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# HIGGS BOSON PLUS 2 JET PRODUCTION: WBF SIGNAL AND QCD BACKGROUND AT NLO

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1. Introduction & Motivation
2. Production Dynamics and WBF Cuts at the LHC
3. Signal Purity and Coupling Uncertainties at the LHC
4. Summary

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E Berger and John Campbell, hep-ph/0403194, Phys Rev D, in press

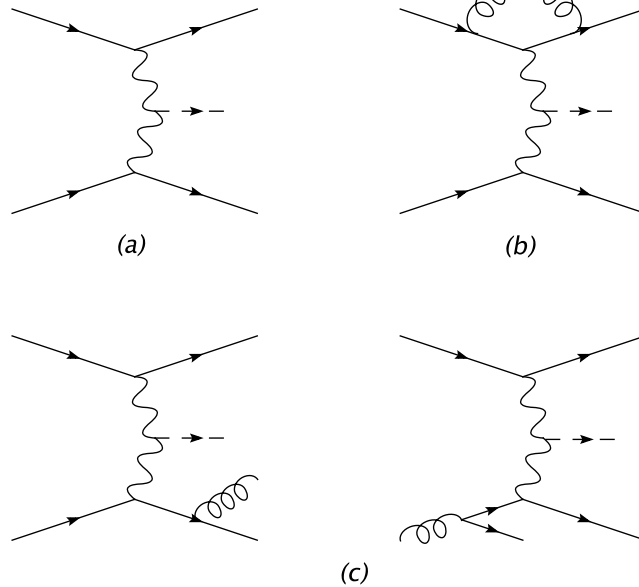
## Introduction and Motivation

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- Assume a SM-like Higgs boson has been discovered,  $115 < m_H < 200$  GeV at the Tevatron or the LHC, and that a sample exists of  $H + 2$  jet events at the LHC
- Want to use these data to determine the Higgs boson couplings  $g$  to weak vector bosons,  $W$  and  $Z$
- Focus on two production subprocesses that contribute to  $H + 2$  jet events:
  - $W + W \rightarrow H$  and  $Z + Z \rightarrow H$  “WBF”
  - $g + g \rightarrow H$  “irreducible QCD background”
- Issues for the determination of couplings:
  - How well can we model the WBF signal and the QCD background?
  - How well can we resolve WBF production of  $H$  from QCD production of  $H$ ?
- Independent calculation of  $H + 2$  jet processes
  - to gauge the effectiveness of cuts used to select the WBF signal, and
  - to evaluate the accuracy with which coupling  $g$  can be determined in experiments at the CERN LHC

## $H + 2$ Jet Production – Signal

- Higgs boson  $H$  production via  $WW$  scattering in NLO QCD. Ex:

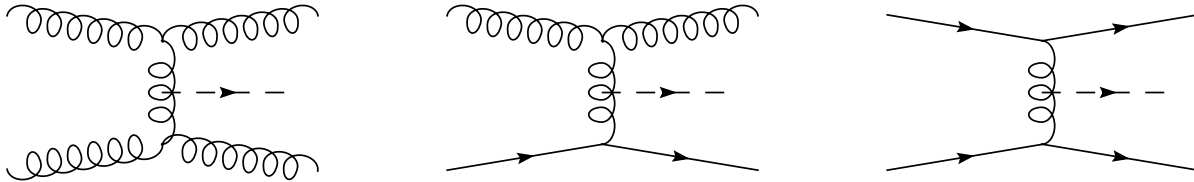


- QCD NLO calculation of  $H + 2$  jets with CTEQ6M parton densities; renormalization/factorization scale  $\mu = m_H$
- Hard perturbative scale  $\mu$  dependence  $\sim 2\%$  for  $\frac{1}{2}m_H < \mu < 2m_H$ , and CTEQ PDF uncertainty  $\sim 3\%$ , both in the WBF region of phase space  
→ signal is calculated fairly reliably
- Events generated with the MCFM code  
J. Campbell & R. K. Ellis PRD65,113007 (2002)
- Independent results (dipole subtraction method) verify the NLO calculation of Figy, Oleari, Zeppenfeld, PRD68, 073005 (2003).  
 $K$ -factor  $\sim 10\%$ , with small variation over the phase space appropriate for the WBF signal

## $H + 2$ Jet Production – Irreducible Background

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- Higgs boson  $H$  production via  $gg$  scattering. Ex:



- Fully differential NLO calculation of  $H + 2$  jet production does not exist; contribution computed at LO Kauffman Desai and Risal, PRD55, 4005 (1997); PRD58, 119901 (1998)
- Effective  $ggH$  coupling included in the limit of  $m_H \ll 2m_t$  and  $p_T^H < m_t$   
(c.f. Del Duca et al NP B616, 367 (2001))
- NLO enhancement ( $K$ ) factor is needed in the region of the WBF cuts. It can be estimated from
  - inclusive NLO  $gg \rightarrow H$   $K \sim 1.7 - 1.8$   
Harlander & Kilgore PRD64, 013015 (2001); Anastasiou & Melnikov, NP B646, 220 (2002)
  - NLO  $gg \rightarrow H + 1$  jet  $K \sim 1.3 - 1.5$   
Ravindran, Smith, van Neerven NP B665, 325 (2003)
- Uncertainty: hard scale  $\mu$  dependence .....

## Event Characteristics

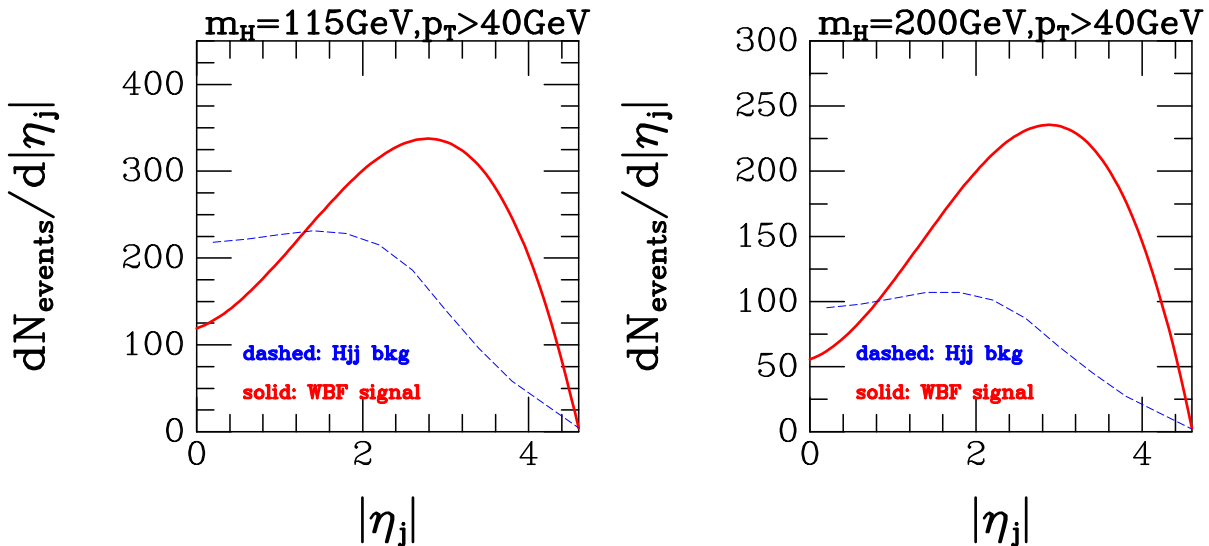
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- Hallmark of WBF events in hadron reactions is a Higgs boson accompanied by two “tagging” jets having large  $p_T \sim \mathcal{O}(\frac{1}{2}M_W)$
- QCD  $gg \rightarrow H + 2 \text{ jets}$  generate a softer  $p_T$  spectrum
- The rapidity spectra for the WBF and QCD production mechanisms also differ, related to the fact that the gluon parton density (that plays a dominant role in the background) is softer than the quark density; figures shown on next slide
- The  $p_T$  spectrum of the Higgs boson is also relatively hard. All-orders resummed calculation Berger and Qiu PRD 67, 034026 (2003) provides  $\langle p_T^H \rangle \sim 35 \text{ GeV}$  at  $m_H = M_Z$ , growing to  $\langle p_T^H \rangle \sim 54 \text{ GeV}$  at  $m_H = 200 \text{ GeV}$
- Require reliable QCD representation of  $Hjj$  for jets at large  $p_T$ . Hard matrix elements are needed. A showering approach for generating the momentum distributions of the jets would not suffice; showering yields softer jets and overestimates signal purity

## $H + 2$ Jet Production – Jet Rapidity Distribution

- Higgs boson  $H$  production via  $WW$  and  $ZZ$  scattering in NLO and via  $gg$  QCD processes (LO)

(for  $1 \text{ fb}^{-1}$ , no BR included):



- Shape of the **signal** distribution depends very little on the Higgs boson mass or on the  $p_T$  cut for the tagging jets.

**Peak at  $|\eta| \sim 3$ . Full width at half-max  $\sim 2.8$**

- Background falls off sharply beyond  $|\eta| \sim 2$
- Motivates a **simple WBF prescription**:

$$\eta_{\text{peak}} - \eta_{\text{width}}/2 < |\eta_j| < \eta_{\text{peak}} + \eta_{\text{width}}/2$$

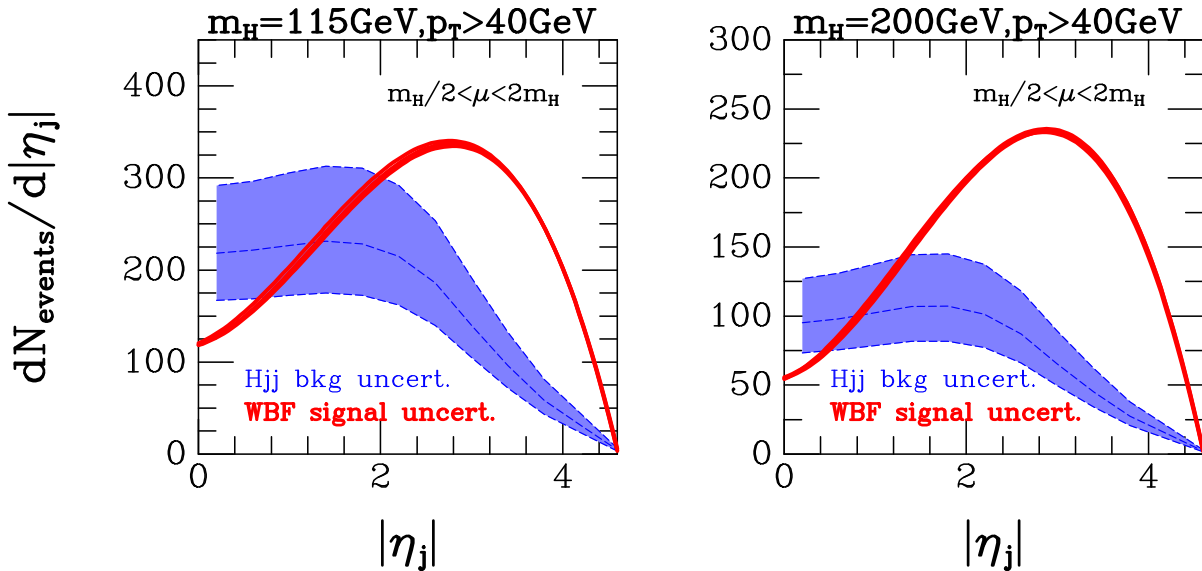
$$j = j_1 \text{ or } j = j_2, \quad \eta_{\text{peak}}=3, \quad \text{and } \eta_{\text{width}}=2.8$$

- This is our working definition of the WBF region

## $H + 2 \text{ Jet Production} - \mu \text{ dependence}$

- Higgs boson  $H$  production via  $WW$  scattering in NLO and via  $gg$  QCD processes (LO)

hard-scale  $\mu$  variation from  $\mu = m_H/2$  to  $\mu = 2m_H$ :



- Magnitude and shape of the **signal** distribution depend very little on  $\mu$ :  $\pm 2\%$
- Magnitude of the background shows significant uncertainty at LO; it is 70% greater at  $\mu = m_H/2$ , and 40% less at  $\mu = 2m_H$
- This uncertainty in the irreducible background translates into uncertainty in the extraction of the coupling strengths. To reduce the uncertainty, a differential NLO calculation is needed for the QCD background process  $H + 2 \text{ jets}$

## Steps toward $H + 2$ jets NLO QCD Background

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- The tree-level matrix elements for  $H + 3$  jets are computed

Del Duca, Frizzo, Maltoni hep-ph/0404013; JHEP 0405, 064 (2004)

- Loop processes remain; appropriate NLO subtractions; soft and collinear singularities

- Extend the NLO study of  $gg \rightarrow H + 1$  jet

Ravindran, Smith, van Neerven NP B665, 325 (2003)

to one additional jet in fully differential fashion

- Equivalent calculation for  $W + 2$  jets and  $Z + 2$  jets done and implemented in MCFM J. Campbell and R. K. Ellis

- Full NLO calculation of  $H + 2$  jets would be similar; the LO process involves 3 independent matrix elements:

$$g + g \rightarrow H + g + g; g + g \rightarrow H + q + \bar{q}; \text{ and } q + \bar{q} \rightarrow H + q + \bar{q}$$

- Anyone already doing this?



## Signal Purity

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- Define Purity  $P = \frac{S}{S+B}$   
 $S$  is the number of signal  $H + 2$  jet events and  
 $B$  is the number of  $H + 2$  jet QCD background events  
both in the WBF region of phase space
- Study Purity  $P$  of the signal vs  $p_T$  of the jets
- Evaluate uncertainty  $\frac{\delta g}{g}$  of the coupling in terms of  
 $P \quad \frac{\delta N}{N} \quad \frac{\delta S}{S} \quad \text{and} \quad \frac{\delta B}{B}$

## $H + 2 \text{ Jet Production} - \text{Event Rates for } 1 \text{ fb}^{-1}$

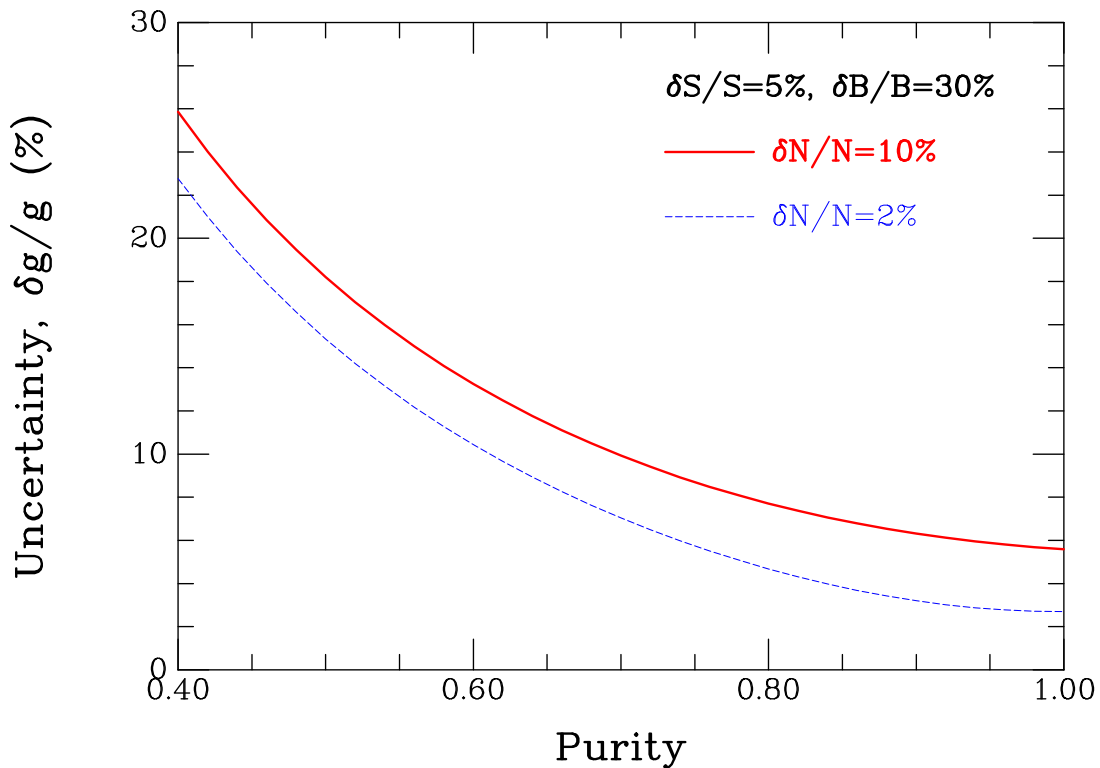
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- Event rates for the  $Hjj$  WBF signal(NLO) and  $Hjj$  background(LO), including our WBF requirement that at least one jet have  $1.6 < |\eta| < 4.4$  (no BR included)

$p_T$ cut [GeV]	20	40	80
Signal ( $m_H = 115$ )	1374	789	166
Bkg	1196	382	92
Purity	0.53	0.67	0.64
Signal ( $m_H = 200$ )	928	545	121
Bkg	534	179	46
Purity	0.63	0.75	0.72

- Recall  $P = S/(S + B)$ 
  - Purity is independent of total integrated luminosity
- $p_T$  cut of 40 GeV yields a good S/B across the range  $m_H = 115\text{--}200$  GeV.  $p_T$  cut of 20 GeV is marginal
- Signal purities of  $\sim 65\%$  for  $p_T$  cut  $\gtrsim 40$  GeV; purity is greater at the larger values of  $m_H$

## Coupling Uncertainty vs Signal Purity



- If  $\delta N/N \sim 10\%$      $\delta g/g \sim 10\%$     for  $P = 0.7$
- If  $\delta N/N \sim 2\%$      $\delta g/g \sim 7\%$     for  $P = 0.7$
- Uncertainties in  $S$  and in  $B$  dominate uncertainty in  $g$ .  
 With  $P = 0.7$  and  $\delta N/N = 2\%$ , then  $\delta S/S$  and  $\delta B/B$  have to be reduced to 3% and 6% before statistics control the answer
- $P > 0.65$  permits  $\delta g/g \sim 10\%$  after  $200 \text{ fb}^{-1}$   
 Obtained for  $p_T^{\text{cut}} > 40 \text{ GeV}$  at  $m_H = 115 \text{ GeV}$  and  
 for  $p_T^{\text{cut}} > 20 \text{ GeV}$  at  $m_H = 200 \text{ GeV}$
- Suppose  $K_{\text{background}}^{\text{NLO}} \sim 1.6$   
 $P = 0.56$  for  $p_T^{\text{cut}} > 40 \text{ GeV}$  at  $m_H = 115 \text{ GeV} \rightarrow$   
 $\delta g/g = 13\%$   
 $P = 0.52$  for  $p_T^{\text{cut}} > 20 \text{ GeV}$  at  $m_H = 200 \text{ GeV} \rightarrow$   
 $\delta g/g = 15\%$

## Summary

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- Studied  $H + 2$  jet production at the energy of the LHC. Fully differential hard matrix elements used to generate  $p_T$  spectra
- Evaluated the signal purity  $P$  (fraction of real  $H$  events produced by WBF) in each case as a function of the transverse momentum cut used to define the tagging jets
- A fully differential NLO calculation of the  $H + 2$  jet QCD background distributions is needed, applicable in the WBF region of phase space, so that  $P$  and  $\delta g/g$  can be determined more accurately
- After  $200 \text{ fb}^{-1}$  are accumulated at the LHC, it may be possible to achieve an accuracy  $\delta g/g \sim 10\%$  in the effective coupling (combination of  $HWW$  and  $HZZ$ ) of the Higgs boson to weak bosons. (These estimates are less optimistic than those in the Les Houches 2003 study)
- With a 500 GeV LC and  $500 \text{ fb}^{-1}$ , the expected accuracies are  $\delta g_{ZZH}/g_{ZZH} \simeq 3\%$  for  $120 < m_H < 200 \text{ GeV}$  and  $\delta g_{WWH}/g_{WWH} \simeq 3\%$  to  $\simeq 7\%$  for  $120 < m_H < 160 \text{ GeV}$