

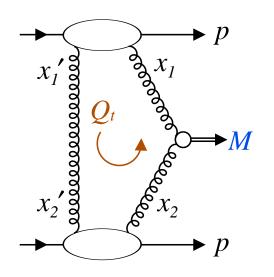
# Central Exclusive Higgs with LDC uPDFs



Fermilab 2003.09.20 Leif Lönnblad

- Higgs à la Khoze, Martin, Ryskin
- Unintegrated gluons from LDC
- Preliminary results

## Exclusive Diffractive Higgs



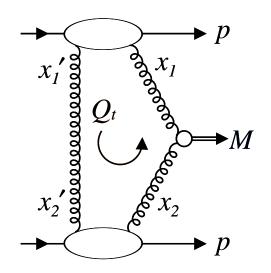
$$\frac{d\sigma_{M}^{\text{excl}}}{dM^{2}dy} = \frac{d\mathcal{L}}{dM^{2}dy}\hat{\sigma}_{gg\to M}(M^{2})$$

$$M^{2}\frac{d\mathcal{L}}{dM^{2}dy} = S^{2}L$$

$$L = S^{2} \left( \frac{\pi}{(N_{c}^{2} - 1)b} \int \frac{dQ_{t}^{2}}{Q_{t}^{4}} f_{g}(x_{1}, x_{1}', Q_{t}^{2}, M^{2}/4) f_{g}(x_{2}, x_{2}', Q_{t}^{2}, M^{2}/4) \right)^{2}$$



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 $f_q$  is the un-integrated, off-diagonal gluon density.

 $S^2$  is a soft survival probability.

b is the t-slope of the proton.

For 
$$x' \approx \frac{Q_t}{\sqrt{s}} \ll x \approx \frac{M}{\sqrt{s}} \ll 1$$
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$$f_g(x, x', Q_t^2, M^2/4) = R_g \frac{\delta}{\delta Q_t^2} \left[ \sqrt{T(Q_t, M/2)xg(x, Q_t^2)} \right]$$



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$$R_g(x,\mu^2) \approx 1 + (0.82 + 0.56\lambda)\lambda$$
 with  $\lambda = d\ln(xg(x,\mu^2))/d\ln(1/x)$ 

$$\langle R_g \rangle \approx 1.2(1.4)$$
 at LHC (Tevatron)

T is the Sudakov form factor (hard survival probability).





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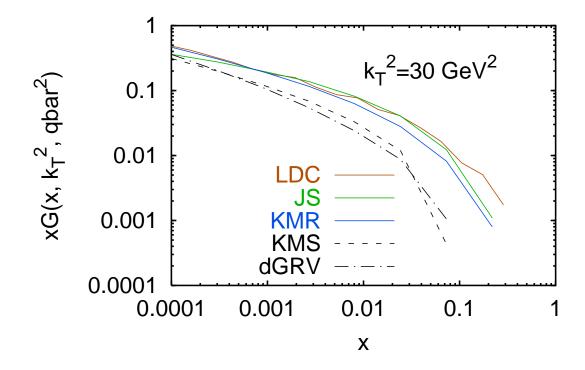
Gap survival probability due to soft/semi-hard rescatterings  $S^2 \approx 0.02 (0.045)$  for the LHC (Tevatron)



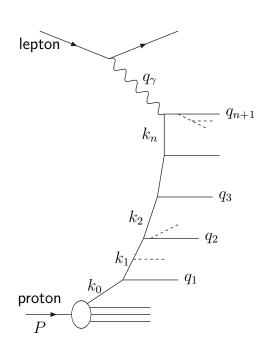
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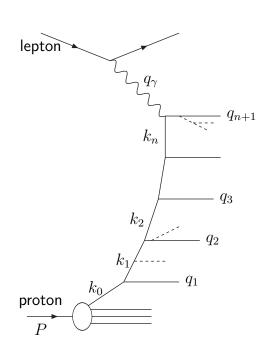




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$$\mathcal{G}(x, k_{\perp}^2, \bar{q}^2) \approx \mathcal{G}(x, k_{\perp}^2, k_{\perp}^2) \Delta_S(k_{\perp}^2, \bar{q}^2)$$

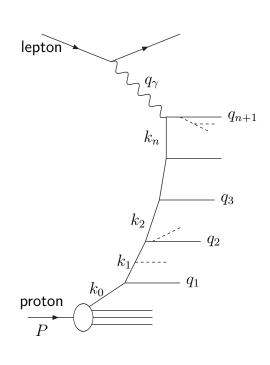




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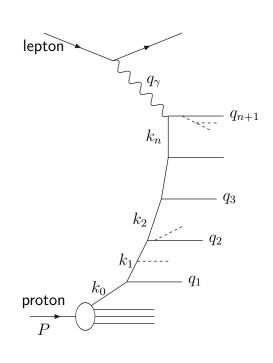




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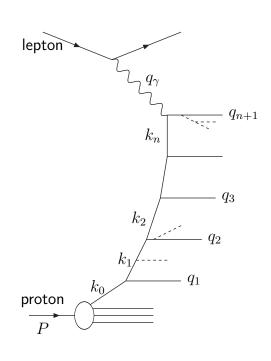




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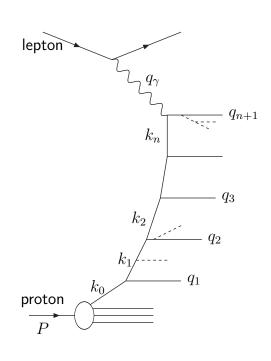




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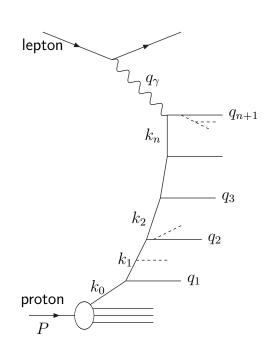




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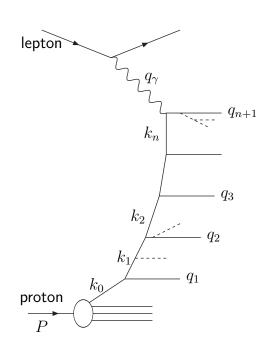




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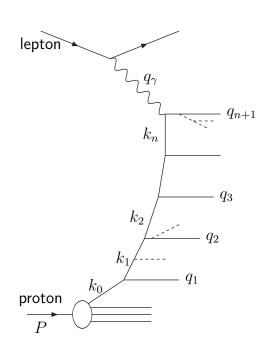




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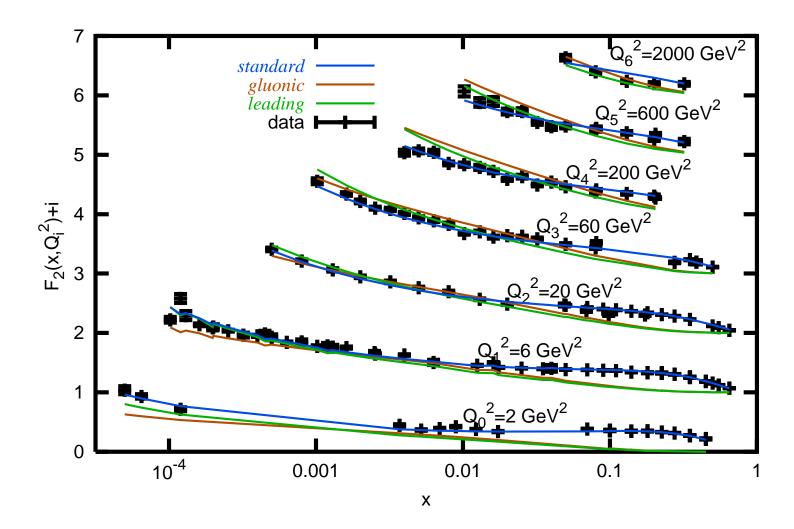




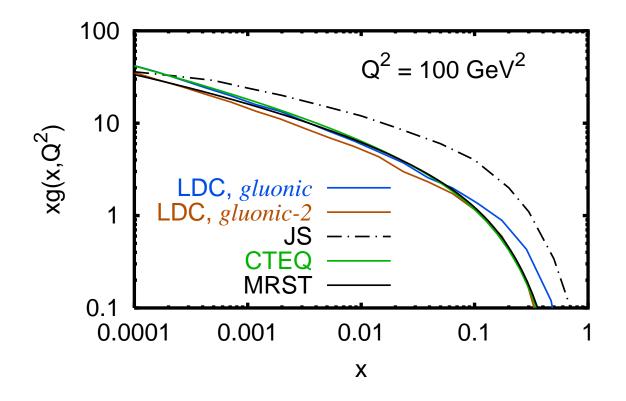
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- and non-singular terms
- Forward–backward symmetric

$$\mathcal{G}(x, k_\perp^2, \bar{q}^2) \approx \mathcal{G}(x, k_\perp^2, k_\perp^2) \Delta_S(k_\perp^2, \bar{q}^2)$$









$$xg(x,Q^{2}) = \int_{k_{\perp 0}^{2}}^{Q^{2}} \frac{dk_{\perp}^{2}}{k_{\perp}^{2}} \mathcal{G}(x,k_{\perp}^{2},Q) + \int_{Q^{2}}^{Q^{2}/x} \frac{dk_{\perp}^{2}}{k_{\perp}^{2}} \mathcal{G}(x\frac{k_{\perp}^{2}}{Q^{2}},k_{\perp}^{2},Q) \frac{Q^{2}}{k_{\perp}^{2}} + xg_{0}(x,k_{\perp 0}^{2}) \times \Delta_{S}$$

$$f_g(x, x', Q_t^2, M^2/4) = R_g \frac{\delta}{\delta Q_t^2} \left[ \sqrt{T(Q_t, M/2)} x g(x, Q_t^2) \right]$$

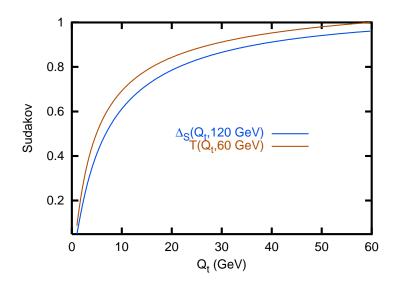
"Strictly speaking the relationship was only proven for integrated gluons. However, it is expected to hold equally well for the unintegrated distribution."

$$f_g(x, x', Q_t^2, M^2) = R_g \sqrt{\Delta_S(Q_t^2, M^2)} \mathcal{G}(x, Q_t^2, Q_t^2)$$

In LDC  $\mathcal{G}(x,Q_t^2,Q_t^2)$  also contains effects of emissions with  $p_{\perp g}>Q_t$ . Should these be included? Also the screening gluon may contain effects of  $p_{\perp g}>Q_t$  which are larger since  $x'\approx \frac{Q_t}{\sqrt{s}}\ll x\approx \frac{M}{\sqrt{s}}$ .

$$\ln T(Q_t, M/2) = -\int_{Q_t^2}^{M^2/4} \frac{\alpha_s(k_\perp^2)}{2\pi} \frac{dk_\perp^2}{k_\perp^2} \int_0^{\frac{M}{M+2k_\perp}} \left[ z P_{gg}(z) + n_f P_{qg}(z) \right] dz$$

$$\ln \Delta_S(Q_t^2, M^2) = -\int_{Q_t^2}^{M^2} \frac{\alpha_s(k_\perp^2)}{2\pi} \frac{dk_\perp^2}{k_\perp^2} \int_0^{1-k_\perp/M} \left[ z P_{gg}(z) + n_f P_{qg}(z) \right] dz$$





LDC needs a cutoff,  $k_{\perp 0}$ , below that we use non-perturbative input densities.

$$L = \left[ \frac{\pi}{(N_c^2 - 1)b} \left( \int_{k_{\perp 0}^2}^{M^2} \frac{dQ_t^2}{Q_t^4} \mathcal{G}(x, Q_t^2, Q_t^2) \mathcal{G}(x, Q_t^2, Q_t^2) \Delta_S(Q_t^2, M^2) \right. \\ + \left. g_0(x, k_{\perp 0}^2) g_0(x, k_{\perp 0}^2) \Delta_S(k_{\perp 0}^2, M^2) / k_{\perp 0}^2 \right) \right]^2$$



We will use three different LDC unintegrated gluons which differs in the treatment of non-leading terms.

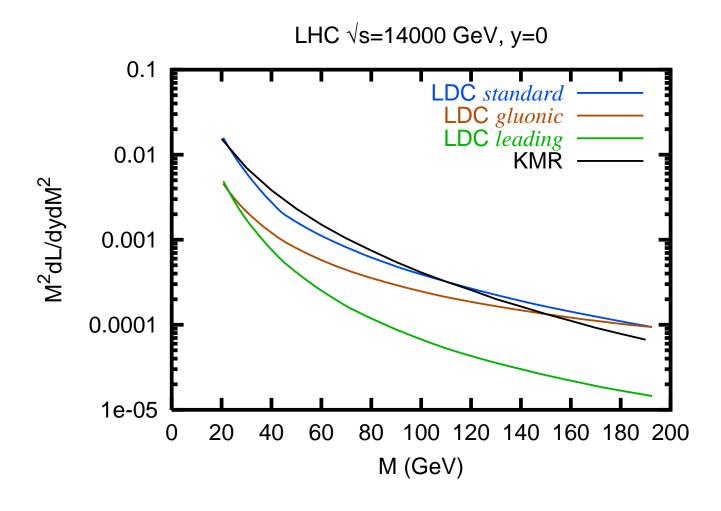
standard uses quark and gluon evolution with full splitting functions. Gives a good description of  $F_2$ .

gluonic uses only gluons with full splitting function. Gives a good description of the integrated gluon.

*leading* uses only gluons with only singular terms in the splitting function. Gives a good description of forward jets and b-production at the Tevatron.

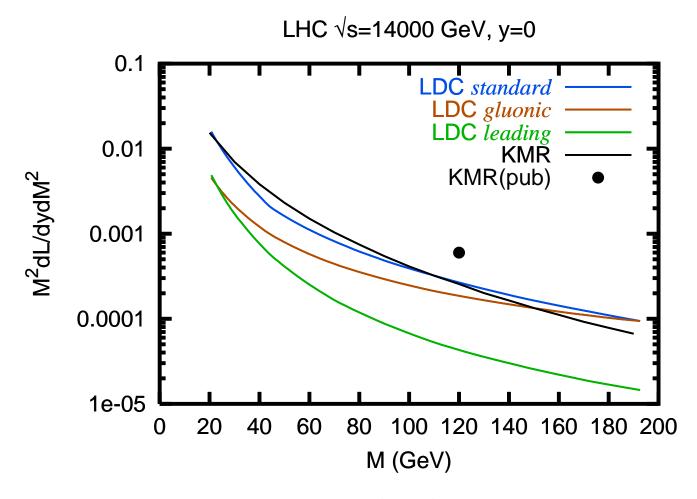
They are all extracted from generating a large number of DIS events with LDCMC and sampling the gluon density in bins of x and  $k_{\perp}$ .

# Preliminary results



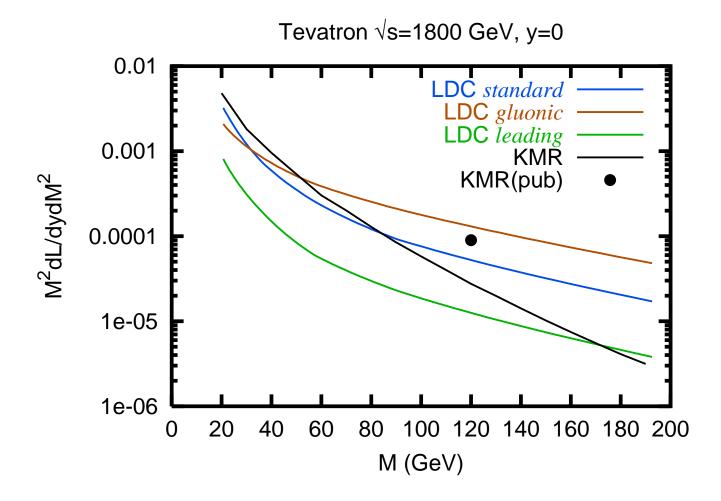


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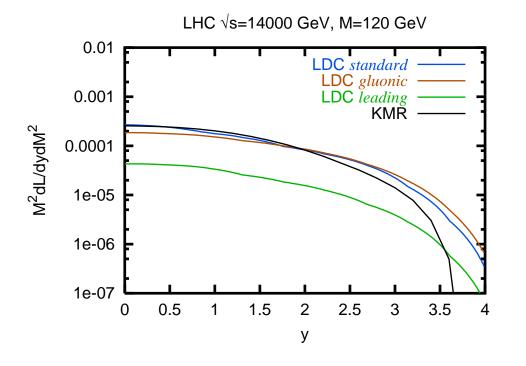


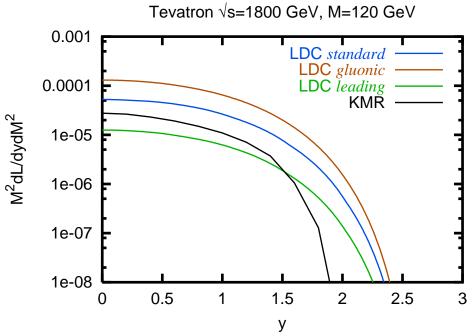
Khoze, Martin, Ryskin, Eur. Phys. J. C23 (2002) 311.



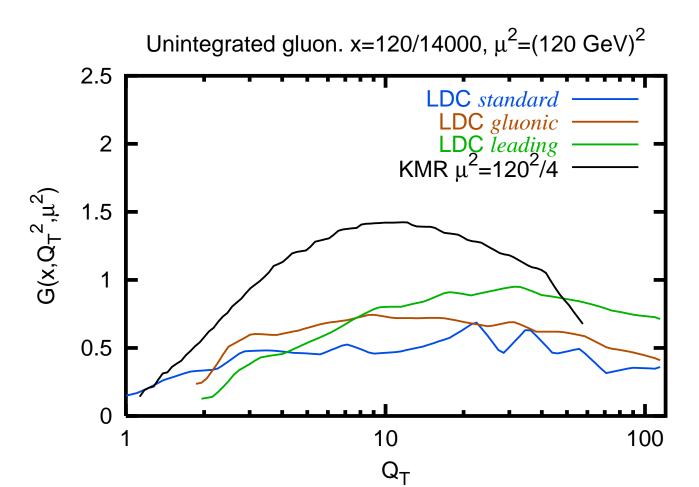




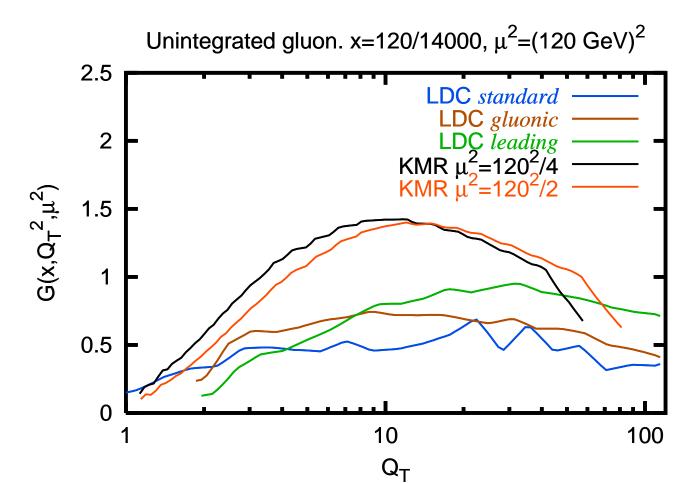




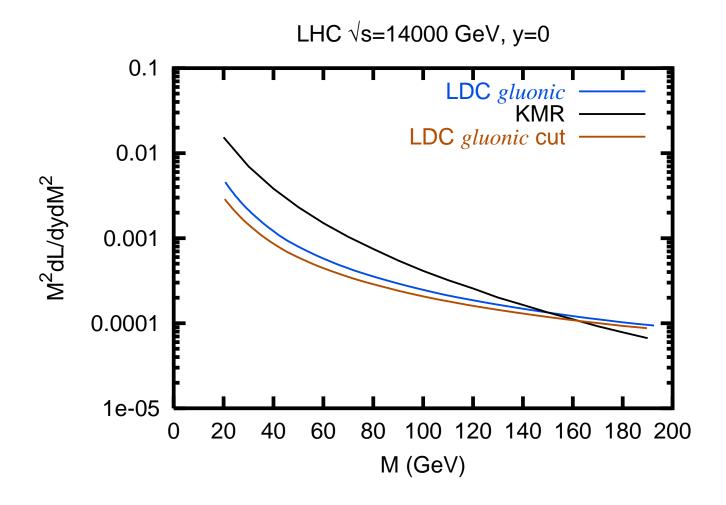




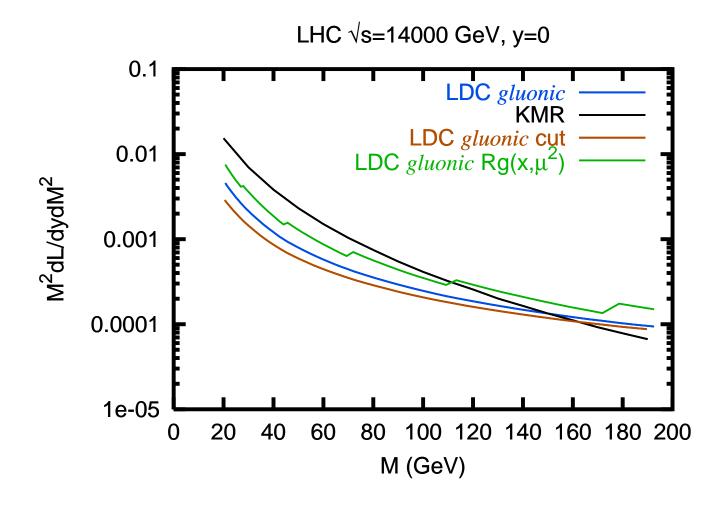
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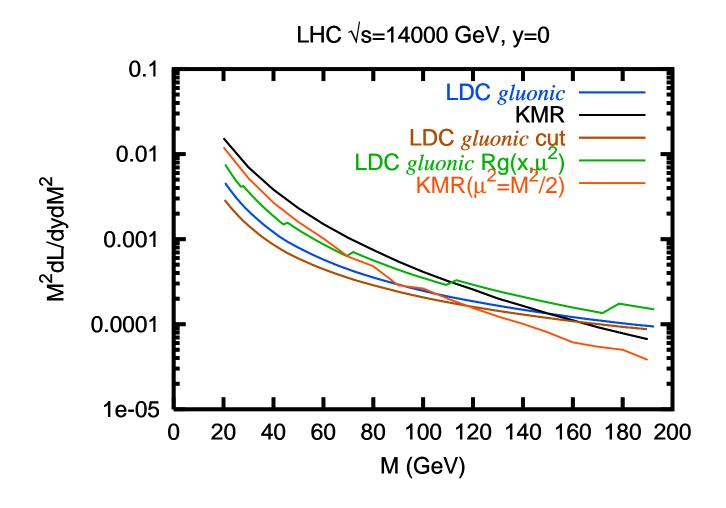
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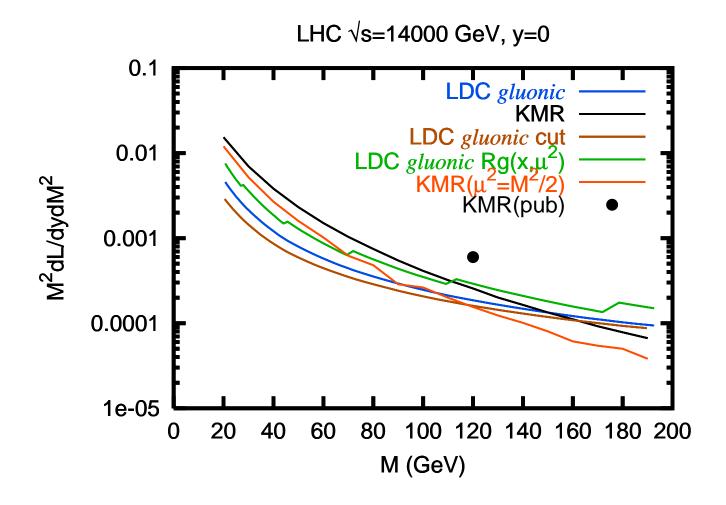














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