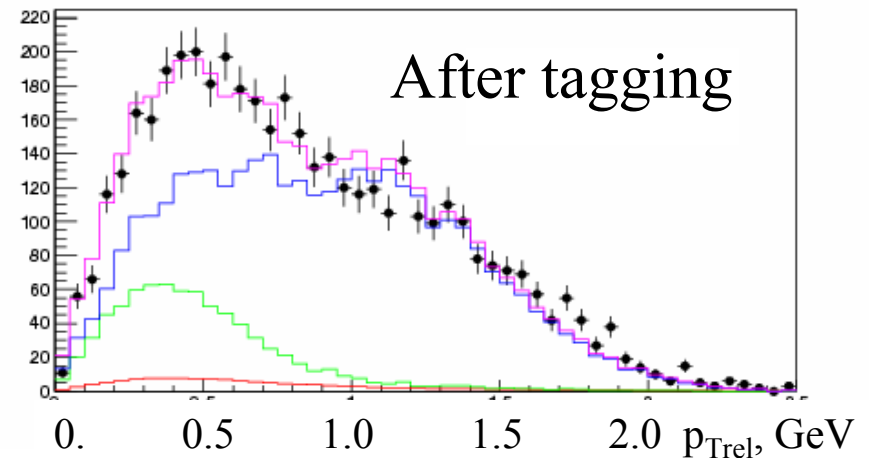
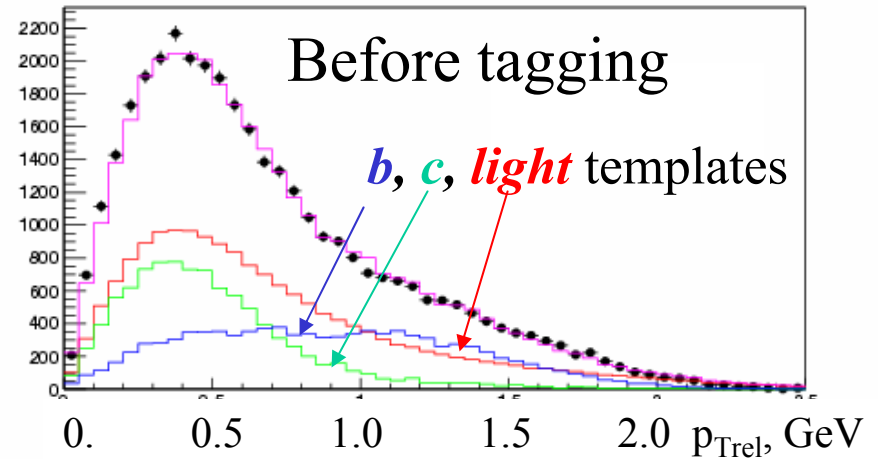
# $P_{Trel}$ method ( $D\cancel{\emptyset}$ )

- Look at muonic jets
- $p_{Trel}$  is different for  $\mu$  originated from light,  $c$  and  $b$ -decays – use this fact to measure fraction of  $b$ -jets before tagging ( $F_{b\rightarrow\mu}$ ) and after tagging ( $F_{b\rightarrow\mu}^{tag}$ )

Efficiency is calculated as

$$\mathcal{E}_{btag} = \frac{N_{\mu}^{tag} \cdot F_{b\rightarrow\mu}^{tag}}{N_{\mu} \cdot F_{b\rightarrow\mu}}$$

- Light template – obtained from data;
- $b, c$  templates obtained on MC



# System 8 (basic method at $D\emptyset$ )

- Have two samples with different heavy flavor fractions
  - $\mu$ -in-jet sample (n-sample)
  - The same sample with tagged away-jet (p-sample)
- Tag muonic jets with two independent tagging algorithms
  - Lifetime (LT = JLIP, CSIP or SVT)
  - SLT requiring  $p_{Trel} > 0.7$  GeV
- Write a system of eight equations to solve for  $\mathcal{E}_{btag}^{LT}$

$$n = n_b + n_l$$

$$p = p_b + p_l$$

$$n^{LT} = n_b \mathcal{E}_{btag}^{LT} + n_l \mathcal{E}_{non-b}^{LT}$$

**N of jets tagged by lifetime methods**

$$p^{LT} = p_b \mathcal{E}_{btag}^{LT} + p_l \mathcal{E}_{non-b}^{LT}$$

$$n^{SLT} = n_b \mathcal{E}_{btag}^{SLT} + n_l \mathcal{E}_{non-b}^{SLT}$$

**N of jets tagged by soft lepton tag**

$$p^{SLT} = p_b \mathcal{E}_{btag}^{SLT} + p_l \mathcal{E}_{non-b}^{SLT}$$

$$n^{dt} = n_b \mathcal{E}_{btag}^{LT} \mathcal{E}_{btag}^{SLT} + n_l \mathcal{E}_{non-btag}^{LT} \mathcal{E}_{non-b}^{SLT}$$

$$p^{dt} = p_b \mathcal{E}_{btag}^{LT} \mathcal{E}_{btag}^{SLT} + p_l \mathcal{E}_{non-btag}^{LT} \mathcal{E}_{non-b}^{SLT}$$

**N of jets tagged by both soft lepton tag and lifetime method (double tags)**

*Assume: decorrelation between taggers; cross checked it on MC, decorrelation factor 0.98*

# Main assumptions for $\epsilon_{b\text{tag}}$

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## ➤ Double tag, System8 methods:

- Probability to tag a jet with soft lepton does not depend on probability to tag away jet – not a big effect;
- There are jets originated from  $g \rightarrow bb$ , with both  $b$ -quarks in one jet – these jets presumably have higher tagging efficiency;
- Assume that gluon splitting contribution in MC is correct, both in shape and in size

## ➤ Double tag specific:

- $b/c$  ratio is constant as function of jet  $p_T$

# Main assumptions for $\epsilon_{b\text{tag}}$ (cont'd)

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## ➤ System8 specific:

- Have  $b$  and non- $b$  efficiencies:  $p_{\text{Trel}}$  (used to enhance HF fraction) templates do not distinguish between  $c$  and light jets;
- Cross-check with other  $b$ -tagging measurements and MC – got the same result within errors;

## ➤ $p_{\text{Trel}}$ fit method (templates obtained from MC):

- correct model of  $b$ -decays – checked with different generators, moderate effect;
- correct fragmentation model – almost no effect

Experimental limitation now – low statistics at high jet  $p_{\text{T}}$ , so have to rely on MC shape of  $b$ -tagging efficiency

# *b,c*-tagging efficiencies in data and MC

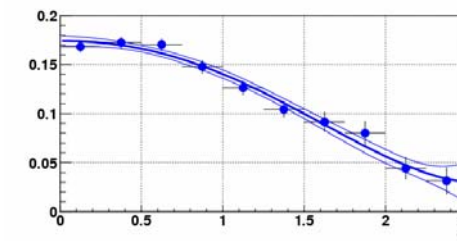
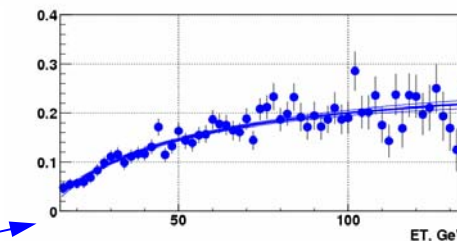
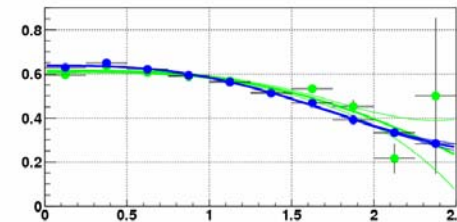
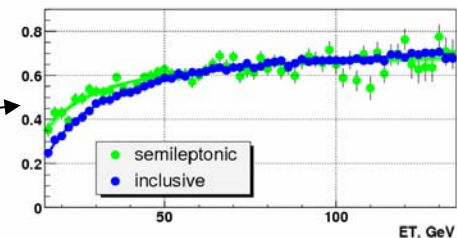
Both CDF and DØ measure semileptonic *b*-tagging efficiency on data;

Semileptonic *b*-tagging efficiency in MC is higher than measured in data – need to introduce a scale factor between data and MC (CSIP at DØ: 0.75; SecVtx at CDF: 0.82):

$$SF_{b \rightarrow \mu} = \mathcal{E}_{b \rightarrow \mu}^{data} / \mathcal{E}_{b \rightarrow \mu}^{MC}$$

Need inclusive *b*-tagging efficiency → assume the same data/MC ratio as for semileptonic jets

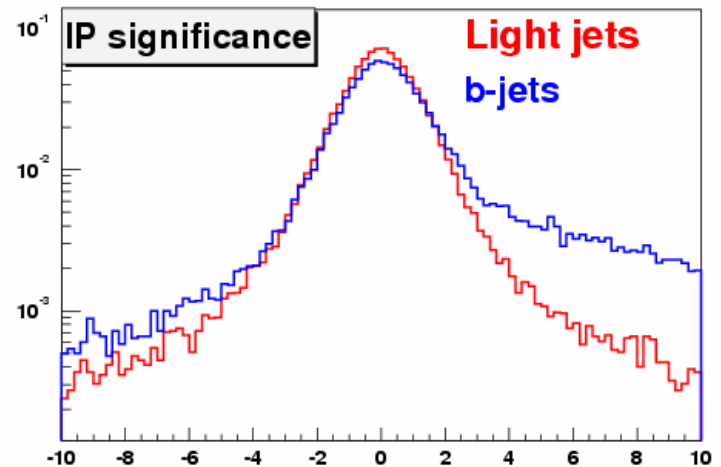
Do not measure *c*-tagging efficiency on data – instead, use MC *c*-tagging efficiency corrected by ratio of *b*-tagging efficiencies in data to MC.



# Measurement of mistagging rate in data

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- Measure negative inclusive tagging rate on data
  - Use negative side of DCA significance distribution (impact parameter based methods) or negative decay length (secondary vertex algorithms)
- Need to convert negative tagging rate into light jet tagging rate



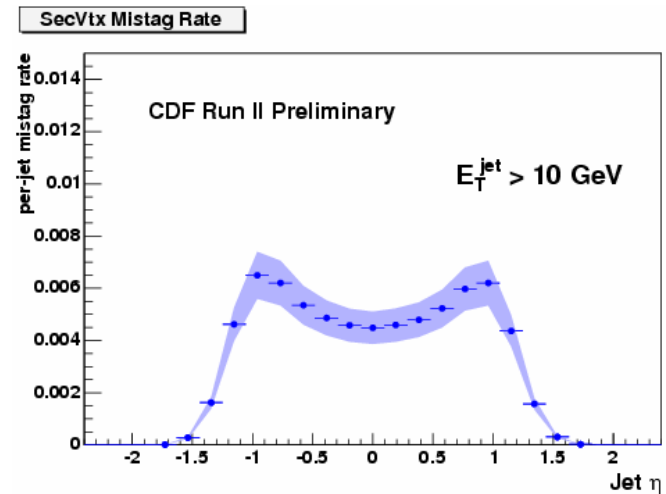
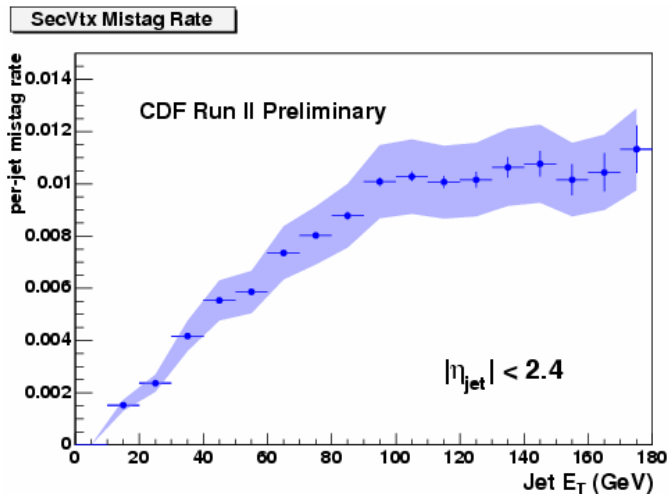
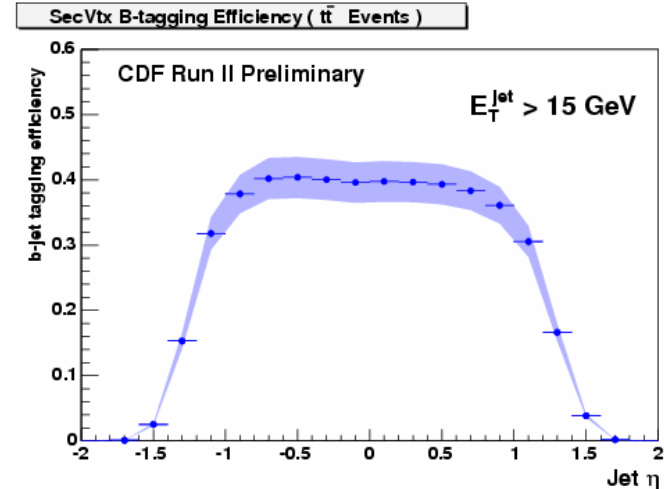
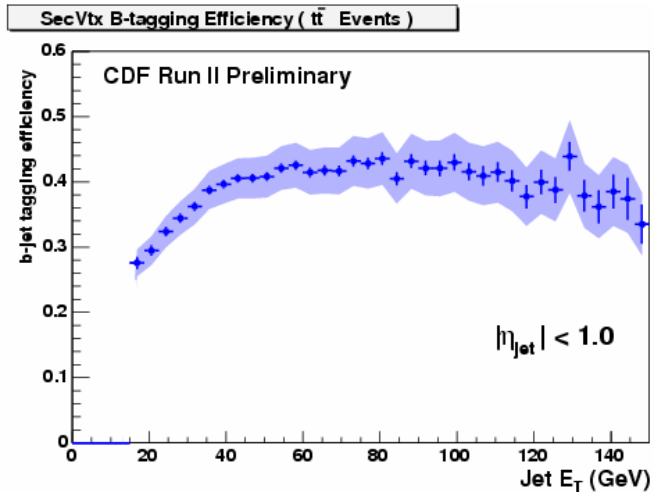
# Measurement of mistagging rate in data

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- Difference between light positive tag rate (mistags) and measured negative tag rate:
  - Fake tracks, long-lived particles not cleaned up by V0 filters, interactions with material give rise to positive tag rate – need scale factor  $SF_{ll}$ ;
    - Both experiments rely on MC for estimation of  $SF_{ll}$ ;
    - CDF has measured correction factor due to material interactions directly on data
  - Presence of heavy flavor in the negative tail artificially increases negative tag rate – introduce another scale factor  $SF_{hf}$
- Finally, mistagging rate is:

$$\varepsilon_{light}(x, y, \dots) = \varepsilon^-(x, y, \dots) \cdot SF_{hf} \cdot SF_{ll}$$

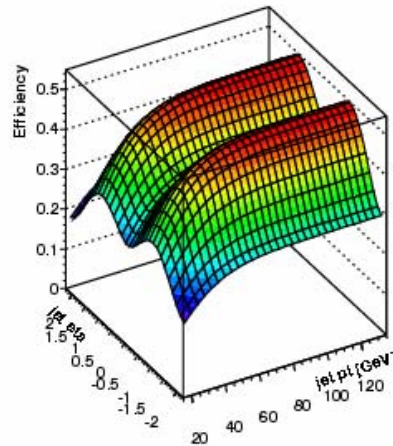
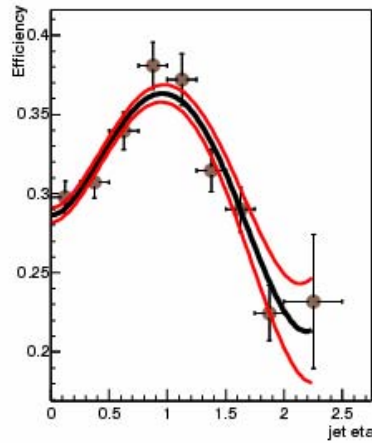
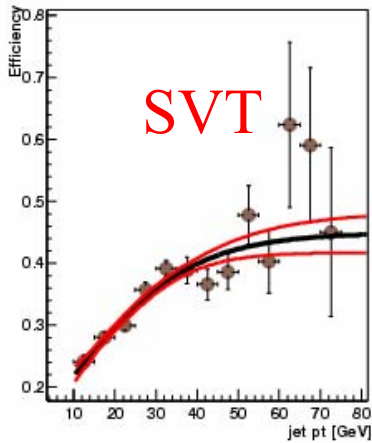
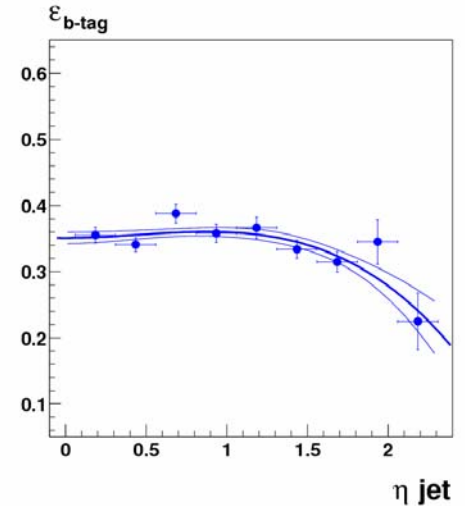
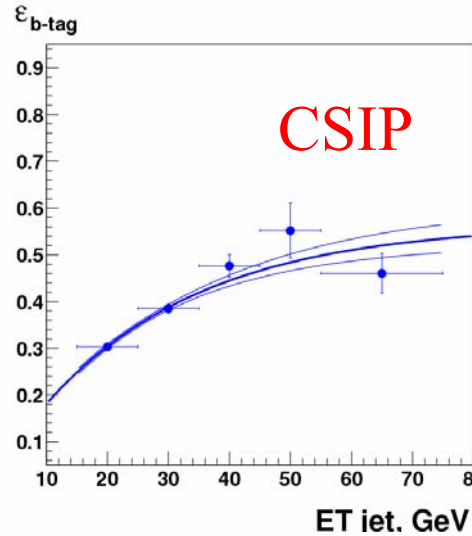
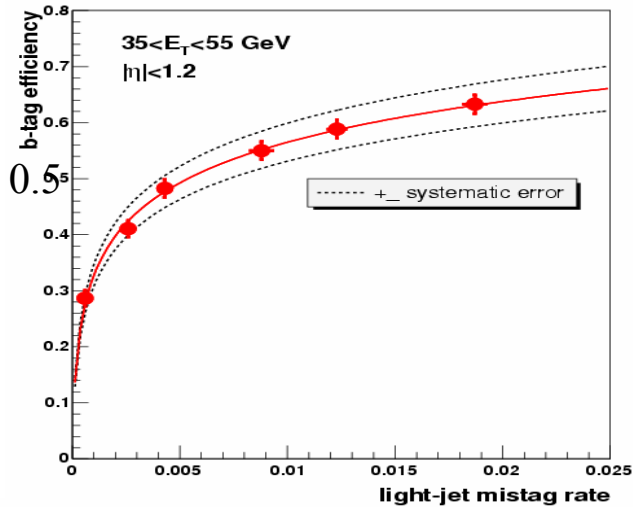
# *b*-tagging performance on data (CDF)





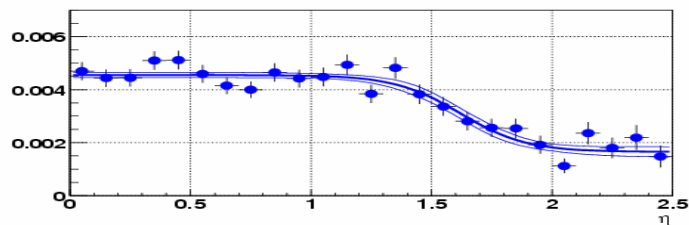
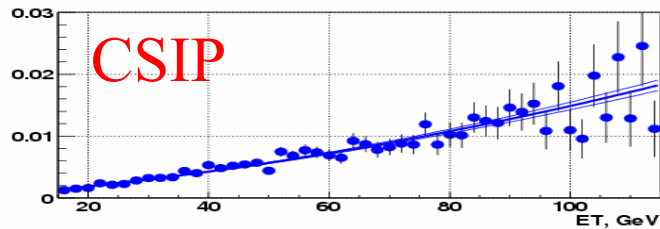
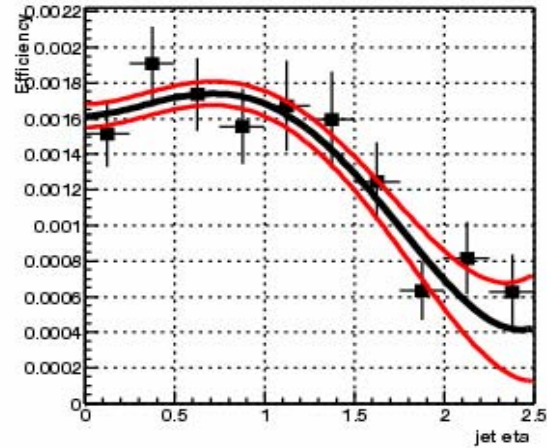
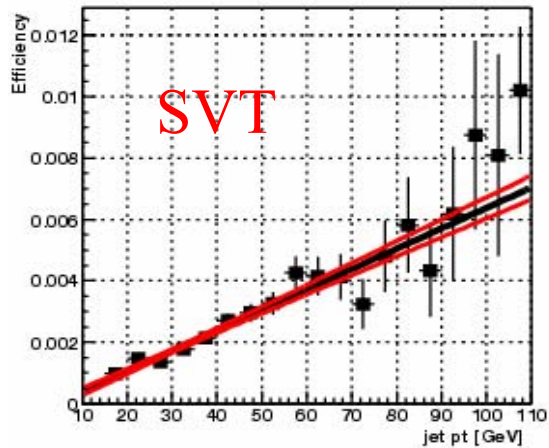
# Results: $b$ -tagging efficiency in data (DØ)

JLIP performance in p14 real Data



Probability to tag a  $tt$  event  $P(n_{\text{tag}} \geq 1)$ :  
 CSIP:  $\sim 61\%$   
 SVT:  $\sim 58\%$

# Mistagging rate in data ( $D\emptyset$ )



W+4 light jets events

$P(n_{\text{tag}} \geq 1)$ :

SVT:  $\sim 1.1\%$

CSIP:  $\sim 2.6\%$

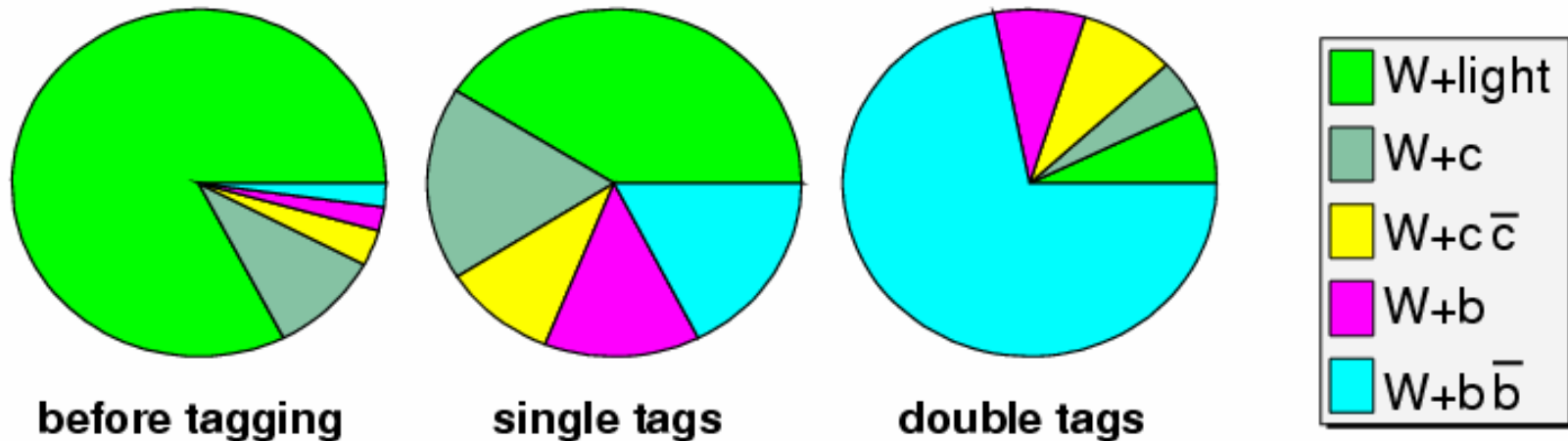
# Role of $b$ -tagging in $t\bar{t}$ studies

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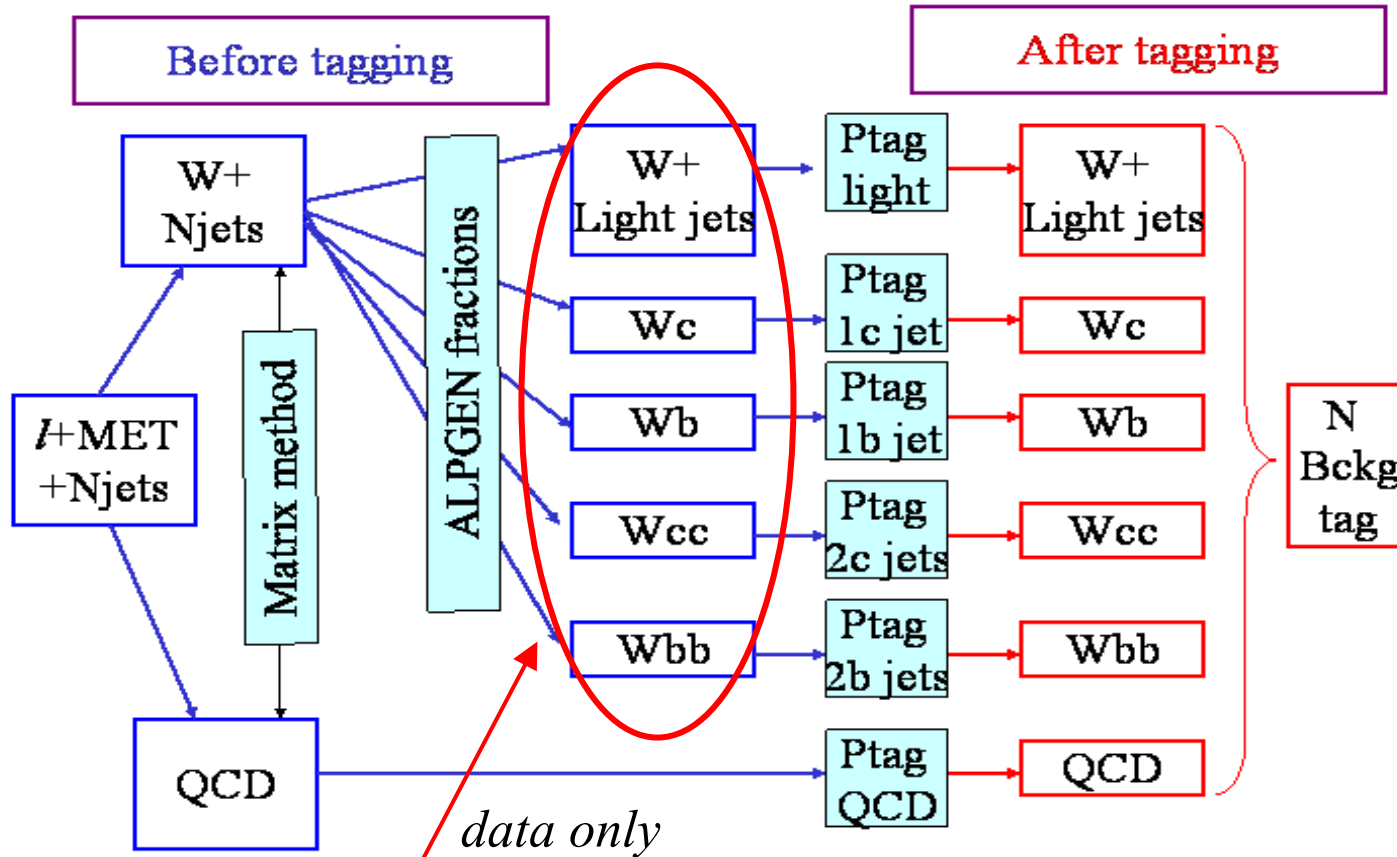
Why do we want to use  $b$ -tagging in top analyses?

After suppressing QCD background by requirement of high MET and “real” isolated lepton,  $W$ +jets production is the main BG.

$W$ +jets composition in the 4<sup>th</sup> jet multiplicity bin:



# *b*-tagging in top cross section measurement



Estimate  $t\bar{t}$  production cross-section from the excess observed in the number of tagged events w.r.t. BG expectation in 3 and 4jet multiplicity bins.

*One of the most important inputs from theory*

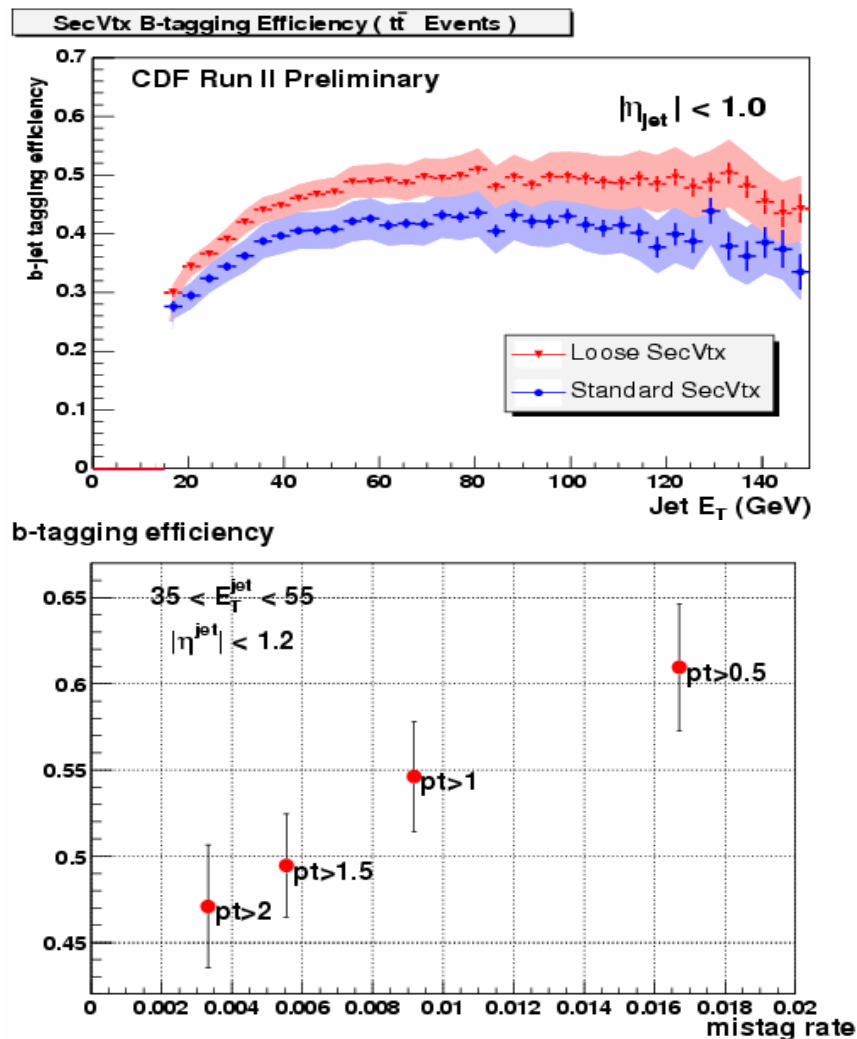
# Estimation of $W$ +jets background

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- Use  $W$ +jets sample generated with ALPGEN (LO ME) interfaced to PYTHIA;
- Apply matching procedure ( $D\emptyset$  - ad hoc) to eliminate double counting and reduce sensitivity to parton generation cuts;
  - Want to have well defined procedure which works for all types of quarks
  - Need predictions for fractions from NLO calculations, for instance, we can correct LO predictions by NLO scale factor using  $W$ +2 jets calculations
- Rely on ratios of the cross sections – apply 50% uncertainty;
  - Is it too conservative?
- Use MC  $b,c$ -tagging efficiencies corrected for the difference between data and MC using scale factors;
- Rely on MC kinematics of  $W$ + $n$  jets (and  $t\bar{t}$ ) events when calculate average event tagging probability
  - cross checks (after tagging) of kinematical distributions made by CDF and  $D\emptyset$  show that kinematics is described reasonably (at the level of available statistics)

# *b*-tagging R&D at the Tevatron

- Increase *b*-tagging efficiency by the price of increasing mis-tagging rate (CDF&DØ)
  - reasonable for cases where the dominant background is expected to be heavy flavor production
- Increase acceptance of *b*-tagging algorithms (CDF)
- Suppress *c*-tagging efficiency (done by CDF, work is going on in DØ)
  - Important for further background rejection in top quark studies, Higgs boson and some signatures of new physics searches.



# *b*-tagging at the LHC

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- Different vertex detector – pixel tracker, much better single hit position resolution
  - But larger inner radius  $R_{inner}$  compared to CDF, DØ detectors – *b*-tagging efficiency is not expected to be essentially higher than at the Tevatron;
- Best sample to measure *b*-tagging efficiency – *tt* $\bar{b}$  events! (in addition to the standard lepton-in-jet sample)
  - For example, dilepton channel requiring one *b*-tag – huge statistics, high purity of *b*-jet sample
- Will have a possibility to measure *c*-tagging efficiency directly on data:
  - *tt* $\bar{b}$  events, lepton+jets sample, look at the hadronic decays of *W* boson (no *b*-jets)
  - good jet energy resolution to reconstruct hadronic *W* in top events.

# Conclusions

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- CDF and DØ have very similar b-tagging performance on data;
- Both experiments have well developed methods to measure b-tagging efficiency and mistagging rates on data;
- Further studies on *b*-tagging are going in the same direction;
- Hope our experience will be useful for LHC.