

# Combining electroweak and QCD corrections to weak boson production at hadron colliders

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LoopFest VI  
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with G. Balossini, C.M. Carloni Calame, M. Moretti, O. Nicrosini, F. Piccinini,  
M. Treccani, A. Vicini

and also based on work and collaboration with  
A. Arbuzov, D. Bardin, U. Baur, M. Bellomo, S. Dittmaier, S. Jadach,  
M. Krämer, G. Polesello, W. Placzek, V. Vercesi, D. Wackerath...

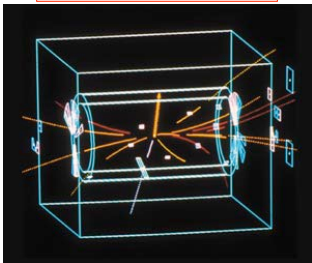
# At CERN, about 20 years ago...



The Nobel Prize in Physics 1984  
to C. Rubbia and S. van der Meer

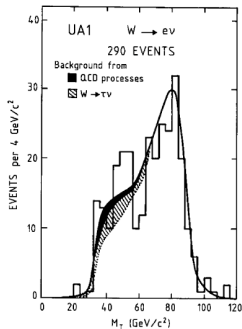


One of the first W particles



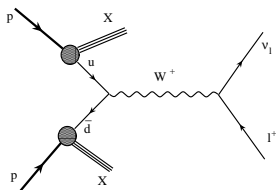
"for their decisive contributions to the large project, which led to the discovery of the field particles W and Z, communicators of weak interaction"

D. Denegri  
The discovery of the W and Z  
Physics Report **403** (2004) 107



# ...at Fermilab today and at CERN, in the near future

Single  $W/Z$  boson production: **clean process with a large cross section** ( $\sim 300(35) \times 10^6$  events/year for  $\mathcal{L}_{\text{LHC}} = 10 \text{ fb}^{-1}$ ). It is useful

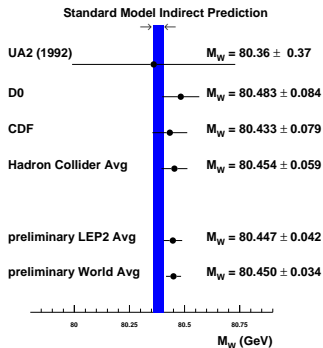


- to derive **precise measurements of the electroweak parameters**  $M_W$ ,  $\Gamma_W$ ,  $\sin^2 \theta_{\text{eff}}^\ell$ . Relevant observables: leptons' transverse momentum  $p_\perp$ ,  $W$  transverse mass  $M_\perp^W$ , ratio of  $W/Z$  distributions, forward-backward asymmetry  $A_{FB}^Z$ ...
- to monitor the **collider luminosity** and constrain the **parton distribution functions** (PDFs). Relevant observables: total cross section,  $W$  rapidity  $y_W$  and charge asymmetry  $A(y_\ell)$ , lepton pseudorapidity  $\eta_\ell$ ...
- to search for **new physics**. Relevant observables:  $Z$  invariant mass distribution  $M_{\ell\ell}^Z$  and  $W$  transverse mass  $M_\perp^W$  in the high tail...

# The quest for precision: $W$ mass $\delta M_W/M_W \sim 7 \rightarrow 2 \times 10^{-4}$

## ● Present (official) experimental status

TeVWWG, Phys. Rev. **D70** (2004) 092008



## Future goals:

### Target $\Delta M_W$ precision:

★ Tevatron RunII:  $\sim 25$  MeV

★ LHC: 15-20 MeV

### Target $\Delta \Gamma_W$ precision:

★ Tevatron RunII: 30 MeV

★ LHC:  $\leq 30$  MeV

★ At the Tevatron, NLO QED corrections shift  $M_W$  by  $\sim 100$  MeV ★

electron channel:  $-65 \pm 20$  MeV

muon channel:  $-168 \pm 20$  MeV

# Higher-order QCD & QCD generators

- NLO/NNLO corrections to  $W/Z$  total production rate

G. Altarelli, R.K. Ellis, M. Greco and G. Martinelli, Nucl. Phys. **B246** (1984) 12

R. Hamberg, W.L. van Neerven, T. Matsuura, Nucl. Phys. **B359** (1991) 343

- NLO calculations for  $W, Z + 1, 2$  jets (**DYRAD**, **MCFM** ...)

W.T. Giele, E.W.N. Glover and D.A. Kosower, Nucl. Phys. **B403** (1993) 633

J.M. Campbell and R.K. Ellis, Phys. Rev. **D65** (2002) 113007

- resummation of leading/next-to-leading  $p_{\perp}^W / M_W$  logs (**ResBos**)

C. Balazs and C.P. Yuan, Phys. Rev. **D56** (1997) 5558

- NLO corrections merged with **HERWIG** Parton Shower (**MC@NLO**)

S. Frixione and B.R. Webber, JHEP **0206** (2002) 029

- Multi-parton matrix elements Monte Carlos (**ALPGEN**, **SHERPA**...) matched with vetoed Parton Showers

M.L. Mangano *et al.*, JHEP **0307** (2003) 001

F. Krauss *et al.*, JHEP **0507** (2005) 018

- fully differential NNLO corrections to  $W/Z$  production (**FEWZ**)

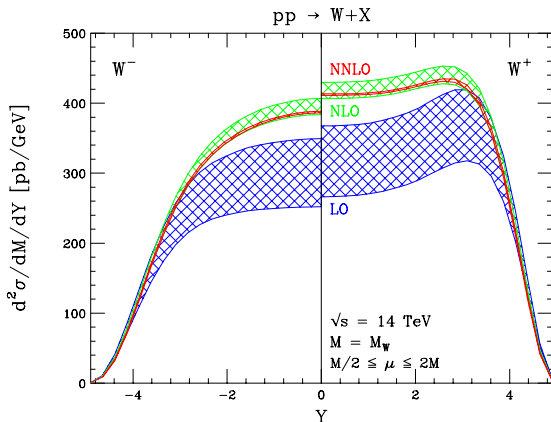
C. Anastasiou *et al.*, Phys. Rev. **D69** (2004) 094008

K. Melnikov and F. Petriello, Phys. Rev. Lett. **96** (2006) 231803, Phys. Rev. **D74** (2006) 114017



# High-precision QCD: $W/Z$ rapidity @ NNLO

C. Anastasiou *et al.*, Phys. Rev. Lett. **91** (2003) 182002  
C. Anastasiou *et al.*, Phys. Rev. **D69** (2004) 094008



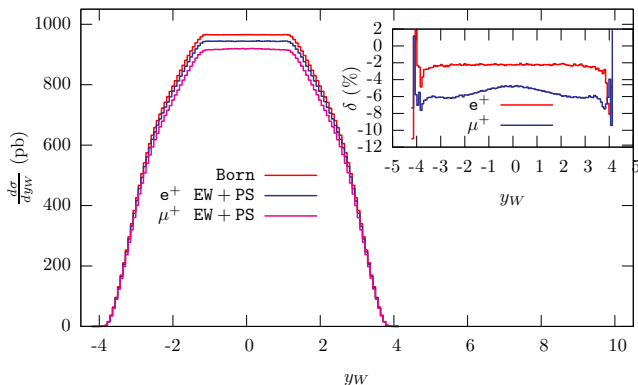
- NNLO QCD corrections to  $W/Z$  rapidity at  $\sim 2\%$  at the LHC and residual scale dependence below 1%
- $\mathcal{O}(\alpha_S^2) \approx \mathcal{O}(\alpha_{em}) \rightarrow$  need to worry about electroweak corrections!

# Electroweak corrections to $W$ rapidity

C.M. Carloni Calame *et al.*, JHEP **0612** (2006) 016

$pp \rightarrow W^+ \rightarrow \ell^+ \nu_\ell (+\gamma)$  at LHC

$G_\mu$  scheme and including detector effects



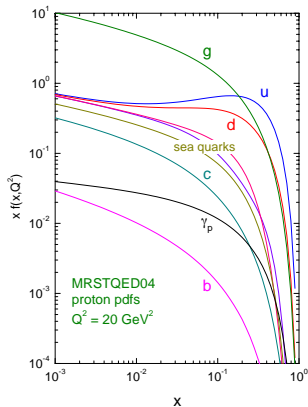
- NLO electroweak corrections to  $W$  rapidity are of the same order of NNLO QCD and PDFs uncertainty  $\rightarrow$  **relevant for precision luminosity and PDFs constraints!**

- $\mathcal{O}(\alpha)$  QED corrections to  $W/Z$  lepton decays  
F.A. Berends *et al.* Z. Physik **C27** (1985) 155,365
- Electroweak corrections to  $W$  production
  - ★ Pole approximation ( $\sqrt{\hat{s}} = M_W$ )  
D. Wackeroth and W. Hollik, Phys. Rev. **D55** (1997) 6788  
U. Baur, S. Keller, D. Wackeroth, Phys. Rev. **D59** (1999) 013002 WGRAD
  - ★ Complete  $\mathcal{O}(\alpha)$  corrections  
V.A. Zykunov, Eur. P. J. **C3** (2001) 9, Phys. Atom. Nucl. **69** (2006) 1522  
S. Dittmaier and M. Krämer, Phys. Rev. **D65** (2002) 073007 DK  
U. Baur and D. Wackeroth, Phys. Rev. **D70** (2004) 073015 WGRAD2  
A. Arbuzov *et al.*, Eur. Phys. J. **C46** (2006) 407 SANC  
C.M. Carloni Calame *et al.*, JHEP **12** (2006) 016 HORACE
- Electroweak corrections to  $Z$  production
  - ★  $\mathcal{O}(\alpha)$  photonic corrections  
U. Baur, S. Keller, W.K. Sakumoto, Phys. Rev. **D57** (1998) 199 ZGRAD
  - ★ Complete  $\mathcal{O}(\alpha)$  corrections  
U. Baur *et al.*, Phys. Rev. **D65** (2002) 033007 ZGRAD2



# QED initial-state singularities & QED-improved PDFs

## MRST2004QED



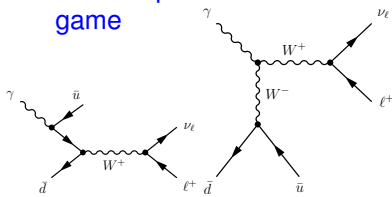
- QED initial-state collinear singularities are universal  $\longrightarrow$  can be absorbed into PDFs
- effect of QED evolution on PDFs through DGLAP equation is **small** ( $\sim 0.1\%$  for  $x < 1$ )

H. Spiesberger, Phys. Rev. **D52** (1995) 4936

M. Roth and S. Weinzierl, Phys. Lett. **B590** (2004) 190

A.D. Martin *et al.*, Eur. Phys. J. **C39** (2005) 155

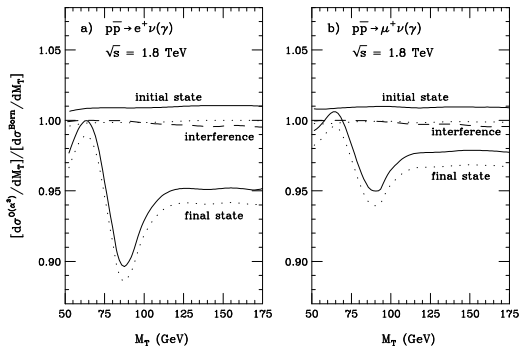
- dynamic generation of photon parton distribution  $\longrightarrow$  **photon induced processes enter the game**



# Electroweak vs final-state photon corrections

U. Baur, S. Keller, D. Wackerath, Phys. Rev. **D59** (1999) 013002

Pole approximation



- Around the  $W$  peak, electroweak corrections amount to **several per cents** and are dominated by **final-state photon radiation**
- **final-state photon radiation (FSR)** modifies the shape of the distributions and is important because it contains mass logarithms of the form  $\log(\hat{s}/m_\ell^2) \rightarrow$  **need to exponentiate FSR!**

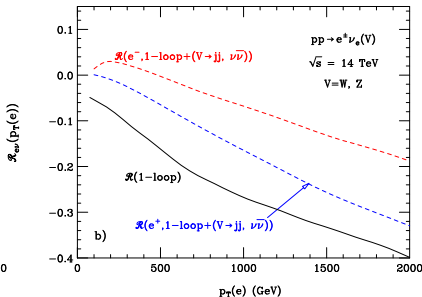
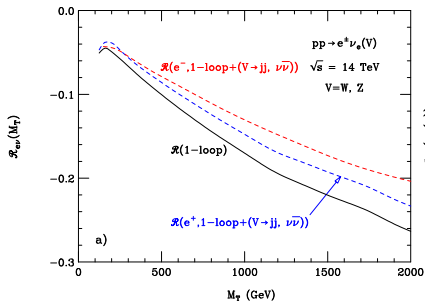
# Electroweak Sudakov logs

S. Dittmaier and M. Krämer, Phys. Rev. **D65** (2002) 073007

U. Baur *et al.*, Phys. Rev. **D65** (2002) 033007

U. Baur and D. Wackerath, Phys. Rev. **D70** (2004) 073015

Complete NLO<sub>EW</sub> calculations



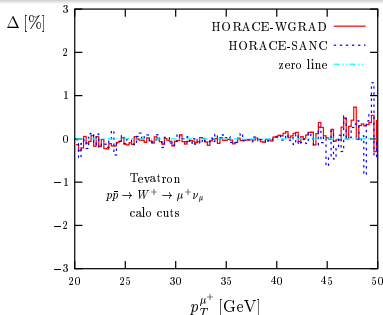
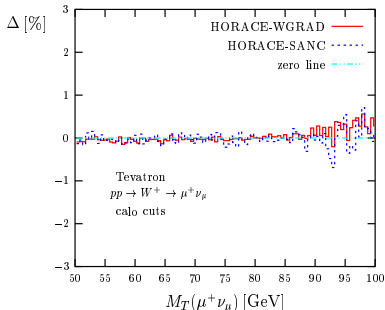
- Pole approximation fails for  $M_{\perp} \gg M_V$ ,  $V = W, Z$ , due to large Sudakov ew logs  $-(\alpha/\pi) \log^2(\hat{s}/M_V^2) \rightarrow$  important for new physics!
- radiation of (undetected) real vector bosons partially cancels the Sudakov logs, e.g.  $pp \rightarrow e^+ \nu_e V + X$   $V \equiv W, Z$   $V \rightarrow jj, \nu\bar{\nu}, \dots$

U. Baur, Phys. Rev. **D75** (2007) 013005

Courtesy of D. Wackeroth

## Process and scheme – Detector modeling and lepton identification

- 1  $p\bar{p}(pp) \rightarrow W^+ \rightarrow \ell^+ \nu_\ell (+\gamma) - \alpha(0), G_\mu, M_Z \rightarrow M_W$  at two – loops
- 2  $\sqrt{s} = 1.96$  TeV, 14 TeV  $p_{\perp, \ell} > 20$  GeV  $\cancel{p}_{\perp} > 20$  GeV  $|\eta_\ell| < 2.5$
- 3 Bare (w/o recombination and smearing) and Calo (with recombination and smearing) event selection  $\Delta R(e, \gamma) = \sqrt{(\Delta\eta(e, \gamma))^2 + (\Delta\phi(e, \gamma))^2} < 0.1$



- Electroweak generators agree within their statistical precision → NLO  
electroweak corrections to  $W$  production well under control!
- Comparisons on electroweak corrections to  $Z$  production in progress

# Multiple photon corrections & tools

- Higher-order (real+virtual) QED corrections to  $W/Z$  production
  - **HORACE** (Pavia): **QED Parton Shower** + NLO electroweak corrections to  $W/Z$  production ( $Z$  production available soon)  
C.M. Carloni Calame *et al.*, Phys. Rev. **D69** (2004) 037301  
C.M. Carloni Calame *et al.*, JHEP **05** (2005) 019; JHEP **12** (2006) 016
  - **WINHAC** (Cracow): **YFS exponentiation** + electroweak corrections to  $W$  decay  
S. Jadach and W. Płaczek, Eur. Phys. J. **C29** (2003) 325

- Perfect agreement between **HORACE** and **WINHAC** on multiphoton corrections to all  $W$  observables  
C.M. Carloni Calame *et al.*, Acta Phys. Pol. **B35** (2004) 1643

- Recent effort to improve the treatment of multiphoton radiation in HERWIG (with **SOPHTY** via YFS) and **PHOTOS** (via QED Parton Shower)  
K. Hamilton and P. Richardson, JHEP **0607** (2006) 010  
P. Golonka and Z. Was, Eur. Phys. J. **C45** (2006) 97

- ★  $W$ -mass shift due to multiphoton radiation is about **10%** of that caused by one photon emission → **non-negligible for precision  $W$  mass measurements!**

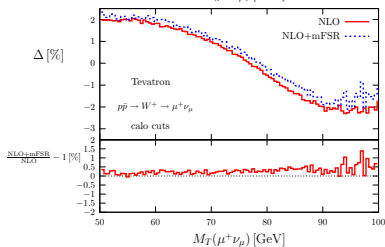
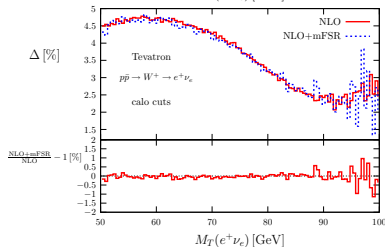
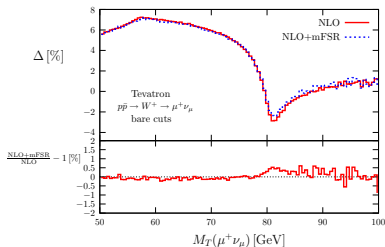
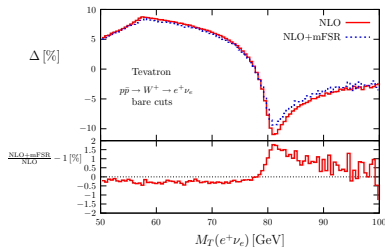
C.M. Carloni Calame *et al.*, Phys. Rev. **D69** (2004) 037301



# Multiple photon corrections by HORACE

C. E. Gerber *et al.*, FERMILAB-CONF-07-052

Courtesy of D. Wackerath



- For **bare**  $e - \mu$  multiple photon corrections enhance the NLO electroweak corrections by  $\sim 1.5\% - 0.5\%$ . For **calo**  $e - \mu$  they survive for  $\mu$  only.

# Combining electroweak and QCD corrections

- First attempt: combination of soft-gluon resummation with NLO final-state QED corrections

Q.-H. Cao and C.-P. Yuan, Phys. Rev. Lett. **93** (2004) 042001  
ResBos-A

- Electroweak and QCD corrections can be combined in factorized form to arrive at

$$\left[ \frac{d\sigma}{d\mathcal{O}} \right]_{\text{QCD} \otimes \text{EW}} = \left\{ \frac{d\sigma}{d\mathcal{O}} \right\}_{\text{QCD}} + \left\{ \left[ \frac{d\sigma}{d\mathcal{O}} \right]_{\text{EW}} - \left[ \frac{d\sigma}{d\mathcal{O}} \right]_{\text{LO}} \right\}_{\text{HERWIG PS}}$$

- **QCD**  $\Rightarrow$  ResBos, MC@NLO, ALPGEN (with CKKW-MLM Parton Shower matching and standard matching parameters), FEWZ, ...

- **EW**  $\Rightarrow$  **Electroweak + multiphoton corrections** from HORACE convoluted with HERWIG QCD Parton Shower

- ★ NLO electroweak corrections are interfaced to QCD Parton Shower evolution  $\Rightarrow \mathcal{O}(\alpha\alpha_s)$  corrections not reliable when hard non-collinear QCD radiation is important
- ★ Beyond this approximation, a full two-loop  $\mathcal{O}(\alpha\alpha_s)$  calculation is needed (unavailable yet)

J.H. Kühn *et al.*, hep-ph/0703283  
NLO/NNLO<sub>EW</sub> to  $pp \rightarrow Wj$



# Monte Carlo “tuning”: Tevatron and LHC

Monte Carlo	ALPGEN	FEWZ	HORACE	ResBos-A
$\sigma_{\text{LO}}$ (pb)	906.3(3)	906.20(16)	905.64(4)	905.26(24)

**Table:** MC tuning at the Tevatron for the LO cross section with cuts of the process  $p\bar{p} \rightarrow W^\pm \rightarrow \mu^\pm \nu_\mu$ , using CTEQ6M with  $\mu_R = \mu_F = \sqrt{x_1 x_2 s}$

Monte Carlo	ALPGEN	FEWZ	HORACE
$\sigma_{\text{LO}}$ (pb)	8310(2)	8304(2)	8307.9(2)

**Table:** MC tuning at the LHC for the LO cross section with cuts of the process  $pp \rightarrow W^\pm \rightarrow \mu^\pm \nu_\mu$ , using MRST2004QED with  $\mu_R = \mu_F = \sqrt{p_{\perp,W}^2 + M_W^2}$

Monte Carlo	$\sigma_{\text{NLO}}^{\text{Tevatron}}$ (pb)	$\sigma_{\text{NLO}}^{\text{LHC}}$ (pb)
MC@NLO	2638.8(4)	20939(19)
FEWZ	2643.0(8)	21001(14)

**Table:** MC tuning for MC@NLO and FEWZ NLO inclusive cross sections of the process  $p\bar{p} \rightarrow W^\pm \rightarrow \mu^\pm \nu_\mu$ , with CTEQ6M (Tevatron) and MRST2004QED (LHC)

- ★ After appropriate “tuning”, and with same input parameters, cuts and PDFs, Monte Carlos **agree at  $\sim 0.1\%$  level** (or better) ★

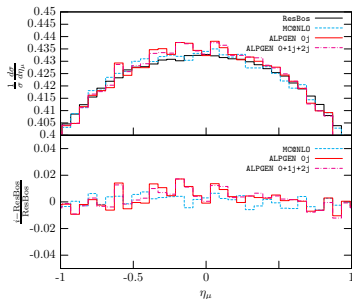
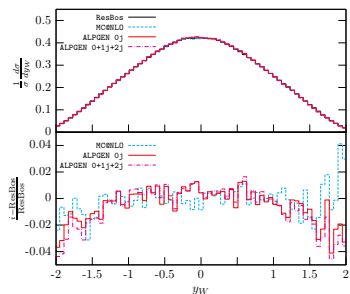


# QCD @ the Tevatron (I)

## Process and scheme – Detector modeling and lepton identification

- 1  $p\bar{p} \rightarrow W^\pm \rightarrow \mu^\pm \nu_\mu$   $\sqrt{s} = 1.96$  TeV –  $G_\mu$  scheme +  $\alpha(0)$  for real  $\gamma$  emission
- 2  $p_\perp^\mu > 25$  GeV  $\cancel{p}_\perp > 25$  GeV  $|\eta_\mu| < 1.2$   $p_\perp^W \leq 50$  GeV  $M_{\mu\nu} \in [50 - 200]$  GeV
- 3 NLO CTEQ6M with  $\mu_R = \mu_F = \sqrt{x_1 x_2 s}$

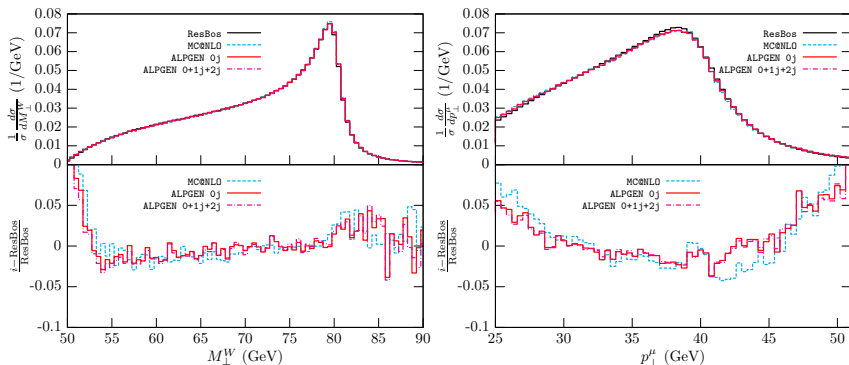
★ QCD generators are normalized to the corresponding integrated cross section, to point out the shape differences. Relative deviations w.r.t. ResBos ★



- For  $W$  rapidity and lepton pseudorapidity QCD generators agree at the  $\sim 1\%$  level

# QCD @ the Tevatron (II)

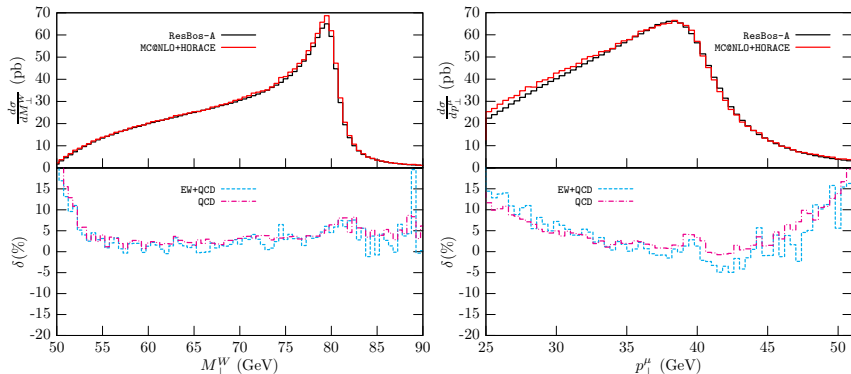
- ★ QCD generators are normalized to the corresponding integrated cross section, to point out the shape differences. Relative deviations w.r.t. ResBos ★



- For  $M_{\perp}^W$  and  $p_{\perp}^{\ell}$  QCD generators agree at a few % level around the jacobian peak
- In the soft  $M_{\perp}^W$  tail and in the  $p_{\perp}^{\ell}$  tails the QCD differences can reach the 5 ÷ 10 % level

# Electroweak $\otimes$ QCD @ the Tevatron

★ Absolute comparison: ResBos-A vs MC@NLO + HORACE<sub>HERWIG PS</sub>

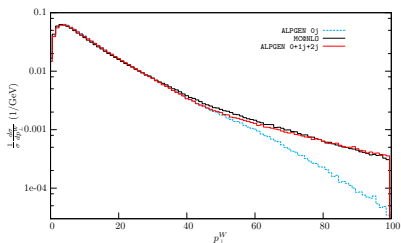
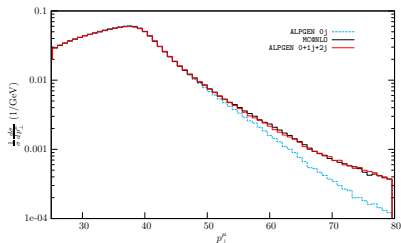


- For  $M_{\perp}^W$  and  $p_{\perp}^l$  the relative differences (including normalization) are at a few % level around the jacobian peak and can reach the  $\sim 10 \div 15$  % level in the tails
- These deviations are dominated by QCD effects

## Process and scheme – Detector modeling and lepton identification

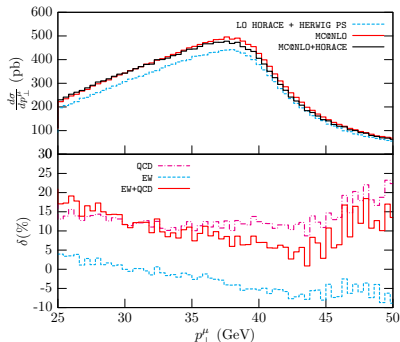
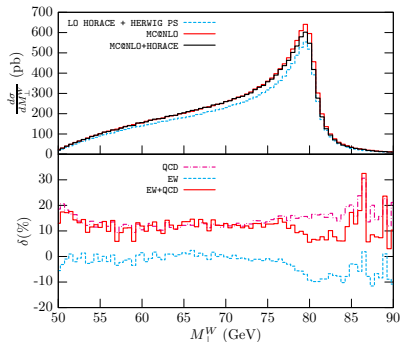
- 1  $pp \rightarrow W^\pm \rightarrow \mu^\pm \nu_\mu$   $\sqrt{s} = 14$  TeV –  $G_\mu$  scheme +  $\alpha(0)$  for real  $\gamma$  emission
- 2  $p_\perp^\mu > 25$  GeV  $p_\perp^\nu > 25$  GeV  $|\eta_\mu| < 2.5$   $\oplus$  (eventually)  $M_\perp^W > 1$  TeV
- 3 NLO MRST2004QED with  $\mu_R = \mu_F = \sqrt{p_{\perp,W}^2 + M_W^2}$

★ QCD generators are normalized to the corresponding integrated cross section, to point out the shape differences. ★



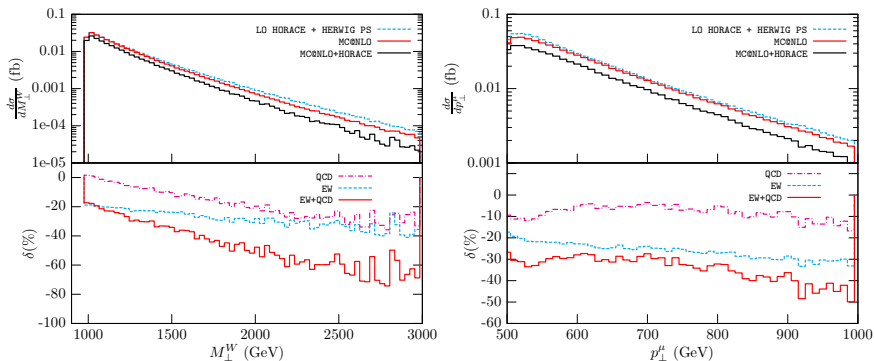
- NLO/Matched matrix elements corrections w.r.t. QCD Parton Shower are important in the high tails of  $p_\perp^l$  and  $p_\perp^W$
- There is a substantial agreement in the shapes predicted by MC@NLO and ALPGEN

# Electroweak $\otimes$ QCD @ the LHC



- Convolution with QCD Parton Shower modifies the relative size and shape of electroweak corrections
- For both  $M_{\perp}^W$  and  $p_{\perp}^l$  (NLO) QCD corrections are positive and **tend to compensate electroweak contributions**
- Around the jacobian peak their interplay is crucial for a precise  $M_W$  extraction and can't be accounted for by a QCD Parton Shower approach

- ★ To what extent large electroweak Sudakov logs compare with QCD corrections in the region relevant for the search of new physics at the LHC? ★



- For both  $M_{\perp}^W$  and  $p_{\perp}^l$  (NLO) QCD corrections are negative and sum up to negative electroweak Sudakov logs
- Their sum is  $\sim -40(-70)\%$  for  $M_{\perp}^W \simeq 1.5(3) \text{ TeV}$  and  $\sim -30(-50)\%$  for  $p_{\perp}^l \simeq 0.5(1) \text{ TeV}$   $\rightarrow$  need to include two-loop electroweak Sudakov logs
- ...But in this region there is a handful of events

# Conclusions

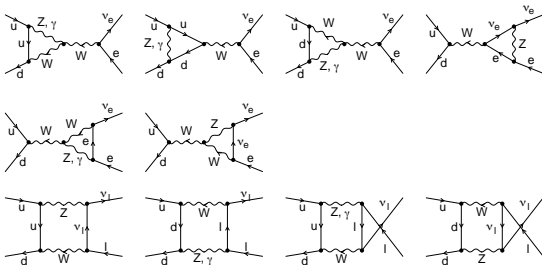
- Recent big theoretical effort towards high-precision predictions for Drell-Yan-like processes, including higher-order QCD and electroweak corrections, to keep under control theoretical systematics
  - All these calculations are essential ingredients for precision studies at the Tevatron RunII and LHC
  - It would be advisable to combine the state-of-the-art of electroweak and QCD corrections into a single, unified generator
  - Precision measurements with per cent accuracy at hadron colliders are very challenging!
  - Work in progress to
    - ★ complete the study of combining electroweak and QCD contributions to  $pp^{(-)} \rightarrow \text{lepton} + X$  (including FEWZ/MCFM and study of PDFs uncertainties)
    - ★ make HORACE available for electroweak corrections to  $Z$  production and compare with independent calculations
    - ★ scrutinize the electroweak and QCD systematics to the so-called “scaled observables method”
- W. Giele and S. Keller, Phys. Rev. **D57** (1998) 4433
- ★ Long term: combine HORACE with ALPGEN into a single EW  $\otimes$  QCD generator

# Backup slides

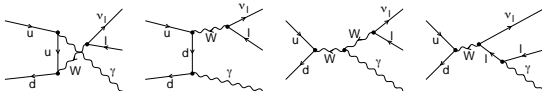


# Electroweak Feynman diagrams

- virtual one-loop corrections ( $\rightarrow$  **electroweak Sudakov logs**)



- bremsstrahlung corrections ( $\rightarrow$  **collinear singularities**)



# Matching NLO electroweak with QED Parton Shower

C.M. Carloni Calame *et al.*, JHEP 12 (2006) 016

- NLO ( $\mathcal{O}(\alpha)$ ) electroweak cross section

$$d\sigma_{\text{ew}}^{\alpha} \equiv d\sigma^{\alpha, \text{ex}} \equiv d\sigma_{\text{SV}}^{\alpha, \text{ex}} + d\sigma_{\text{H}}^{\alpha, \text{ex}}$$

- $\mathcal{O}(\alpha)$  Parton Shower (PS) cross section

$$d\sigma^{\alpha, \text{PS}} = [\Pi_S(Q^2)]_{\mathcal{O}(\alpha)} d\sigma_0 + \frac{\alpha}{2\pi} P_{ff}(x) I(k) dx dc d\hat{\sigma}_0 = \\ \equiv d\sigma_{\text{SV}}^{\alpha, \text{PS}} + d\sigma_{\text{H}}^{\alpha, \text{PS}}$$

- Resummed PS

$$d\sigma_{\text{PS}}^{\infty} = \Pi_S(Q^2) F_{\text{sv}} \sum_{n=0}^{\infty} d\hat{\sigma}_0 \frac{1}{n!} \prod_{i=0}^n \left[ \frac{\alpha}{2\pi} P_{ff}(x_i) I(k_i) dx_i dc_i F_{\text{H},i} \right]$$

where  $F_{\text{SV}} = 1 + \frac{d\sigma_{\text{SV}}^{\alpha, \text{ex}} - d\sigma_{\text{SV}}^{\alpha, \text{PS}}}{d\sigma_0}$  and  $F_{\text{H},i} = 1 + \frac{d\sigma_{\text{H},i}^{\alpha, \text{ex}} - d\sigma_{\text{H},i}^{\alpha, \text{PS}}}{d\sigma_{\text{H},i}^{\alpha, \text{PS}}}$

- $[\sigma_{\text{matched}}^{\infty}]_{\mathcal{O}(\alpha)} = \sigma_{\text{exact}}^{\alpha}$ , avoiding NLO double counting and preserving quark mass independence and exponentiation of QED leading logs

$W^+$ cross section (pb) at LHC	$\mathcal{O}(\alpha)$	matched
$m_q$	$4410.98 \pm 0.20$	$4412.14 \pm 0.26$
$m_q/10$	$4410.92 \pm 0.26$	$4411.89 \pm 0.33$
$m_q/100$	$4410.99 \pm 0.29$	$4411.92 \pm 0.50$

# Matching NLO electroweak with QED Parton Shower

C.M. Carloni Calame *et al.*, JHEP 12 (2006) 016

- NLO ( $\mathcal{O}(\alpha)$ ) electroweak cross section

$$d\sigma_{\text{ew}}^{\alpha} \equiv d\sigma^{\alpha, \text{ex}} \equiv d\sigma_{SV}^{\alpha, \text{ex}} + d\sigma_H^{\alpha, \text{ex}}$$

- $\mathcal{O}(\alpha)$  Parton Shower (PS) cross section

$$d\sigma^{\alpha, PS} = [\Pi_S(Q^2)]_{\mathcal{O}(\alpha)} d\sigma_0 + \frac{\alpha}{2\pi} P_{ff}(x) I(k) dx dc d\hat{\sigma}_0 = \\ \equiv d\sigma_{SV}^{\alpha, PS} + d\sigma_H^{\alpha, PS}$$

- Resummed PS + NLO electroweak

$$d\sigma_{\text{matched}}^{\infty} = \Pi_S(Q^2) F_{sv} \sum_{n=0}^{\infty} d\hat{\sigma}_0 \frac{1}{n!} \prod_{i=0}^n \left[ \frac{\alpha}{2\pi} P_{ff}(x_i) I(k_i) dx_i dc_i F_{H,i} \right]$$

$$\text{where } F_{SV} = 1 + \frac{d\sigma_{SV}^{\alpha, \text{ex}} - d\sigma_{SV}^{\alpha, PS}}{d\sigma_0} \text{ and } F_{H,i} = 1 + \frac{d\sigma_{H,i}^{\alpha, \text{ex}} - d\sigma_{H,i}^{\alpha, PS}}{d\sigma_{H,i}^{\alpha, PS}}$$

- $[\sigma_{\text{matched}}^{\infty}]_{\mathcal{O}(\alpha)} = \sigma_{\text{exact}}^{\alpha}$ , avoiding NLO double counting and preserving quark mass independence and exponentiation of QED leading logs

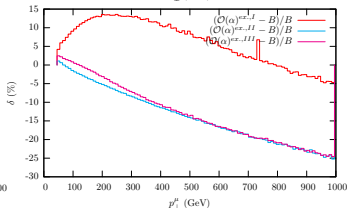
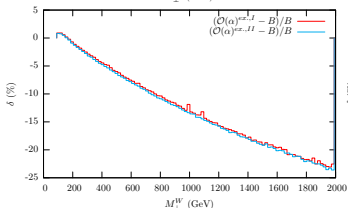
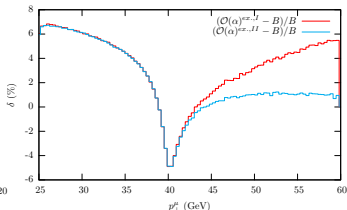
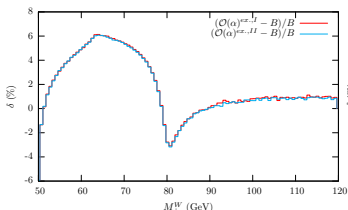
$W^+$ cross section (pb) at LHC	$\mathcal{O}(\alpha)$	matched
$m_q$	$4410.98 \pm 0.20$	$4412.14 \pm 0.26$
$m_q/10$	$4410.92 \pm 0.26$	$4411.89 \pm 0.33$
$m_q/100$	$4410.99 \pm 0.29$	$4411.92 \pm 0.50$

# $\gamma$ -induced processes vs NLO electroweak (LHC)

## ★ Legenda

$pp \rightarrow W^\pm \rightarrow \mu^\pm \nu (+\gamma)$  with MRTS2004QED -  $\alpha(0)$ ,  $M_W$ ,  $M_Z$  scheme

- I. with  $\gamma$  induced processes, without jet cut
- II. without  $\gamma$  induced processes (pure NLO electroweak)
- III. with  $\gamma$  induced processes, with jet cut ( $p_\perp^{\text{jet}} < 30$  GeV and  $|\eta^{\text{jet}}| > 2.5$ )



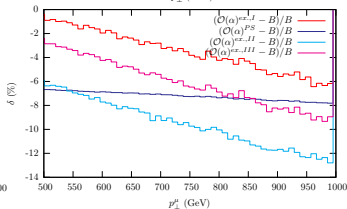
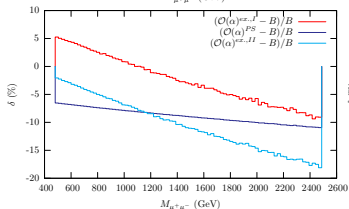
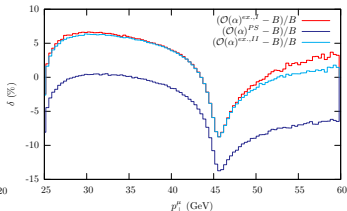
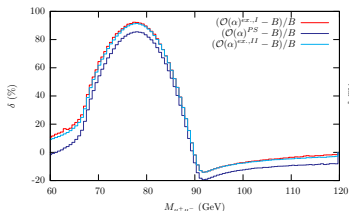
- $\gamma$  induced processes are very small for  $M_\perp^W$  and important (at some % level) for  $p_\perp^\ell$  at the LHC (everywhere negligible at the Tevatron)
- $\gamma$  induced processes are strongly suppressed by jet cuts and overwhelmed by QCD effects at high  $p_\perp^\ell$

# NLO electroweak corrections to $Z$ observables (LHC)

## ★ Legenda

$pp \rightarrow \gamma/Z \rightarrow \mu^+ \mu^- (+\gamma)$  with MRTS2004QED -  $\alpha(0)$ ,  $M_W$ ,  $M_Z$  scheme

- I. with  $\gamma$  induced processes, without jet cut
- II. without  $\gamma$  induced processes (pure NLO electroweak)
- III. with  $\gamma$  induced processes, with jet cut ( $p_{\perp}^{\text{jet}} < 30$  GeV and  $|\eta^{\text{jet}}| > 2.5$ )
- IV. QED Parton Shower approximation



- non-negligible  $\gamma$  induced effects both for  $M_{l+l-}$  and  $p_{\perp}^{\ell}$  in the hard tails
- large corrections due to Sudakov logs not accounted for by QED PS

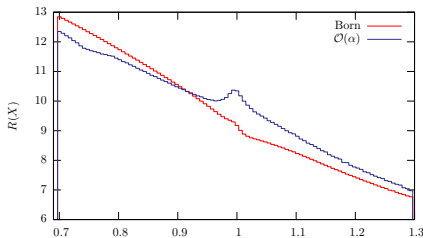
- the ratio  $\frac{d\sigma}{dM_{\perp}^W} / \frac{d\sigma}{dM_{\perp}^Z}$  can be used to measure  $M_W$ , being slightly sensitive to pQCD corrections

W. Giele and S. Keller, Phys. Rev. **D57** (1998) 4433

- defining  $X_V \equiv \frac{M_{\perp}^V}{M_V}$ :

$$\left. \frac{d\sigma}{dM_{\perp}^W} \right|_{\text{predicted}} = \frac{M_Z}{M_W} \times R \times \left. \frac{d\sigma}{dM_{\perp}^Z} \right|_{\text{measured}}$$

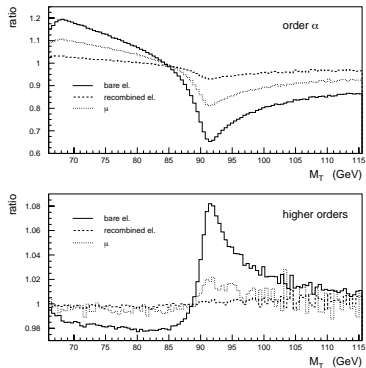
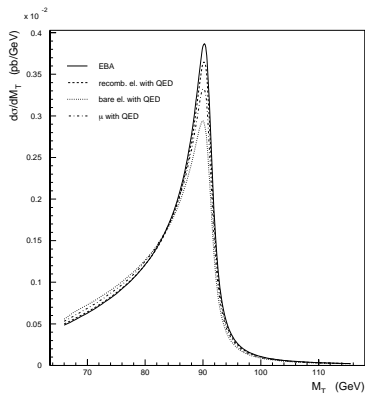
where  $R \equiv \frac{d\sigma}{dX_W} / \frac{d\sigma}{dX_Z}$ , the predicted  $M_{\perp}^W$  distribution can be used to extract  $M_W$  ...



★  $\mathcal{O}(\alpha)$  EW corrections do not cancel! ★

# Higher-order QED corrections to $Z$ production: $M_T^Z$

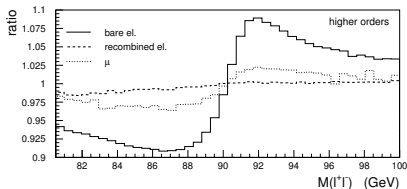
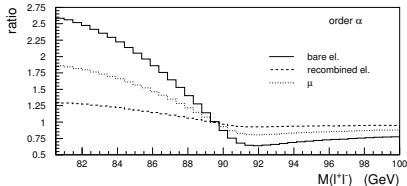
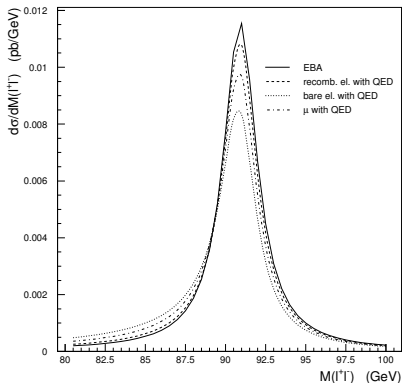
C.M. Carloni Calame *et al.* JHEP **05** (2005) 019



- Multiple photon corrections to  $Z$  transverse mass are  $\sim 2\%$  for bare muons and a few mille level for calorimetric electrons.

# Higher-order QED corrections to $Z$ production: $M_{\ell\ell}$

C.M. Carloni Calame *et al.* JHEP **05** (2005) 019

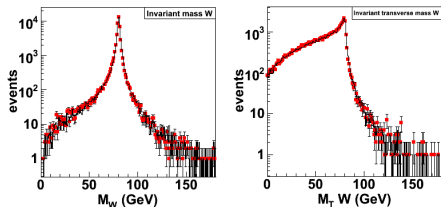


- Multiple photon corrections to  $Z$  production are also needed, because important  $W$  systematics are strongly related to  $Z$  parameters extraction and statistics

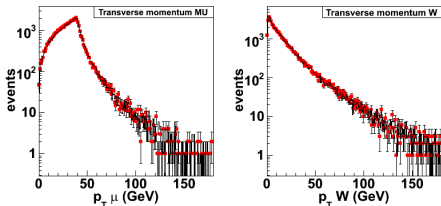


# HORACE & QCD showering MCs

- HORACE is “Les Houches Accord” compliant. Its events can be passed through QCD Parton Shower & hadronization MCs
- e.g. HORACE (with QED PS) +PYTHIA vs. PYTHIA+PHOTOS



courtesy of M. Bellomo and  
G. Polesello (ATLAS)

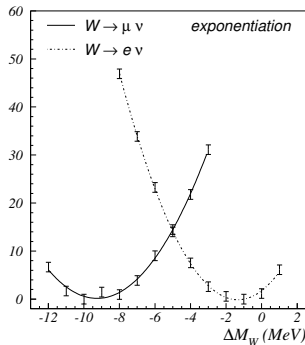
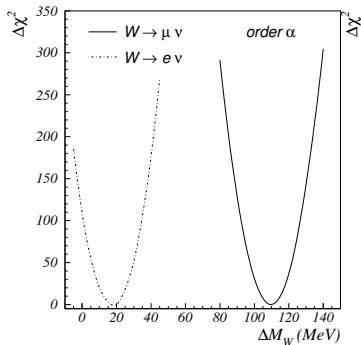


● HORACE+PYTHIA  
— PYTHIA+PHOTOS

# Why higher-order QED is important: $W$ mass

C.M. Carloni Calame *et al.*, Phys. Rev. **D69** (2004) 037301

Including recombination and smearing



$$\Delta M_W^{\alpha,e} \sim 20 \text{ MeV}$$
$$\Delta M_W^{\alpha,\mu} \sim 110 \text{ MeV}$$

$$\Delta M_W^{\infty,e} \sim 2 \text{ MeV}$$
$$\Delta M_W^{\infty,\mu} \sim 10 \text{ MeV}$$

- $W$ -mass shift due to multiphoton radiation is about **10%** of that caused by one photon emission  $\longrightarrow$  **non-negligible for  $W$  mass!**

<b>Tevatron, <math>p\bar{p} \rightarrow W^+ \rightarrow e^+\nu_e</math></b> <span style="float: right;">Courtesy of D. Wackeroth</span>						
	bare cuts			calo cuts		
	LO [pb]	NLO [pb]	$\Delta$ [%]	LO [pb]	NLO [pb]	$\Delta$ [%]
HORACE	773.509(5)	791.14(2)	2.279(3)	733.012(5)	762.21(3)	3.983(4)
SANC	773.510(2)	791.04(8)	2.27(1)	733.024(2)	762.03(9)	3.96(1)
WGRAD2	773.516(5)	791.01(5)	2.268(7)	733.004(6)	762.00(5)	3.956(6)
<b>Tevatron, <math>p\bar{p} \rightarrow W^+ \rightarrow \mu^+\nu_\mu</math></b>						
	bare cuts			calo cuts		
	LO [pb]	NLO [pb]	$\Delta$ [%]	LO [pb]	NLO [pb]	$\Delta$ [%]
HORACE	773.509(5)	804.18(2)	3.965(3)	732.913(6)	738.16(3)	0.716(4)
SANC	773.510(2)	804.07(6)	3.951(7)	732.908(2)	738.01(5)	0.696(7)
WGRAD2	773.516(5)	804.11(1)	3.955(2)	732.917(6)	738.00(1)	0.693(2)
<b>LHC, <math>pp \rightarrow W^+ \rightarrow e^+\nu_e</math></b>						
	bare cuts			calo cuts		
	LO [pb]	NLO [pb]	$\Delta$ [%]	LO [pb]	NLO [pb]	$\Delta$ [%]
HORACE	5039.11(4)	5140.6(1)	2.014(2)	4924.17(4)	5115.5(2)	3.886(4)
SANC	5039.21(1)	5139.5(5)	1.99(1)	4925.31(1)	5113.5(4)	3.821(9)
WGRAD2	5039.16(7)	5139.6(6)	1.99(1)	4924.15(5)	5114.1(6)	3.86(1)
<b>LHC, <math>pp \rightarrow W^+ \rightarrow \mu^+\nu_\mu</math></b>						
	bare cuts			calo cuts		
	LO [pb]	NLO [pb]	$\Delta$ [%]	LO [pb]	NLO [pb]	$\Delta$ [%]
HORACE	5039.11(4)	5230.5(2)	3.798(4)	4925.16(5)	4944.5(2)	0.393(4)
SANC	5039.21(1)	5229.4(3)	3.775(7)	4925.31(1)	4942.5(5)	0.349(9)
WGRAD2	5039.16(7)	5229.9(1)	3.786(3)	4925.30(7)	4943.0(1)	0.360(3)

Tevatron and LHC	
electrons	muons
combine $e$ and $\gamma$ momentum four vectors, if $\Delta R(e, \gamma) < 0.1$	reject events with $E_\gamma > 2 \text{ GeV}$ for $\Delta R(\mu, \gamma) < 0.1$
reject events with $E_\gamma > 0.1 E_e$ for $0.1 < \Delta R(e, \gamma) < 0.4$	reject events with $E_\gamma > 0.1 E_\mu$ for $0.1 < \Delta R(\mu, \gamma) < 0.4$

**Table:** Summary of lepton identification requirements.

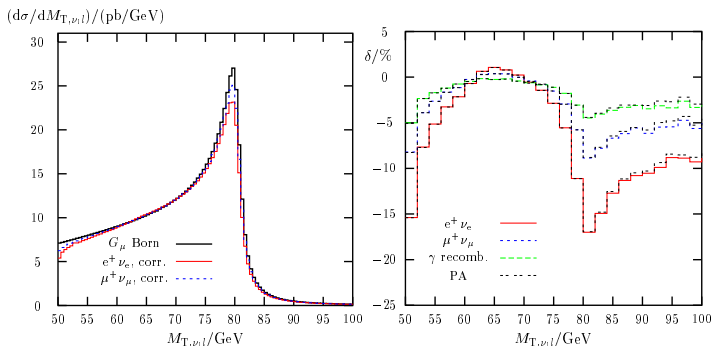
where

$$\Delta R(e, \gamma) = \sqrt{(\Delta\eta(e, \gamma))^2 + (\Delta\phi(e, \gamma))^2},$$

- ★ Uncertainties in the energy measurements of the charged leptons in the detector are simulated by Gaussian smearing of the particle four-momentum vector with standard deviation  $\sigma$  based on the DØ(upgrade) and ATLAS specifications.

# Photon radiation and lepton identification

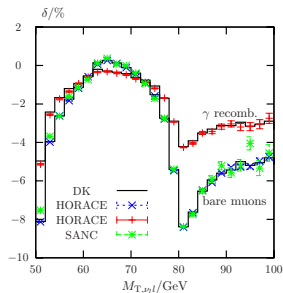
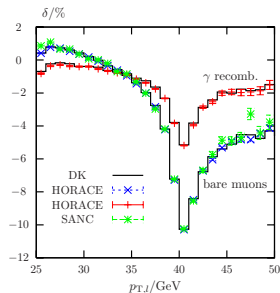
S. Dittmaier and M. Krämer, Phys. Rev. **D65** (2002) 073007



- Lepton identification requirements (and detector effects) strongly affect final-state photon radiation (“the KLN theorem at work”)
- Pole approximation agrees with the full calculation within a few 0.1% around the  $W$  resonance

## Process and scheme – Detector modeling and lepton identification

- 1  $pp \rightarrow W^+ \rightarrow \ell^+ \nu_\ell (+\gamma)$  –  $G_\mu$  scheme +  $\alpha(0)$  for real  $\gamma$  emission
- 2  $\sqrt{s} = 14$  TeV  $p_{T,\ell} > 25$  GeV  $\cancel{p}_T > 25$  GeV  $|\eta_\ell| < 1.2$
- 3  $R_{l\gamma} = \sqrt{(\eta_l - \eta_\gamma)^2 + \phi_{l\gamma}^2} \leq 0.1 \Rightarrow$  electron/photon recombination



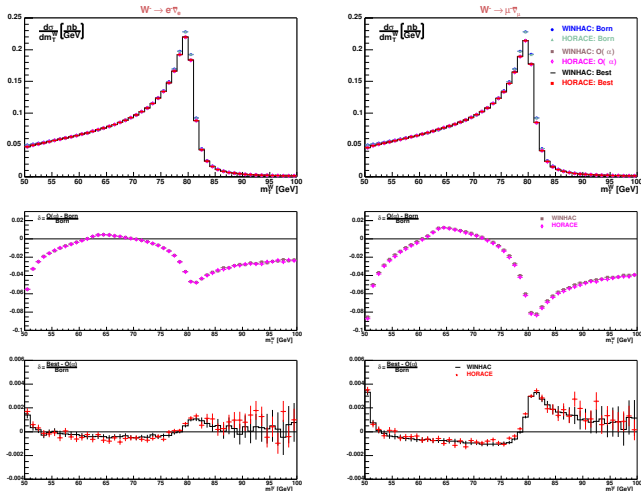
- Perfect agreement between independent calculations!

$$pp \rightarrow \nu_l l^+ (+\gamma) @ \sqrt{s} = 14 \text{ TeV (with MRSTQED04)}$$

$p_{T,l}/\text{GeV}$	25- $\infty$	50- $\infty$	100- $\infty$	200- $\infty$	500- $\infty$	1000- $\infty$
$\sigma_0/\text{pb}$						
DK	2112.2(1)	13.152(2)	0.9452(1)	0.11511(2)	0.0054816(3)	0.00026212(1)
HORACE	2112.21(4)	13.151(6)	0.9451(1)	0.11511(1)	0.0054812(4)	0.00026211(2)
SANC	2112.22(2)	13.1507(2)	0.94506(1)	0.115106(1)	0.00548132(6)	0.000262108(3)
WGRAD	2112.3(1)	13.149(1)	0.94510(5)	0.115097(5)	0.0054818(2)	0.00026209(2)
$\delta_{e+\nu_e}/\%$						
DK	-5.19(1)	-8.92(3)	-11.47(2)	-16.01(2)	-26.35(1)	-37.92(1)
HORACE	-5.23(1)	-8.98(1)	-11.49(1)	-16.03(1)	-26.36(1)	-37.92(2)
WGRAD	-5.10(1)	-8.55(5)	-11.32(1)	-15.91(2)	-26.1(1)	-38.2(2)
$\delta_{\mu+\nu_\mu}/\%$						
DK	-2.75(1)	-4.78(3)	-8.19(2)	-12.71(2)	-22.64(1)	-33.54(2)
HORACE	-2.79(1)	-4.84(1)	-8.21(1)	-12.73(1)	-22.65(1)	-33.57(1)
SANC	-2.80(1)	-4.82(2)	-8.17(2)	-12.67(2)	-22.63(2)	-33.50(2)
WGRAD	-2.69(1)	-4.53(1)	-8.12(1)	-12.68(1)	-22.62(2)	-33.6(2)
$\delta_{\text{recomb}}/\%$						
DK	-1.73(1)	-2.45(3)	-5.91(2)	-9.99(2)	-18.95(1)	-28.60(1)
HORACE	-1.77(1)	-2.51(1)	-5.94(1)	-10.02(1)	-18.96(1)	-28.65(1)
SANC	-1.89(1)	-2.56(1)	-5.97(1)	-10.02(1)	-18.96(1)	-28.61(1)
WGRAD	-1.71(1)	-2.32(1)	-5.94(1)	-10.11(2)	-19.08(3)	-28.73(6)
$\delta_{\gamma q}/\%$						
DK	+0.071(1)	+5.24(1)	+13.10(1)	+16.44(2)	+14.30(1)	+11.89(1)

# HORACE vs WINHAC: $M_{\perp}^W$

C.M. Carloni Calame *et al.*, Acta Phys. Pol. **B35** (2004) 1643

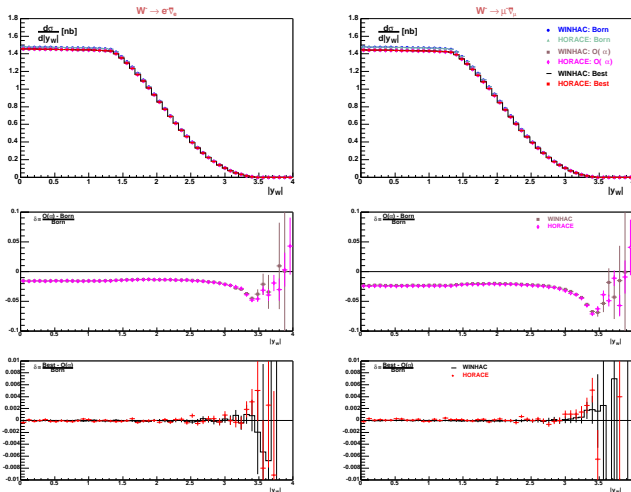


• Same effect of multiple photon radiation  $\sim 0.2 - 0.5\%$  around  $W$  peak



# HORACE vs WINHAC: $W$ rapidity

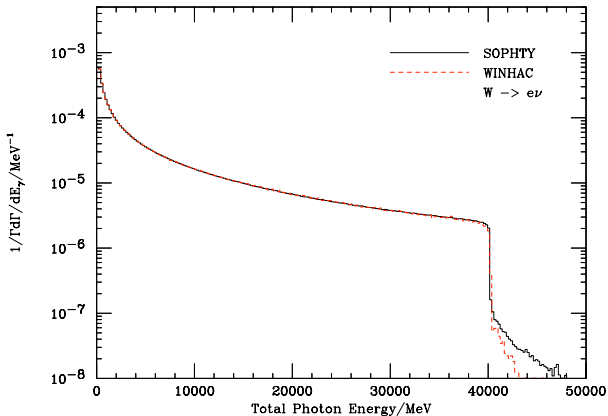
C.M. Carloni Calame *et al.*, Acta Phys. Pol. **B35** (2004) 1643



- $\mathcal{O}(\alpha)$  corrections at **2/5%** level for recombined  $e/\text{bare } \mu$

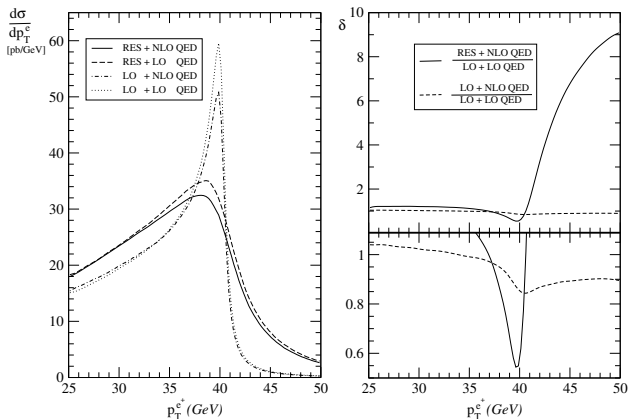
# HERWIG+SOPHTY vs WINHAC

K. Hamilton and P. Richardson, JHEP **0607** (2006) 010



# Matching soft-gluon resummation with NLO QED

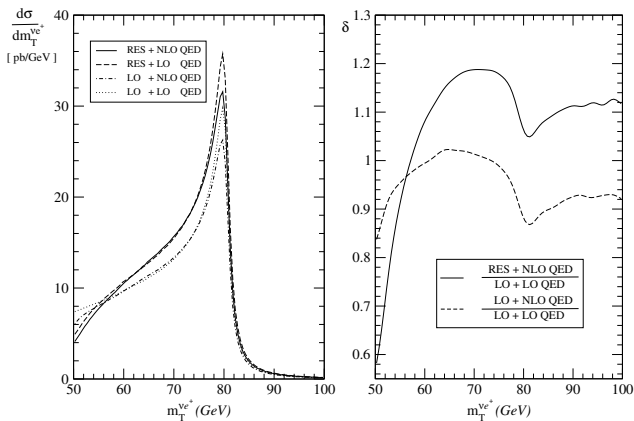
Q.-H. Cao and C.-P. Yuan, Phys. Rev. Lett. **93** (2004) 042001  
ResBos-A



- QCD resummation and NLO QED differently modify the shape of  $p_T^\ell$  and reach  $\sim -45\%$   $\rightarrow$  need to merge QCD and EW generators!

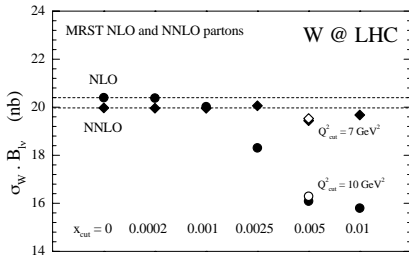
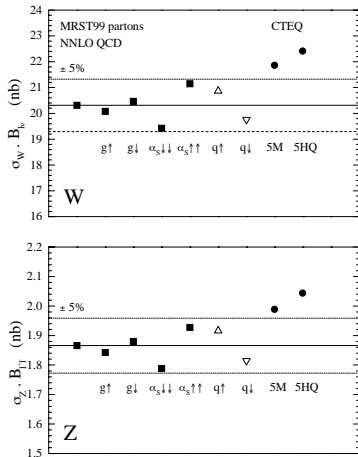
# Matching soft-gluon resummation with NLO QED: $M_T^W$

Q.-H. Cao and C.-P. Yuan, Phys. Rev. Lett. **93** (2004) 042001



- QCD resummation ( $\sim +6\%$  at the peak) is compensated by NLO QED ( $\sim -12\%$ )  $\rightarrow$  **need to merge QCD and EW generators!!**

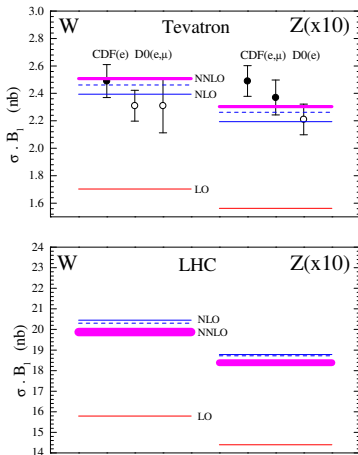
W and Z Cross Sections: LHC



- Present PDFs uncertainty  $\sim 3\% - 5\%$  at the LHC

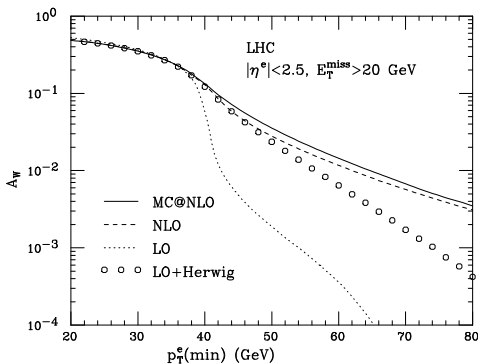
# QCD predictions for $W/Z$ total rates

R. Hamberg, W.L. van Neerven, T. Matsuura, Nucl. Phys. **B359** (1991) 343  
A.D. Martin *et al.*, Eur. Phys. J. **C19** (2001) 313

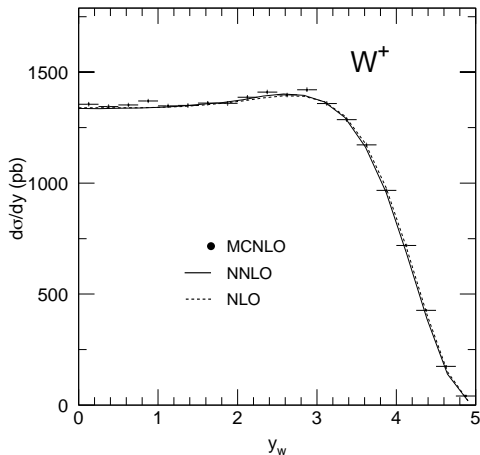


- Good convergence of  $\alpha_s$  expansion. NLO-NNLO difference  $\sim 2\%$  at the LHC

$$\sigma^{\text{exp}}(W) = \frac{1}{\text{BR}(W \rightarrow l\nu)} \frac{1}{\int \mathcal{L} dt} \frac{N^{\text{obs}}}{A_W}$$



- Overall QCD uncertainty (NLO + Parton Shower corrections, spin correlations, PDFs and scale uncertainties) at  $\sim 2\%$  level



- For an inclusive sample NNLO and MC@NLO agree well!



# QED initial-state collinear singularities

- QED initial-state collinear singularities are universal  $\rightarrow$  can be absorbed into PDFs, as in QCD



$$f(x) \rightarrow f(x, \mu_F^2) - \int_x^1 \frac{dz}{z} f\left(\frac{x}{z}, \mu_F^2\right) \frac{\alpha}{2\pi} Q_q^2 \times \left\{ \ln\left(\frac{\mu_F^2}{m_q^2}\right) [P_{ff}(z)]_+ - [P_{ff}(z) (2 \ln(1-z) + 1)]_+ + C(z) \right\}$$

$$C(z) = \left\{ \begin{array}{l} 0 \\ [P_{ff}(z) (\ln(\frac{1-z}{z}) - \frac{3}{4}) + \frac{9+5z}{4}]_+ \end{array} \right. \overline{\text{MS}} \text{ DIS}$$

# The Parton Shower algorithm

- the PS is a MC solution of the QED DGLAP equation

$$Q^2 \frac{\partial}{\partial Q^2} D(x, Q^2) = \frac{\alpha}{2\pi} \int_x^1 \frac{dt}{t} P_+(t) D\left(\frac{x}{t}, Q^2\right)$$

- the solution can be cast in the form

$$D(x, Q^2) = \Pi_S(Q^2) \sum_{n=0}^{\infty} \int \frac{\delta(x-x_1 \cdots x_n)}{n!} \prod_{i=0}^n \left[ \frac{\alpha}{2\pi} P(x_i) L dx_i \right]$$

- ★  $\Pi_S(Q^2) \equiv e^{-\frac{\alpha}{2\pi} LI_+}$  is the Sudakov form factor,  
 $I_+ \equiv \int_0^{1-\epsilon} P(x) dx$ ,  $L \equiv \log \frac{Q^2}{m^2}$  and  $\epsilon$  soft/hard separator

- the PS MC algorithm reproduces this solution
- at NLO, the resulting cross section has a **leading log accuracy**

# Fitting the $W$ mass

$\chi^2$  fits to Monte Carlo pseudo-data for the  $M_T^W$  spectrum with

- $\sqrt{s} = 2 \text{ TeV}$   $p_T(\ell) > 25 \text{ GeV}$   $|\eta(\ell)| < 1.2$   $\cancel{p}_T > 25 \text{ GeV}$
- lepton identification requirements based on Tevatron analyses (e.g., if  $\Delta R_{e\gamma} = \sqrt{\Delta\eta^2 + \Delta\phi^2} < 0.2$ ,  $e$  and  $\gamma$  momenta are recombined)
- particles' momenta are smeared according to RunII DØ detector specifications

$$\chi^2(M_W) = \sum_{i=\text{bins}} (\sigma_{i,\text{exp}} - \sigma_{i,\alpha})^2 / (\Delta\sigma_{i,\text{exp}}^2 + \Delta\sigma_{i,\alpha}^2)$$

histogram: no lepton identification criteria, no detector effects

markers: with lepton identification criteria

shaded: with lepton identification criteria and detector effects

arrows: fitting region,  $65 \text{ GeV} < M_T < 100 \text{ GeV}$

