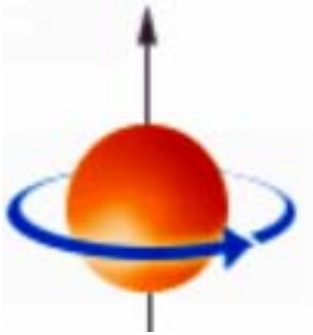


Aug 15, 2003  
Lepton-Photon 2003



# Measurements with Polarized Hadrons

**T.-A. Shibata**

**Tokyo Institute of Technology**

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# Contents:

## Introduction: Spin of Proton

## Polarized Deep Inelastic Lepton-Nucleon Scattering

1. Flavor Separation of Quark Helicity Distributions
2. Deeply Virtual Compton Scattering
3. Single-Spin Azimuthal Asymmetries  
in Semi-Inclusive Deep Inelastic Scattering

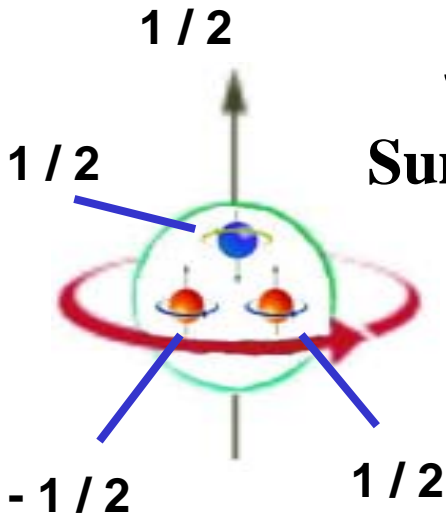
## Polarized Proton-Proton Collisions

### Measurements with **Polarized Hadrons**

**‘Explore spin structure of hadrons and further develop QCD using Spin’**

**QCD was successful, both in perturbative and non-perturbative regions, but spin of the nucleon still needs to be studied in many aspects to be fully explained with QCD.**

# Introduction : Spin of Proton

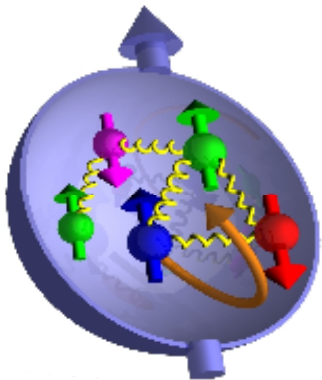


## SU(6) Quark Wave Functions of Baryons

Sum of Spins of u u d Quarks = Spin of Proton

$$\frac{1}{2} + \frac{1}{2} + \left(-\frac{1}{2}\right) = \frac{1}{2}$$

## EMC Experiment (1988)



$$\frac{1}{2}(\Delta u + \Delta d + \Delta s) = 0.06 \pm 0.047 \pm 0.068 \leq \frac{1}{2}$$

(12 ± 9 ± 14)%

20 – 30 % of Nucleon Spin

$$\frac{1}{2} = \frac{1}{2} \sum_q (\Delta u + \Delta d + \Delta s) + L_q + J_G$$

‘Nucleon Spin Problem’ 4

## Experimental Methods: Lepton-Hadron Scattering, Hadron-Hadron Collision

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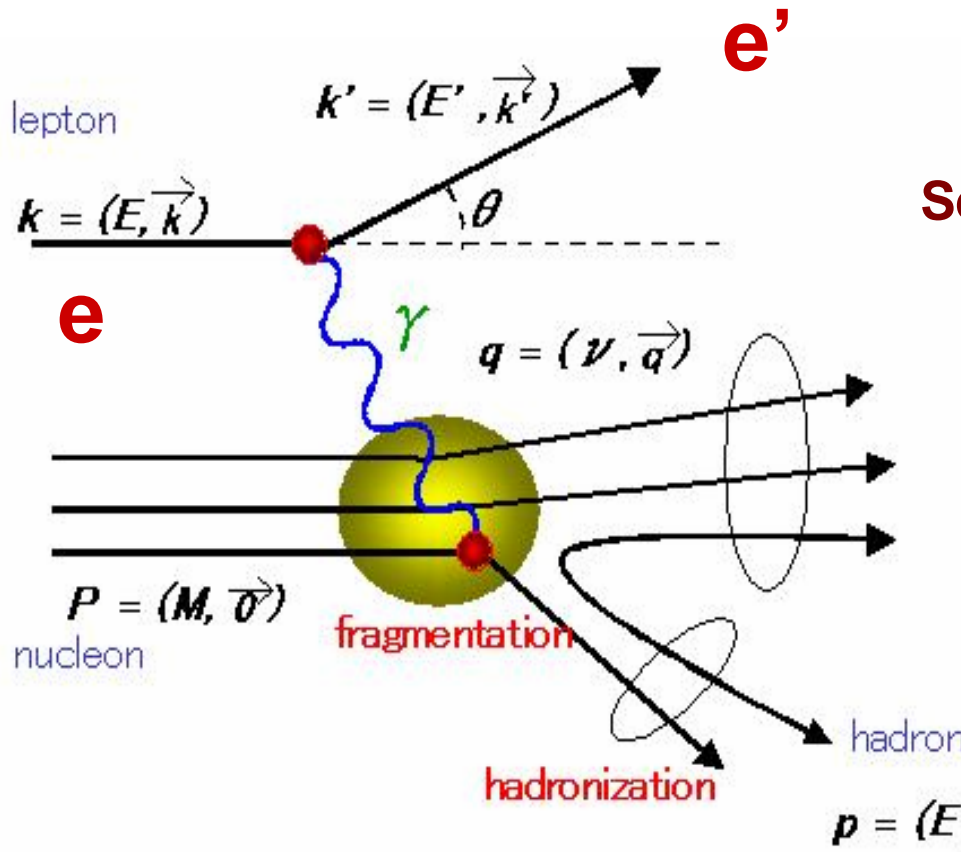
### Fixed Target Experiments :

|                          |          |                                   |                   |
|--------------------------|----------|-----------------------------------|-------------------|
| <b>Polarized Targets</b> | <b>+</b> | <b>(Polarized) Beams</b>          |                   |
| <b>Nucleon (p, n)</b>    | <b>+</b> | <b><math>e^+/e^-</math></b>       | <b>HERMES</b>     |
|                          |          | <b><math>e^-</math></b>           | <b>SLAC, JLab</b> |
|                          |          | <b><math>\mu^+ / \mu^-</math></b> | <b>COMPASS</b>    |

### Collider Experiments :

**Polarized Proton - Proton Collisions**    **RHIC**

# Deep Inelastic Scattering, Semi-inclusive Measurements



**Inclusive measurement,  $e'$**

$$\sigma(x) \propto \sum_q e_q^2 q(x)$$

**Semi-inclusive measurement,  $e'$  and  $\pi, K, p, \bar{p} \dots$**

**Flavor tagging**

$$\sigma_h(x, z) \propto \sum_q e_q^2 q(x) D_q^h(z)$$

( quark distribution ) x  
 ( fragmentation function )

$$z = E_h / \nu$$

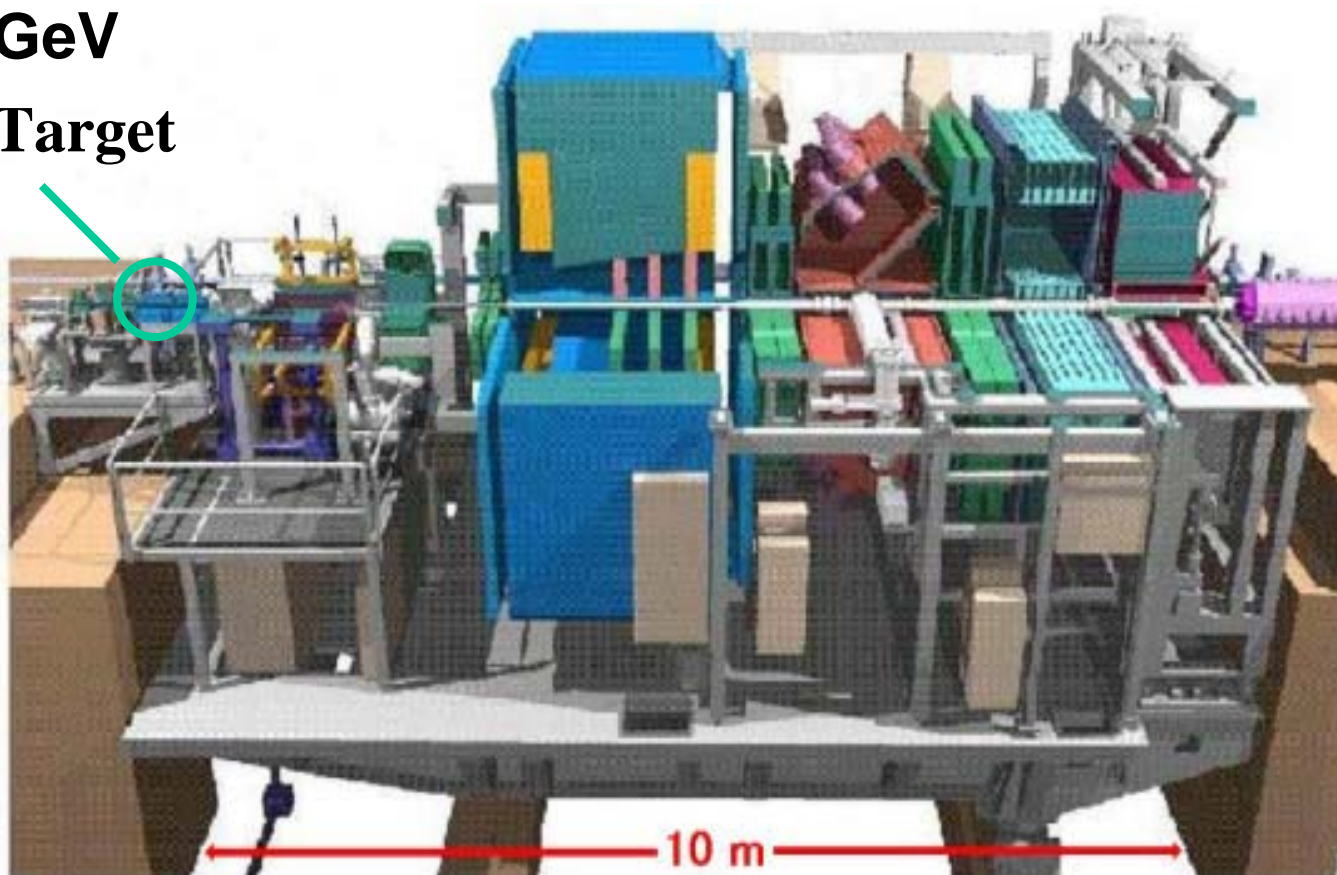
# Detectors

**HERMES @ DESY- HERA**  
**1995 --**

**Polarized Internal gas targets**  
**( $^3\text{He}$ , H, D)**

**27.6 GeV**

**Target**

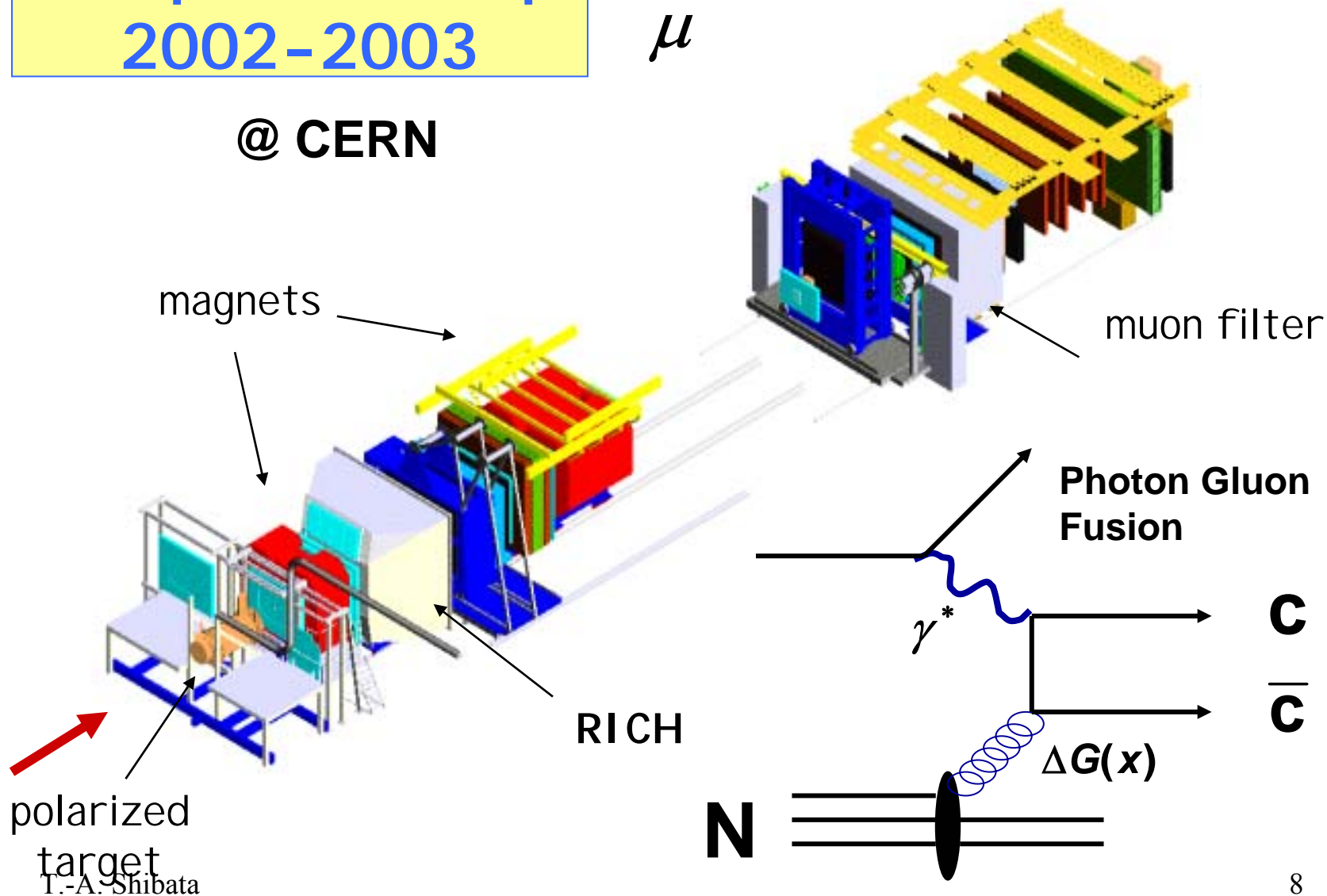


# Compass Set-up 2002-2003

@ CERN

**160 GeV** Gluon Spin Contribution  
D's identified in 2002.

$\mu$





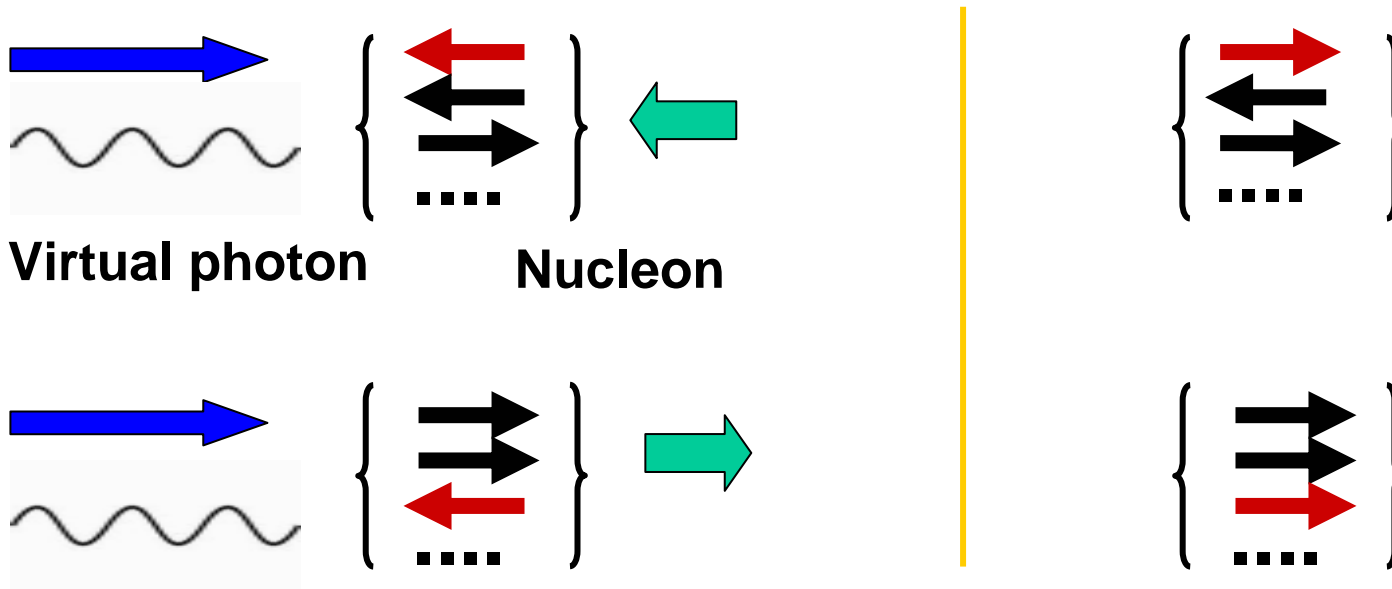
# 1. Flavor Separation of Quark Helicity Distributions

$$\Delta u(x), \Delta d(x), \Delta \bar{u}(x), \Delta \bar{d}(x), \Delta s(x)$$

## Double-spin asymmetry

$$\vec{e} + \vec{N} \rightarrow e' + X$$

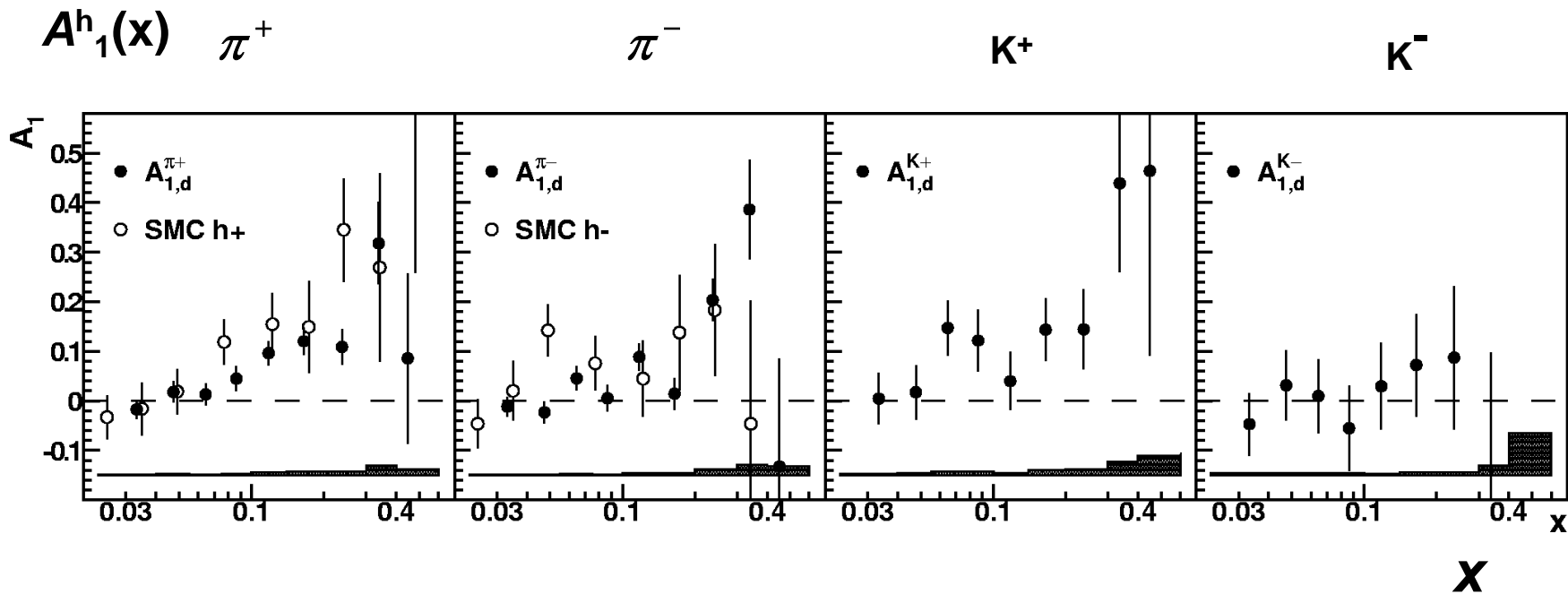
Beam and target, both polarized



$$A_1(\mathbf{x}, \mathbf{z}) = \frac{\sigma_{\leftarrow}^{\rightarrow}(\mathbf{x}) - \sigma_{\rightarrow}^{\rightarrow}(\mathbf{x})}{\sigma_{\leftarrow}^{\leftarrow}(\mathbf{x}) + \sigma_{\rightarrow}^{\leftarrow}(\mathbf{x})}$$

## Double-spin asymmetries $A_1^h(d)$ from semi-inclusive DIS

Hadron identification for the first time



$\pi^\pm, K^+$  asymmetries similar to inclusive asymmetry,  
except  $K^-$  asymmetry.

HERMES

# Quark Helicity Distributions , Flavor Separation

$$\vec{e} + \vec{N} \rightarrow e' + m + X \quad N = p, d \quad m = \pi^\pm, K^\pm$$

Semi-inclusive DIS cross section

$$\sigma_h(\mathbf{x}, \mathbf{z}) \propto \sum_q e_q^2 q(\mathbf{x}) D_q^h(\mathbf{z}) \quad \mathbf{z} = E_h / \nu$$

Double-spin asymmetry

$$A_1^h(\mathbf{x}, \mathbf{z}) = \frac{\sigma_{h \leftarrow}(\mathbf{x}, \mathbf{z}) - \sigma_{h \rightarrow}(\mathbf{x}, \mathbf{z})}{\sigma_{h \leftarrow}(\mathbf{x}, \mathbf{z}) + \sigma_{h \rightarrow}(\mathbf{x}, \mathbf{z})} = \frac{\sum_q e_q^2 \Delta q(\mathbf{x}) D_q^h(\mathbf{z})}{\sum_q e_q^2 q(\mathbf{x}) D_q^h(\mathbf{z})}$$

$$q(\mathbf{x}) = q^{\rightarrow}(\mathbf{x}) + q^{\leftarrow}(\mathbf{x})$$

Quark Density Distributions

$$\Delta q(\mathbf{x}) = q^{\rightarrow}(\mathbf{x}) - q^{\leftarrow}(\mathbf{x})$$

Quark Helicity Distributions

$$\vec{A}_1(\mathbf{x}) = P(\mathbf{x}) \cdot \vec{Q}(\mathbf{x})$$

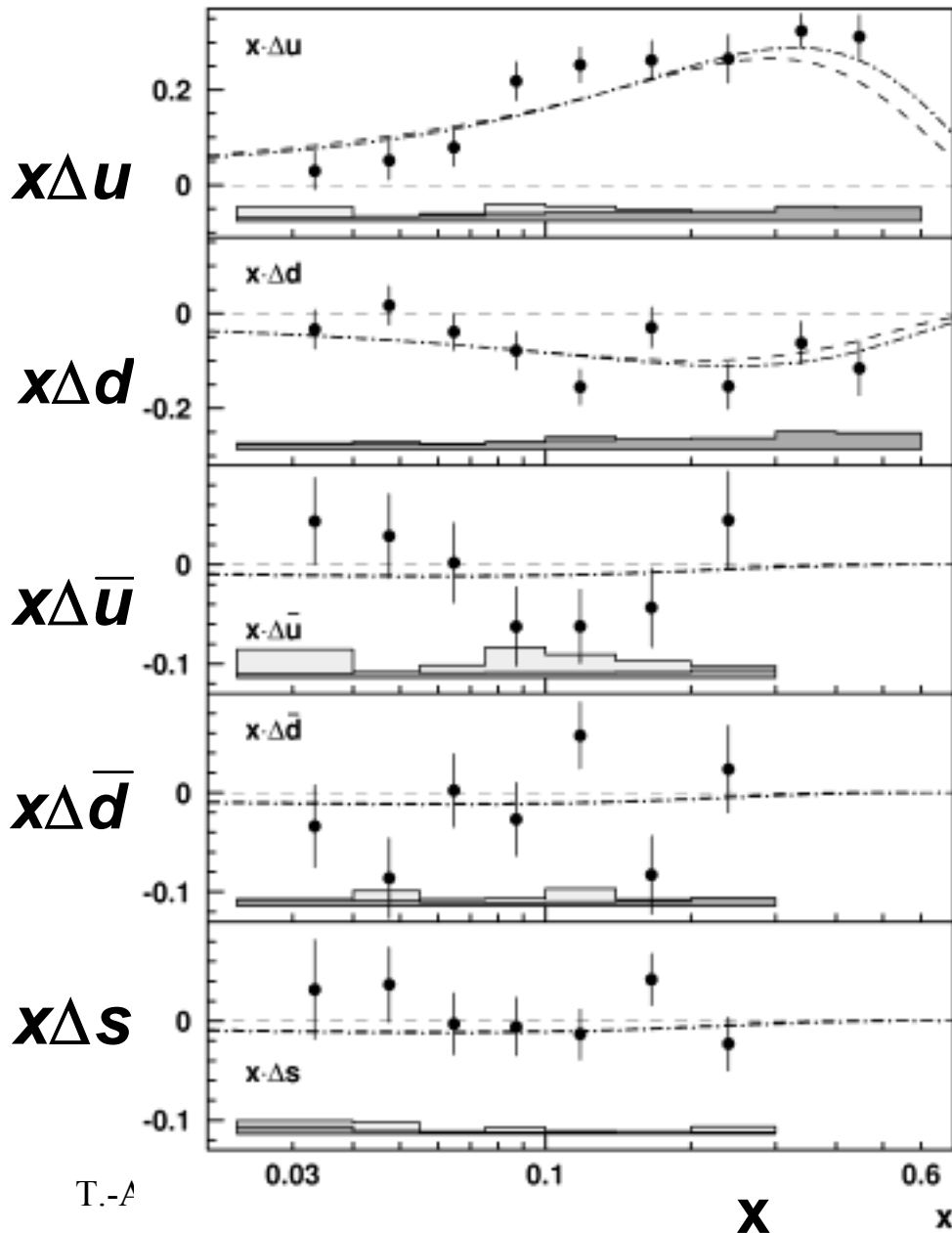
$$\vec{Q}(\mathbf{x}) = \left( \frac{\Delta u}{u}, \frac{\Delta d}{d}, \frac{\Delta \bar{u}}{\bar{u}}, \frac{\Delta \bar{d}}{\bar{d}}, \frac{\Delta s}{s} \right)$$

↑  
unpol. PDF and FF from data of  
unpol. semi-inclusive DIS

$\bar{s}$  unconstrained ←  $K^-(\bar{u}s), K^+(u\bar{s})$

# HERMES

# Flavor Separation, Quark Helicity Distributions



Result:  $\Delta u > 0$

$\Delta d < 0$

$\Delta \bar{q} \approx 0$

- X bin by bin analysis except for smearing correction.
- No functional forms are assumed.
- No first moments are assumed.
- Helicity conservation not assumed  $\frac{\Delta d}{d} \rightarrow 1$  as  $x \rightarrow 1$  etc.

Error band – systematic error

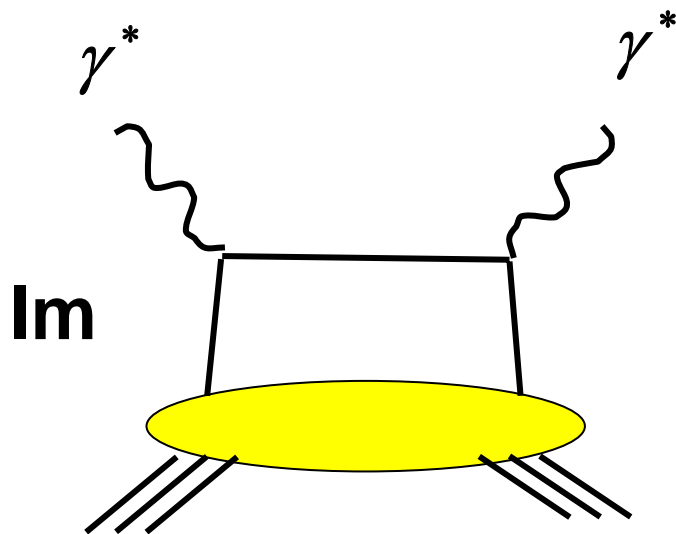
— . — QCD fits to inclusive measurements  
 - - - -

## **2. Deeply Virtual Compton Scattering**

**-- Generalized (Off-forward) Parton Distributions**

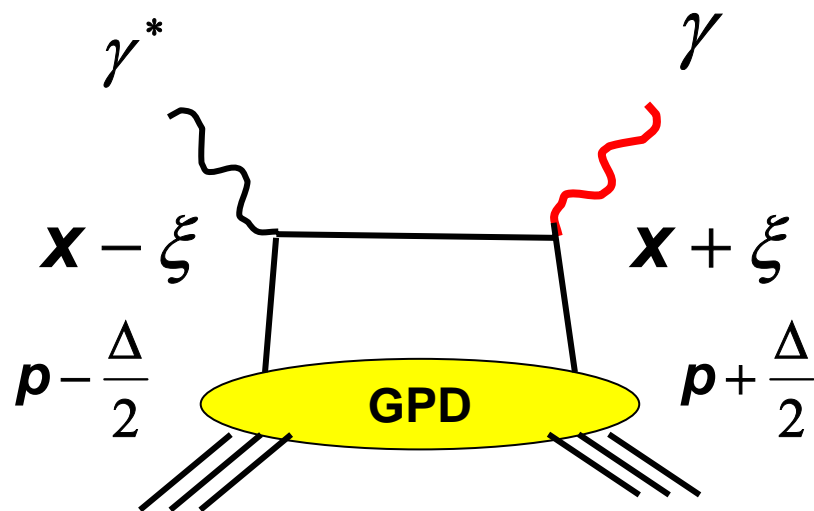
# Deeply Virtual Compton Scattering

Cross section for inclusive deep inelastic scattering



## Deeply Virtual Compton Scattering (DVCS)

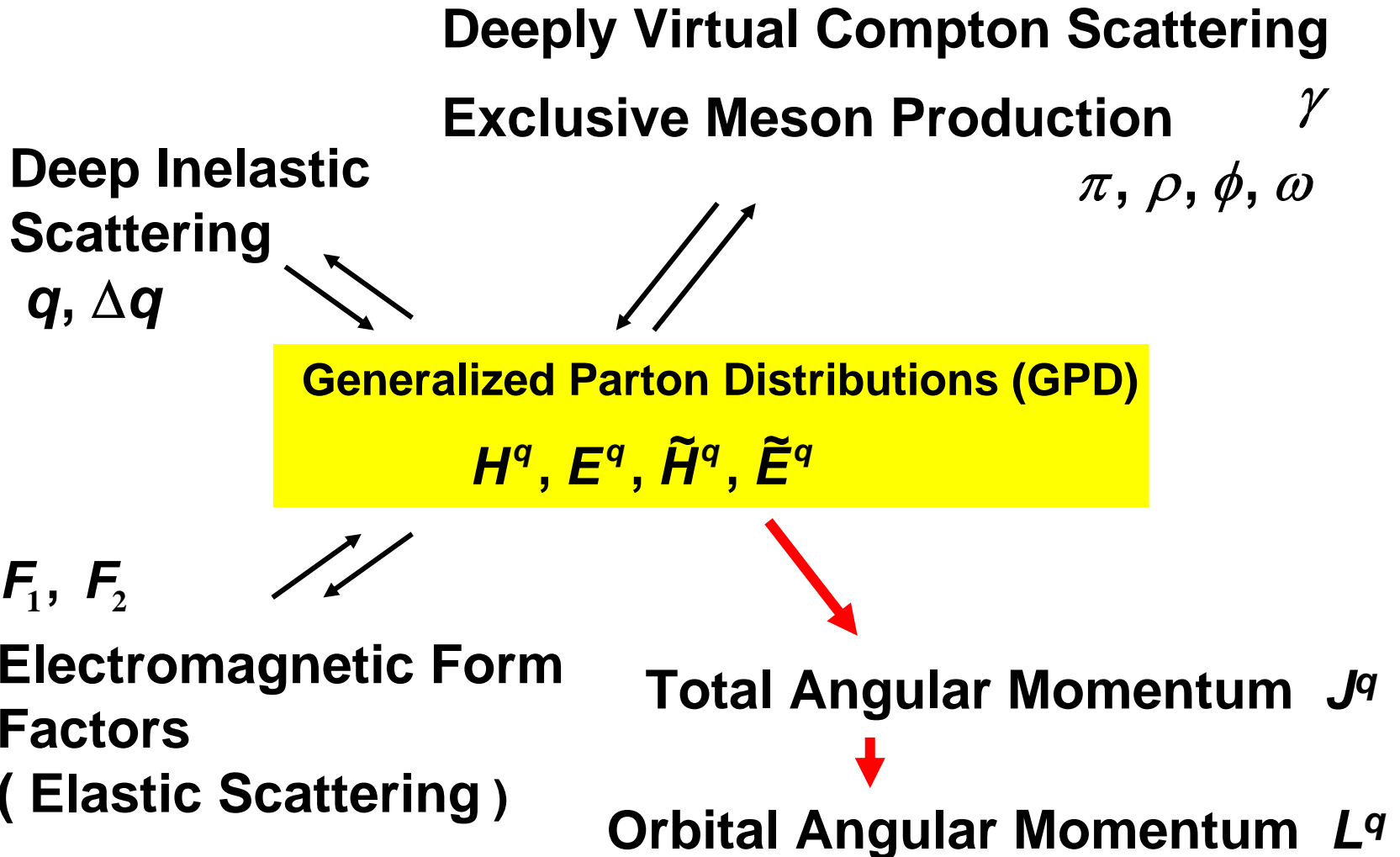
-- Exclusive production of a real photon



$\mathbf{x}$  : Light cone momentum fraction  
 $\xi = \frac{x_{BJ}}{2 - x_{BJ}}$  : Exchanged longitudinal momentum fraction  
 $\mathbf{t} = \Delta^2$  : Momentum transfer

# Generalized (Off-Forward) Parton Distributions

---





# Generalized Parton Distributions

$$H^q(x, \xi, t), \quad E^q(x, \xi, t), \quad \tilde{H}^q(x, \xi, t), \quad \tilde{E}^q(x, \xi, t)$$

**Forward limit**  $t \rightarrow 0, \quad \xi \rightarrow 0$

$$H^q(x, 0, 0) = q(x), \quad \tilde{H}^q(x, 0, 0) = \Delta q(x) \quad \text{Ordinary Quark Distributions}$$

**Sum rules,**  $x$  – integral, sum over  $q$

$$H^q(x, \xi, t) \rightarrow F_1(t), \quad E^q(x, \xi, t) \rightarrow F_2(t) \quad \text{Dirac and Pauli Nucleon Form Factors}$$

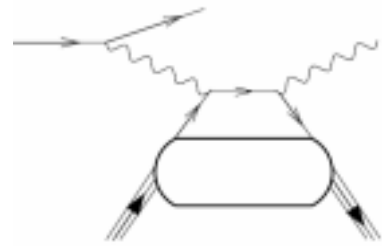
$$\tilde{H}^q(x, \xi, t) \rightarrow g_A(t), \quad \tilde{E}^q(x, \xi, t) \rightarrow h_A(t) \quad \text{Axial-vector and Pseudo-scalar Form Factors}$$

$$\lim_{t \rightarrow 0} \frac{1}{2} \int_{-1}^{+1} dx \, x [H^q(x, \xi, t) + E^q(x, \xi, t)] = \mathbf{J}^q \quad \text{2nd moment}$$

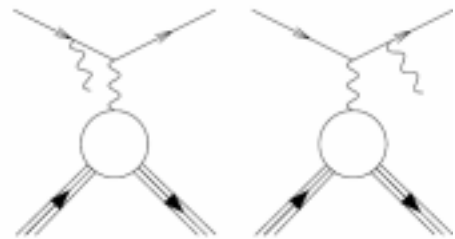
$$\mathbf{J}^q = \frac{1}{2} \Delta q + \mathbf{L}_z^q \quad \text{Total angular momentum}$$

Orbital angular momentum

## How to measure DVCS



Deeply Virtual Compton Scattering



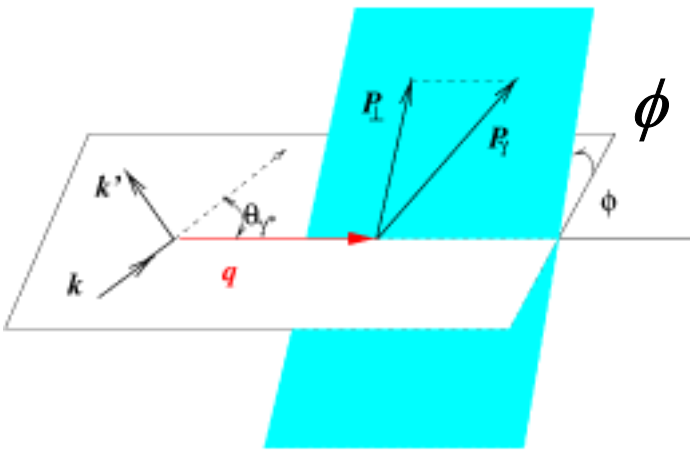
Bethe-Heitler Process, known calculable

$$\frac{d^4\sigma}{d\phi dt dQ^2 dx} \propto |A_{DVCS} + A_{BH}|^2 = |A_{DVCS}|^2 + |A_{BH}|^2 + I$$

$$\Delta\sigma_{LU} = \sigma(\vec{e}^{\pm} p) - \sigma(\vec{e}^{\mp} p) \propto \mp \sin\phi \times \text{Im } I$$

$$\Delta\sigma_{ch} = \sigma(e^+ p) - \sigma(e^- p) \propto \cos\phi \times \text{Re } I$$

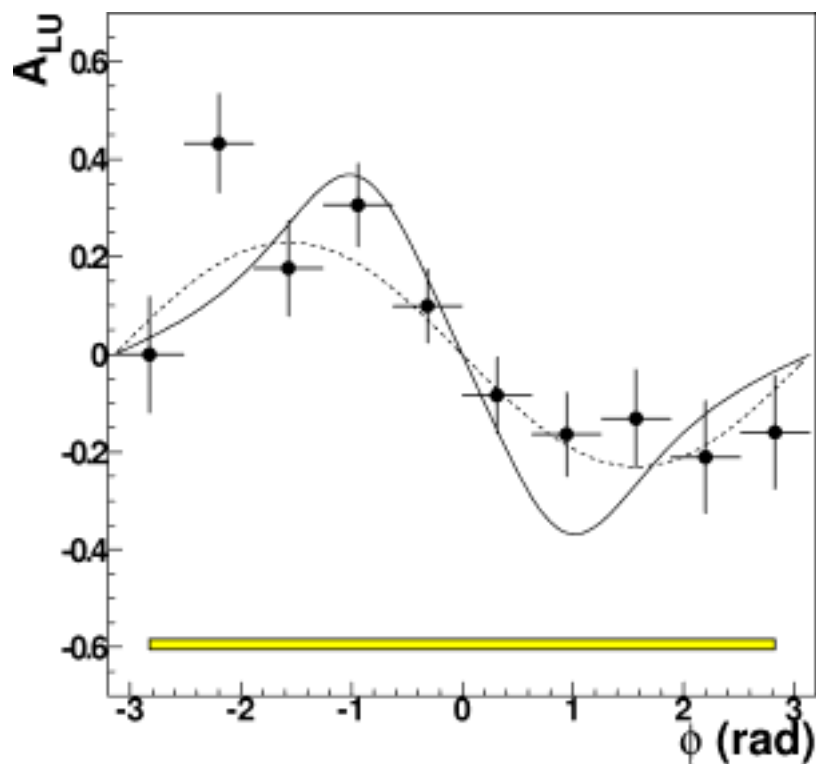
- Beam-spin asymmetry by HERMES and CLAS
- Beam-charge asymmetry by HERMES
- DVCS-BH Interference, Real and Imaginary



# Deeply Virtual Compton Scattering

## First observation of beam-spin asymmetry of DVCS

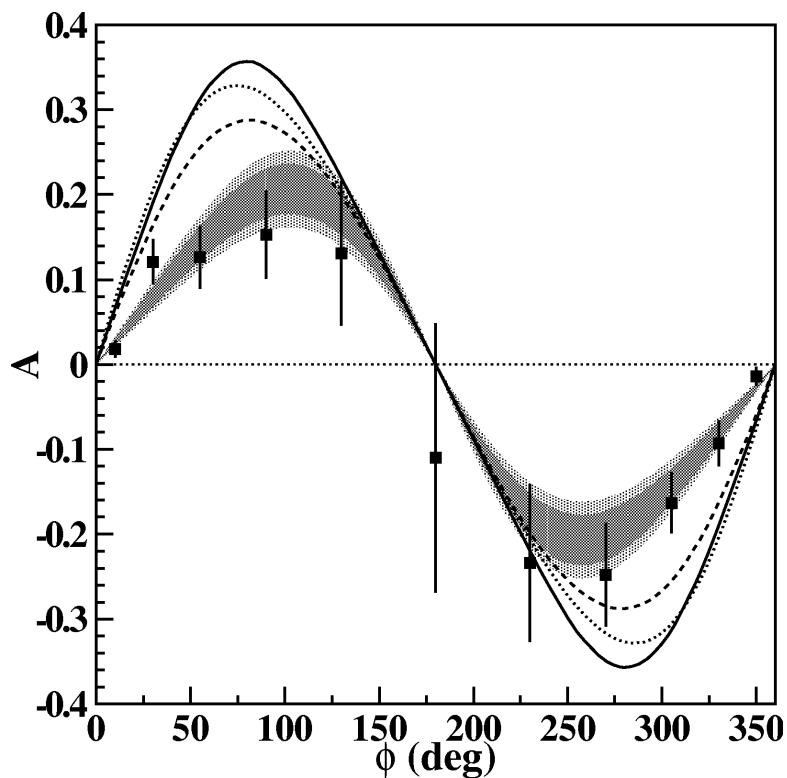
$A_{LU}$  HERMES (2001)



$\phi$

~ 30% effect

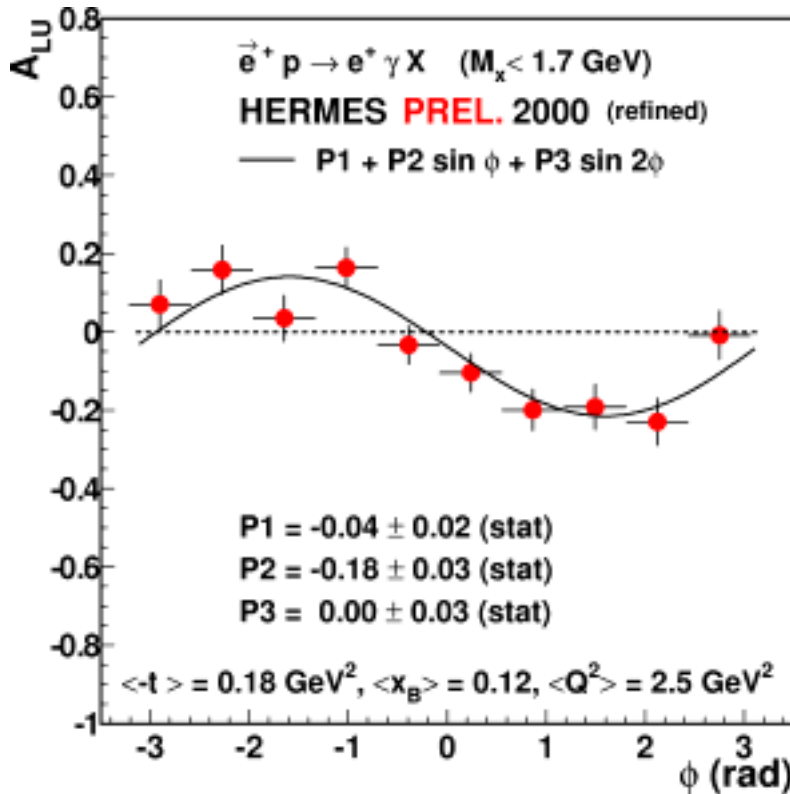
CLAS (2001)



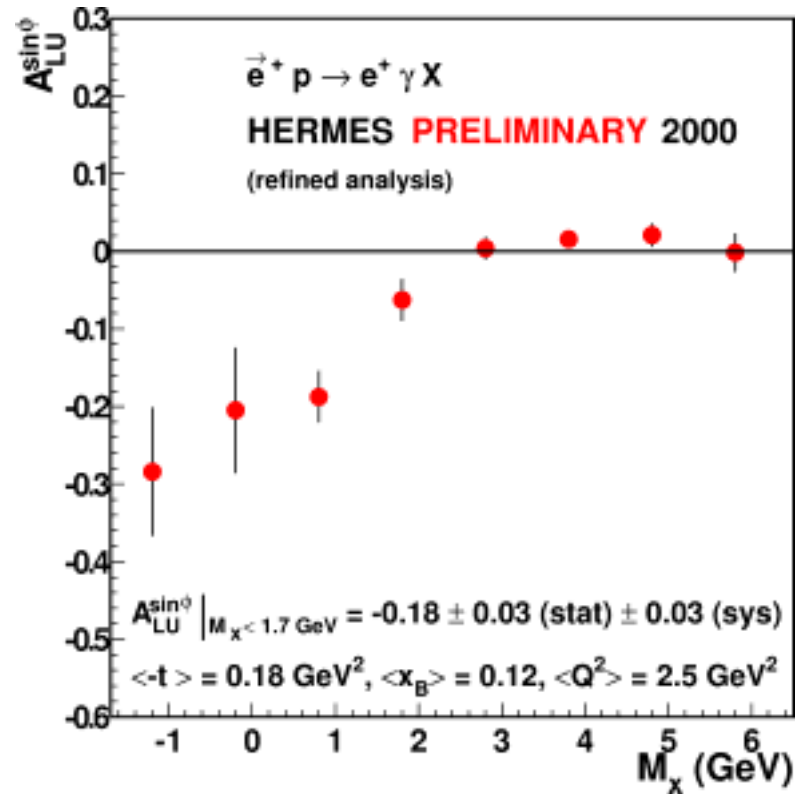
$\phi$

# Beam-Spin Asymmetry

$\sin\phi$  Moment HERMES



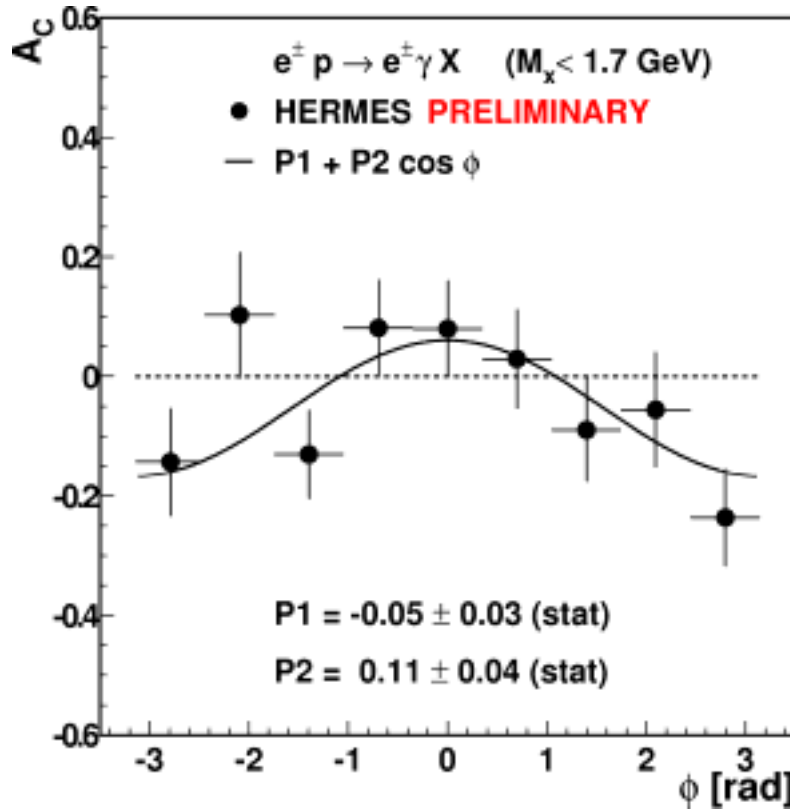
$\phi$



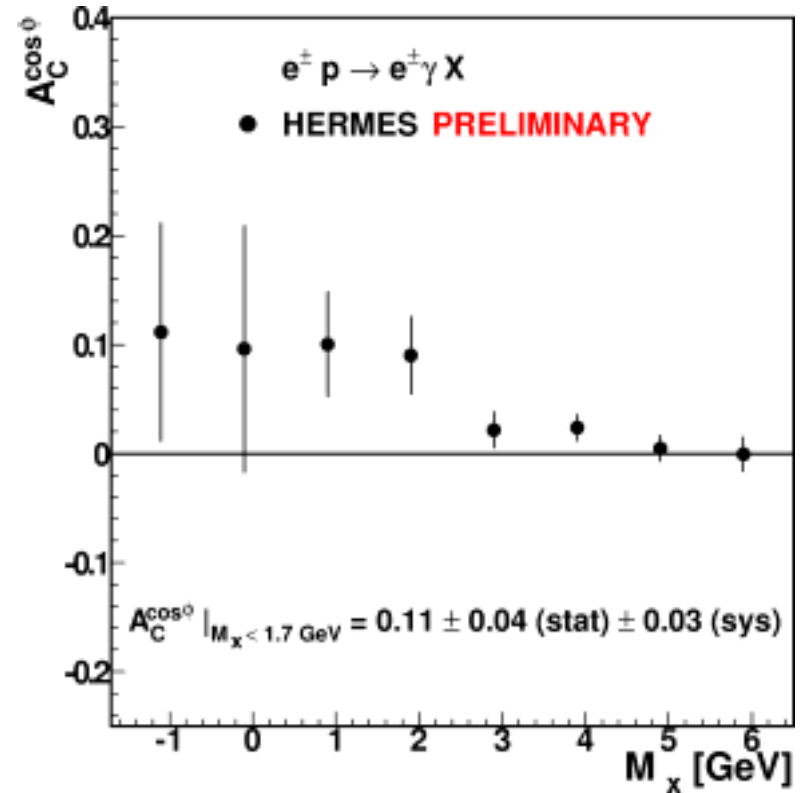
$M_x$

# Beam-Charge Asymmetry

# $\cos\phi$ Moment



$\phi$

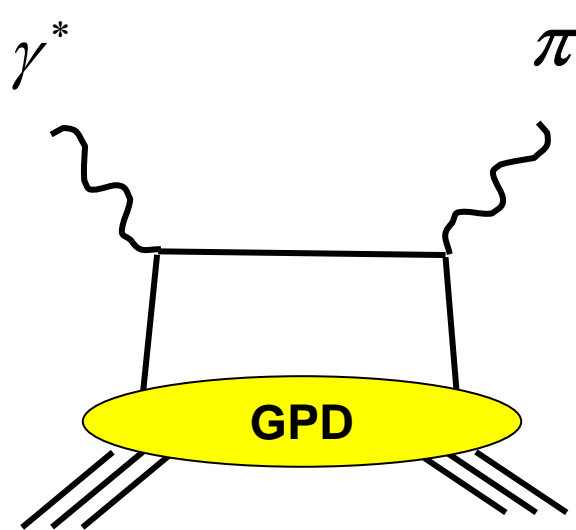


$M_x$

# How to extend

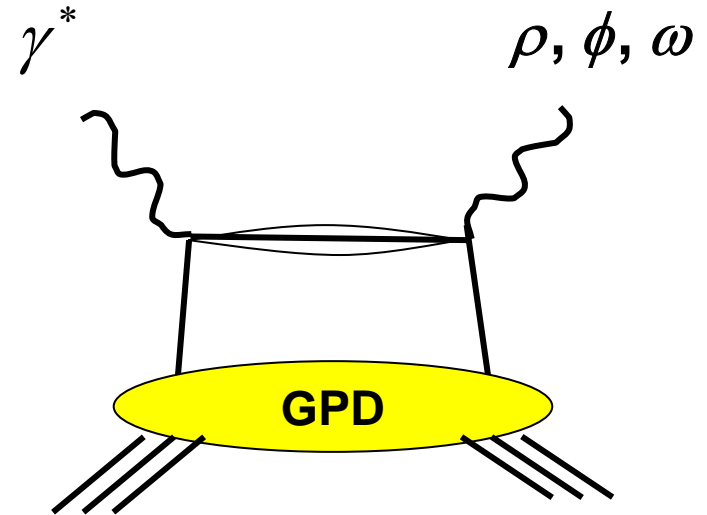
Quantum number of final state  $\longrightarrow$  Select different GPD

## Exclusive Meson Productions



Pseudo scalar meson

$$\tilde{H}^q(x, \xi, t), \tilde{E}^q(x, \xi, t)$$

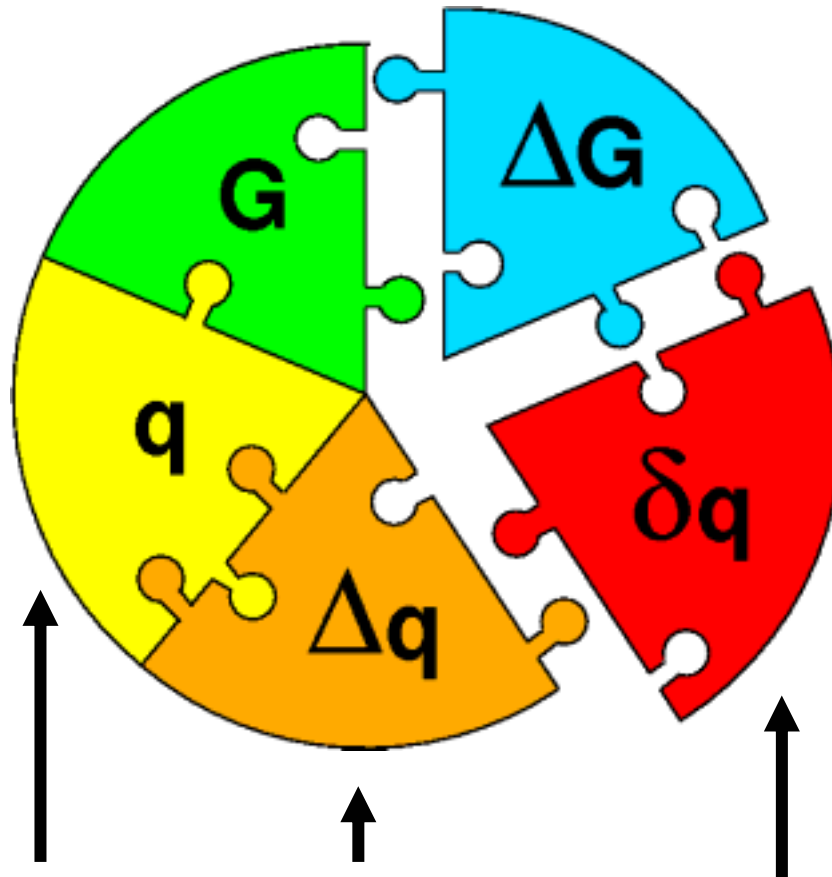


Vector meson

$$H^q(x, \xi, t), E^q(x, \xi, t)$$

### **3. Single-Spin Azimuthal Asymmetry in Semi-inclusive Deep Inelastic Scattering**

**‘Quark Transversity Distributions  $\delta q(x)$  ’**

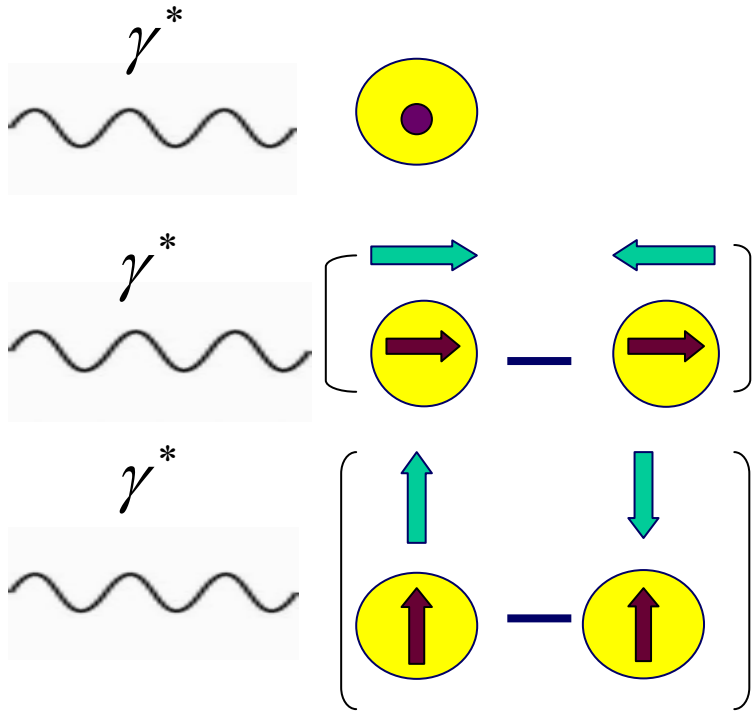


**3 leading twist quark distributions**

**$\delta q$ :** Last unmeasured leading twist distribution



# Single-Spin Azimuthal Asymmetries in Semi-Inclusive DIS, Transversity



## Quark Density Distributions

$q(x)$  Spin averaged, vector charge

## Quark Helicity Distributions

$\Delta q(x)$  Helicity difference, axial charge

## Quark Transversity Distributions

$\delta q(x)$  Helicity flip, tensor charge

$$|\delta q(x)| \leq \frac{1}{2} |q(x) + \Delta q(x)|$$

Soffer bound

$$A^h \approx \sum_q e_q^2 \delta q(x) \cdot H_{1,q}^{\perp h}(z)$$

$\delta q(x)$  is Chiral Odd. Not accessible with inclusive DIS

It is accessible with semi-inclusive DIS,

accompanied with a Chiral Odd Fragmentation Function  $H_1^\perp(z)$

$\delta q(x)$  does not couple with gluon. (Collins FF)

⇒  $Q^2$  evolution is different from  $q(x), \Delta q(x)$

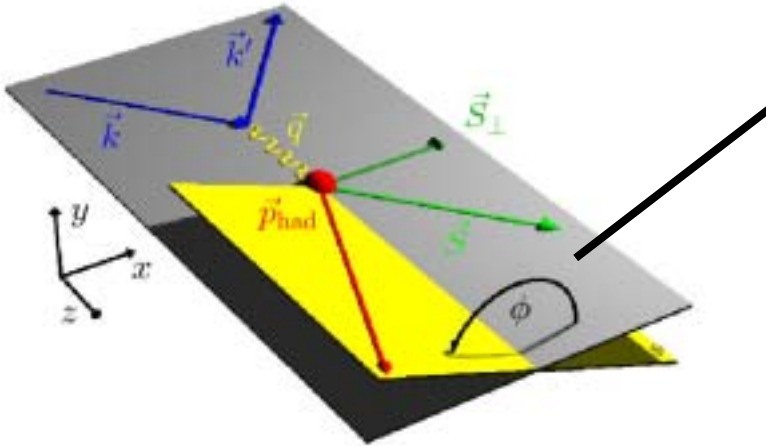
# Single-Spin Azimuthal Asymmetries in Semi-Inclusive DIS



$N \rightarrow$  HERMES, JLab

$N \uparrow$  HERMES, COMPASS, JLab

**Longitudinally  
Polarized  
Target**



Azimuthal Angle  $\phi$

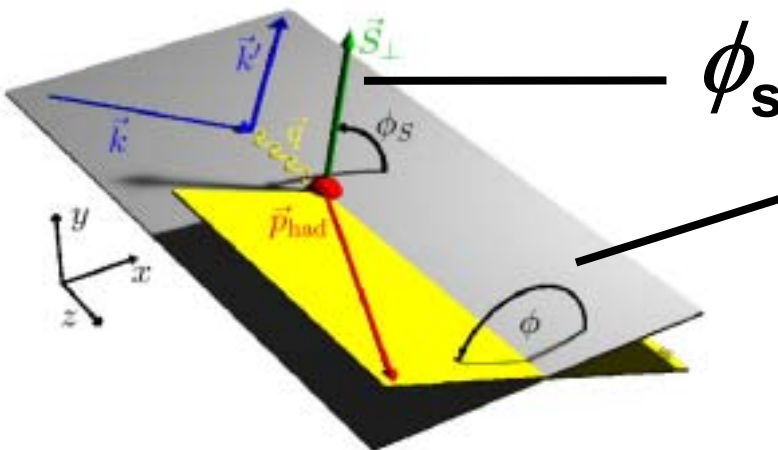
$$S_T \approx \frac{2Mx}{Q} \sqrt{1-y}$$

$$= \langle \sin \theta \gamma \rangle \approx 0.15$$

with respect to  $\gamma^*$

$\phi$  dependence

**Transversely  
Polarized  
Target**



$\phi_s$

Azimuthal Angle  $\phi$

$\phi + \phi_s$  dependence

$\phi - \phi_s$  dependence

# Single-Spin Azimuthal Asymmetries in Semi-Inclusive DIS

Longitudinally polarized target ,  
Target Spin Asymmetry  $A_{UL}$

$$\mathbf{e} + \vec{\mathbf{d}} \rightarrow \mathbf{e}' + \mathbf{m} + \mathbf{X}$$

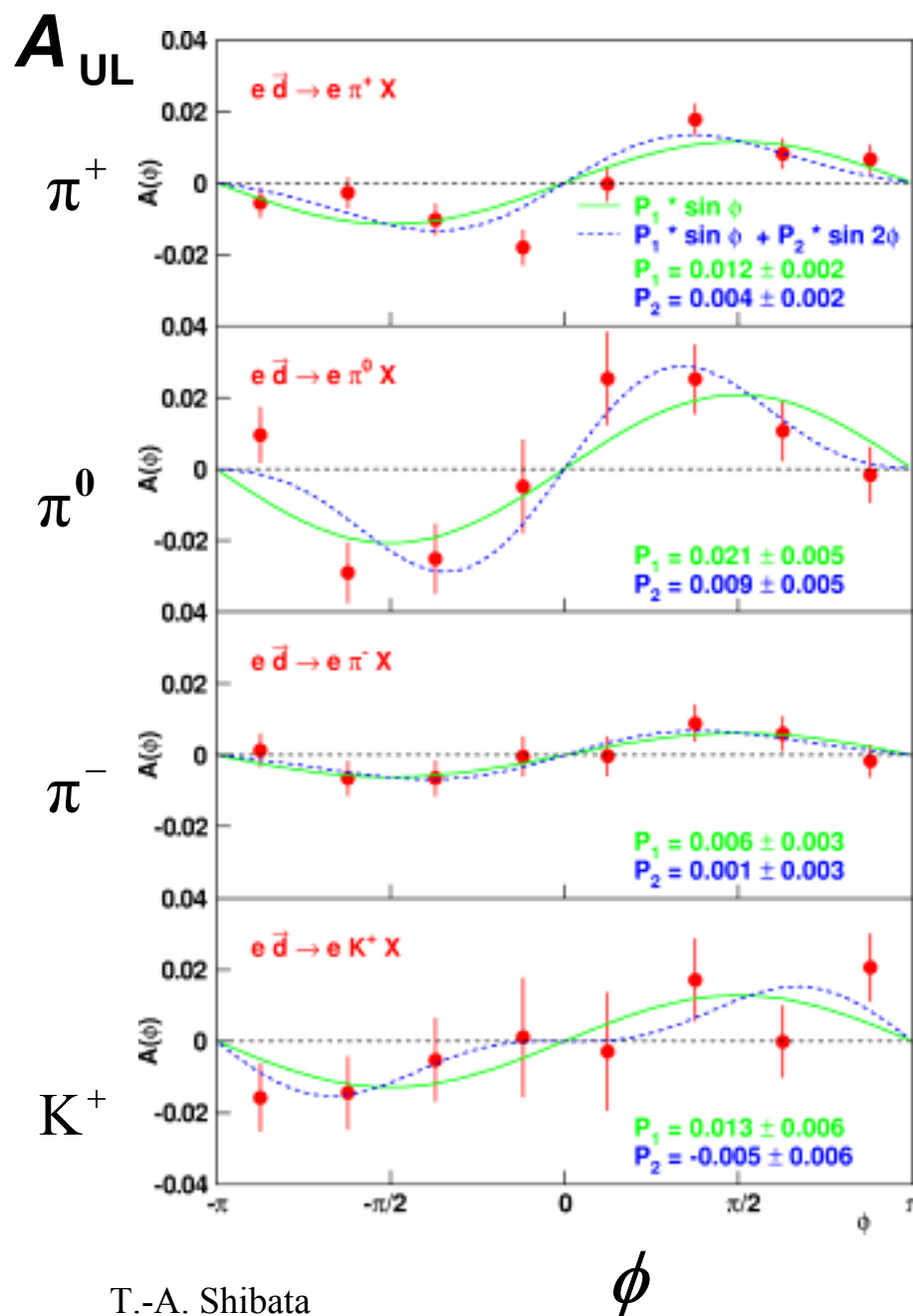
$$A_{UL}(\phi) = \frac{1}{|p_L|} \cdot \frac{N^{\rightarrow}(\phi)/L^{\rightarrow} - N^{\leftarrow}(\phi)/L^{\leftarrow}}{N^{\rightarrow}(\phi)/L^{\rightarrow} + N^{\leftarrow}(\phi)/L^{\leftarrow}}$$

—  $P_1 \cdot \sin \phi$   
- - -  $P_1 \cdot \sin \phi + P_2 \cdot \sin 2\phi$

$\rightarrow A_{UL}^{\sin \phi}$  positive for  $\pi^+, \pi^0, K^+$   
 Increases with  $x$   
 nearly zero for  $\pi^-$

$\sin 2\phi$  moment  $\sim 0$

HERMES



$$A_{UL}^{\sin\phi} \sim \mathbf{S}_L \langle \sin\phi \rangle_{UL} - \mathbf{S}_T \langle \sin\phi \rangle_{UT}$$

**Origins of  $\langle \sin\phi \rangle$  moment, Longitudinally polarized target**

$$\phi_S = 0$$

$$\langle \sin\phi \rangle_{UL} \sim \frac{1}{Q} \sum_q e_q^2 (h_L^q(x) H_1^{\perp,q}(z) - \frac{1}{z} h_{1L}^{\perp,q}(x) \tilde{H}(z))$$

$$\langle \sin\phi \rangle_{UT} \sim \sum_q e_q^2 \delta q(x) H_1^{\perp,q}(z)$$

**Collins Effect:**

(Quark transversity distribution) x (Chiral odd FF)

$$\sim \sum_q e_q^2 f_{1T}^{\perp}(x) D_1^q(z)$$

**Sivers Effect:**

(  see also polarized pp collisions )

**Transversely** polarized target data can distinguish between the two.  $\mathbf{S}_T$  becomes dominant.

$$\langle \sin(\phi + \phi_S) \rangle_{UT} \text{ moment: } \mathbf{Collins Effect}$$

$$\langle \sin(\phi - \phi_S) \rangle_{UT} \text{ moment: } \mathbf{Sivers Effect}$$

HERMES (2002--) focused on it. 700K D.I.S. events recorded.

Further data taking 2003-- . COMPASS data at higher  $Q^2$ , JLab

# Polarized Proton-Proton Collisions

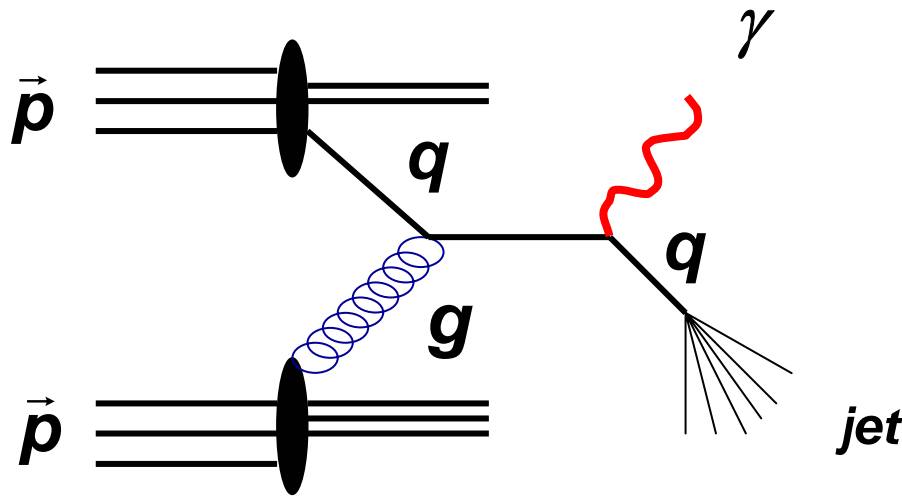
# Polarized Proton-Proton Collision

## Polarized Parton-Parton Collision

### **Gluon spin** contribution to the nucleon spin

#### Gluon Compton scattering

$$g + q \rightarrow \gamma + q$$



#### 2 jet production

Inclusive  $\pi^0$   
measurement

$$g + g \rightarrow \text{jet } (\pi^0) + \text{jet}$$

$$g + q$$

$$q + q$$

$$A_{LL} \propto \frac{\Delta G(x_1)}{G(x_1)} \cdot \frac{\Delta q(x_2)}{q(x_2)} \cdot \hat{a}_{LL}$$

# Polarized pp Collisions at RHIC

---

**100 GeV + 100 GeV**

**2001/2002    P = ~0.2,   Int L ~ 0.3 pb<sup>-1</sup>,   transverse**

**- May 2003    P = ~0.3,   Int L ~ 0.8 pb<sup>-1</sup>,   transverse +  
**longitudinal****

**Physics Goal   P = 0.7,   Int L = 320 pb<sup>-1</sup> , at 100 + 100 GeV  
800 pb<sup>-1</sup> , at 250 + 250 GeV**

# Polarized pp Collisions at RHIC

## PHENIX and STAR collected data of inclusive $\pi^0$ production

Single-Spin Asymmetry,  
Transversely Polarized  
Beam

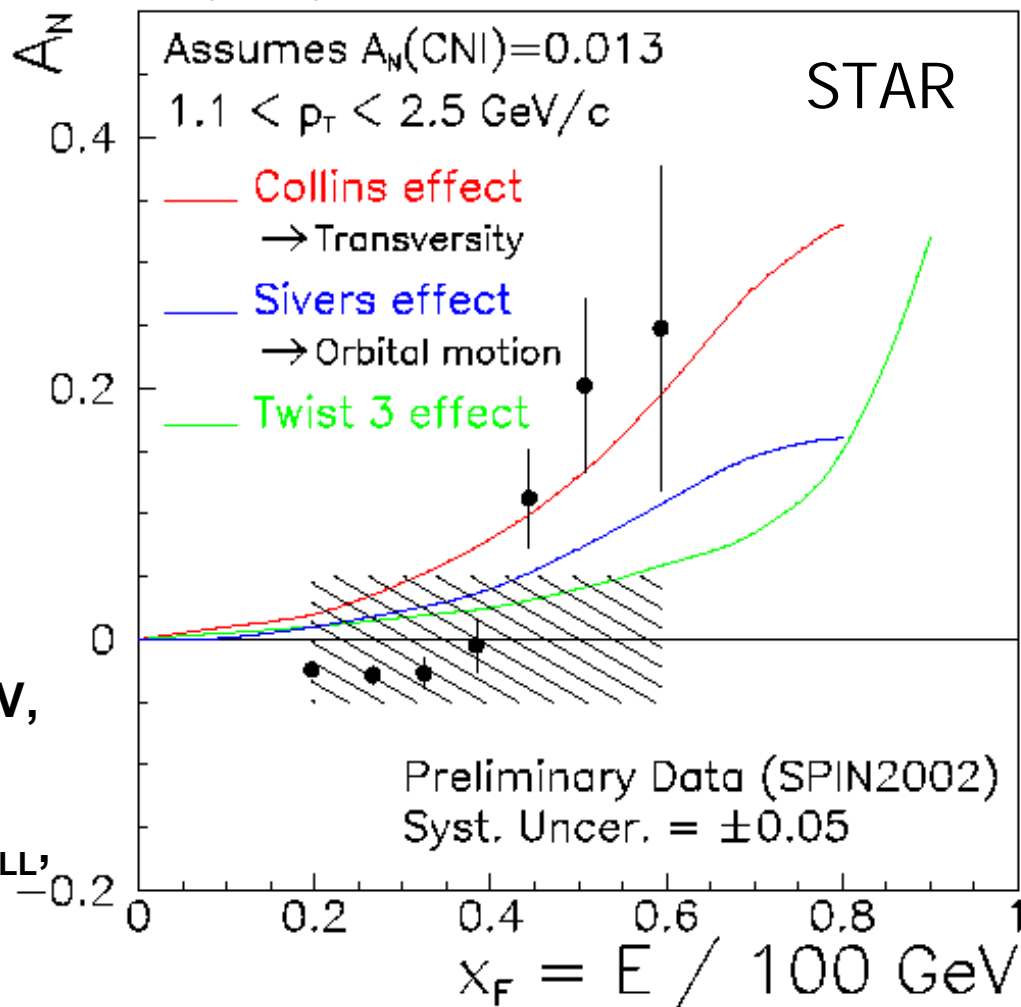
$$p_{\uparrow} + p \rightarrow \pi^0 + X,$$

$$\sqrt{s} = 200 \text{ GeV}$$

Forward  $\pi^0$ , small  $p_T$

Similar to the earlier  
Fermilab data at  $\sqrt{s}=20 \text{ GeV}$ ,  
 $p_T = 0.5\text{-}2.0 \text{ GeV}/c$

Double spin asymmetry,  $A_{LL}$ ,  
at large  $p_T$  will become  
available soon





# Conclusions 1

---

- To understand hadrons in terms of QCD, **Spin Structure of the Nucleon** is an important subject.
- Many experiments are currently running with  $e, \mu, \gamma, p \dots$  beams at different labs in the world.
- Flavor separation of quark helicity distributions  $\Delta q$  has been made.
- **Deeply Virtual Compton Scattering** provides access to **Generalized Parton Distributions**.
- Single-spin azimuthal asymmetries in semi-inclusive DIS have been observed. **Quark Transversity Distributions**  $\delta q$  is a new subject which is being investigated. Results from transversely polarized targets will become available soon.

## Conclusions 2

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- Polarized proton-proton collider has now longitudinally as well as transversely polarized beams. Single-spin asymmetries in  $\pi^0$  productions at small angles from transversely polarized beam have been obtained. The asymmetries at large  $p_T$  are being analyzed.
- Spin physics with the nucleon is a rapidly expanding field. Many **new ideas** of measurements are being proposed. **High precision data** as well as **new surprises** are expected.

