

# O'Mega & WHIZARD: Monte Carlo Event Generator Generation For Future Colliders

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- - High Energy Precision Physics
     Computer Aided Calculations

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  - the phase space also becomes much more intricate



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- some essential parts will need a lot more work
  - loops for many particles
  - :: complete one-loop calculations for  $2 \rightarrow 4$  are the limit of our capabilities



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$$F(n) = (2n-5)!! = (2n-5) \cdot (2n-7) \cdot \ldots \cdot 3 \cdot 1$$

n	
4	
5	
6	
7	
8	
9	
10	
11	
12	



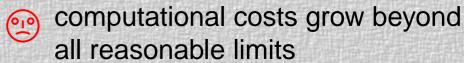
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n	F(n)	
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- : Feynman diagrams extremely redundant for many particles in the final state!
- terms much too large to expect any help from common subexpression elimination by optimizing compilers that don't understand any physics!





$$ab(ab+c) = \begin{pmatrix} & & & \\ & & & \\ a & & b \end{pmatrix} \begin{pmatrix} & & \\$$



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One particle off-shell wave functions (1POWs) are obtained from Greensfunctions by applying the LSZ reduction formula to all but one line:

$$W(\mathbf{x}; \mathbf{p}_1, \dots, \mathbf{p}_n; \mathbf{q}_1, \dots, \mathbf{q}_m) = \langle \phi(\mathbf{q}_1), \dots, \phi(\mathbf{q}_m); \mathsf{out} | \Phi(\mathbf{x}) | \phi(\mathbf{p}_1), \dots, \phi(\mathbf{p}_n); \mathsf{in} \rangle .$$



Directed Acyclical Graphs (DAGs) are a more efficient representation for arithmetical expressions than the equivalent trees. E. g.:

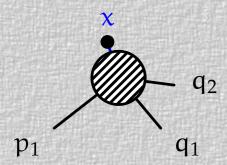
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E. g.  $\langle \phi(q_1), \phi(q_2); \text{out} | \Phi(x) | \phi(p_1); \text{in} \rangle$  in unflavored scalar  $\phi^3$ -theory at tree level





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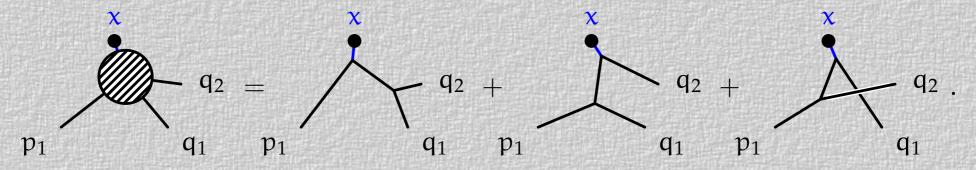
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- Theorem: all tree level scattering amplitudes can be represented by combinations of 1POWs (correct combinations are termed keystones)
- **Grow:** starting from the external particles, build the tower of all 1POWs up to a given height (the height is always less than the number of external lines) and translate it to the equivalent DAG D.
- **Select:** from D, determine all possible flavored keystones for the process under consideration and the 1POWs appearing in them.
- **Harvest:** construct a sub-DAG  $D^* \subseteq D$  consisting only of nodes that contribute to the 1POWs appearing in the flavored keystones.
- Calculate: multiply the 1POWs as specified by the keystones and sum the keystones.
- the resulting DAG contains no more redundancies
- the symbolic algorithm contains the numerical methods of Alpha (Caravaglios/Moretti) and HELAC (Kanaki/Papadopoulos) as special cases.



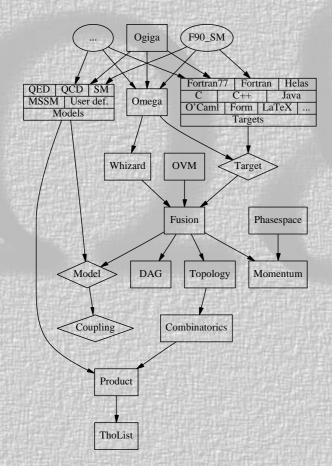
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Matrix element compiler O'Mega implemented in Objective Caml (INRIA, France).

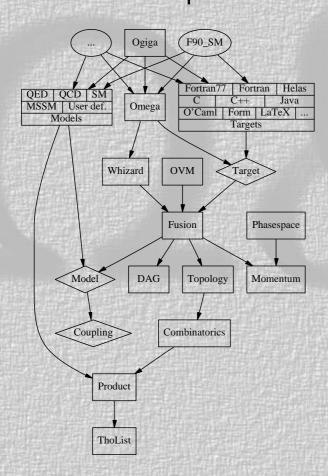




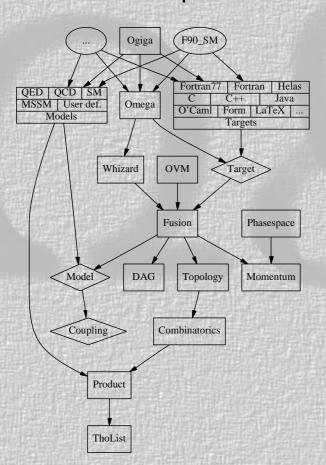




The module Targets contains implementations of the signature Target for each target language

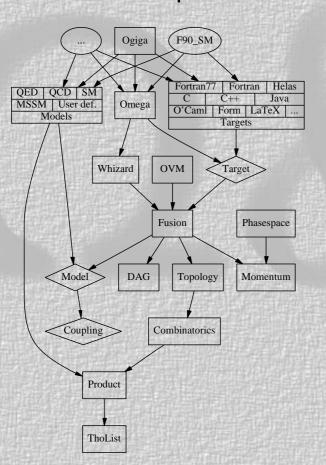






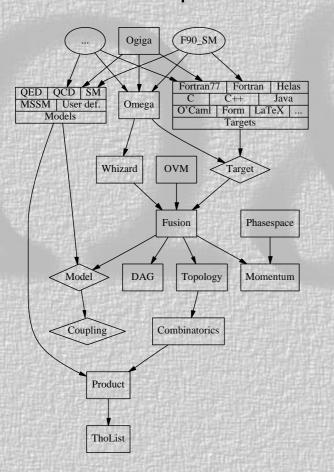
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 any volunteers for Java and C++ targets?

# First Results

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process	Diag	grams	
$e^+e^- \rightarrow$	#		
e <sup>+</sup> v̄ <sub>e</sub> dū			
e <sup>+</sup> ν̄ <sub>e</sub> dūγ			
$e^+ \bar{\nu}_e d\bar{u} \gamma \gamma$			
$e^+ \bar{\nu}_e d\bar{u} \gamma \gamma \gamma$			
$e^+\bar{\nu}_e d\bar{u}\gamma\gamma\gamma\gamma$			



process	Diag	grams	
$e^+e^- \rightarrow$	#		
$e^+\bar{\nu}_e d\bar{u}$	20		
$e^+\bar{\nu}_e d\bar{u}\gamma$	146		
$e^+\bar{\nu}_e d\bar{u}\gamma\gamma$	1112		
$e^+\bar{\nu}_e d\bar{u}\gamma\gamma\gamma$	12420		
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process	Diagrams	O'Mega
$e^+e^- \rightarrow$	#	#prop.
$e^+\bar{\nu}_e d\bar{u}$	20	14
$e^+ \bar{\nu}_e d\bar{u}\gamma$	146	36
$e^+\bar{\nu}_e d\bar{u}\gamma\gamma$	1112	94
$e^+\bar{\nu}_e d\bar{u}\gamma\gamma\gamma$	12420	168
$e^+ \bar{\nu}_e d\bar{u} \gamma \gamma \gamma \gamma$	138816	344



process	Diagrams		O'Mega	
$e^+e^- \rightarrow$	#	vertices	#prop.	vertices
$e^+\bar{\nu}_e d\bar{u}$	20	80	14	44
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## First realistic application

 simulation of six fermion final states in W<sup>+</sup>W<sup>-</sup> scattering for the TESLA
 Technical Design Report, using WHIZARD by Wolfgang Kilian as unweighted
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• QCD

Th. Ohl

O'Mega & WHIZARD

LCWS2000



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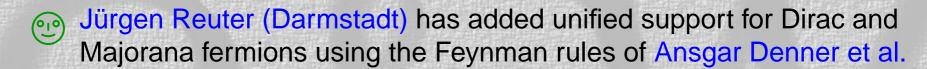
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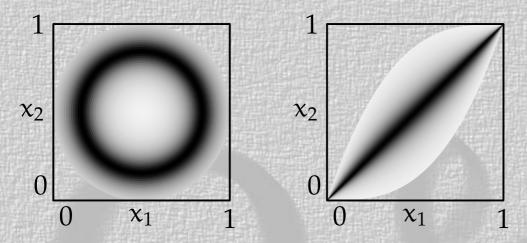
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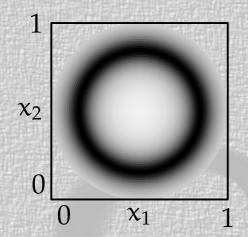
	WHIZARD	11
1	Mission	2
2	O'Mega	5
3	WHIZARD	
	VAMP	12
	Phase Space	13
	Component Architecture	14
	Example: $e^-e^+ \rightarrow \nu_e \bar{\nu}_e b\bar{b}$	16
4	Further On Up The Road	20

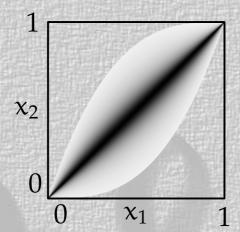




separately after appropriate mapping.



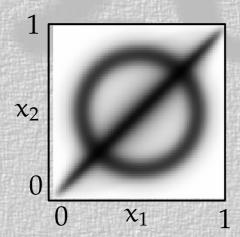




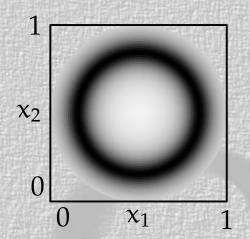
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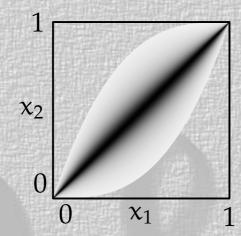
(%)

fails for overlapping singularities







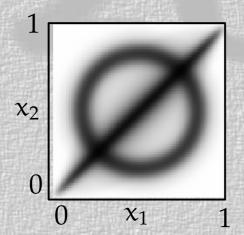


which is the common case (if more than one diagram contributes)

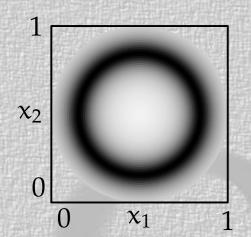
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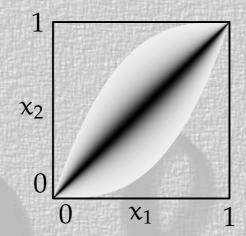


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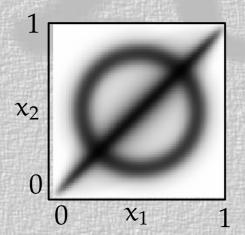






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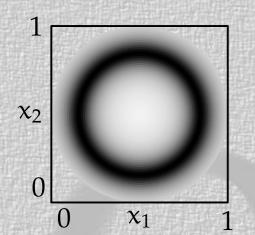
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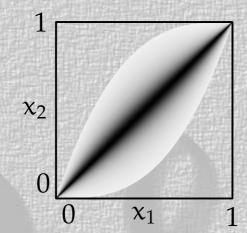
: adaptive multichannel approach

$$I(f) = \int_{M} d\mu(p) f(p)$$

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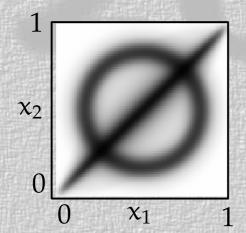






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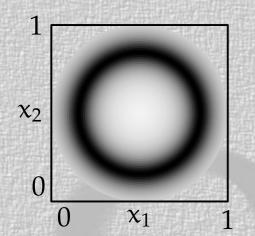
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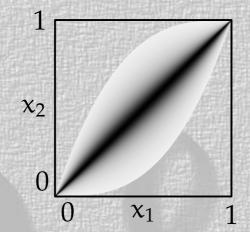
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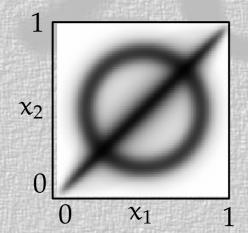






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works with factorized  $g_i$  adapted by VEGAS and  $\alpha_i$  adapted by variance reduction.



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WHIZARD phase space & steering



cuts

parameters



cuts

parameters

σ

histograms

unweighted events



cuts

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σ

histograms

unweighted events

hadronization & detector



cuts

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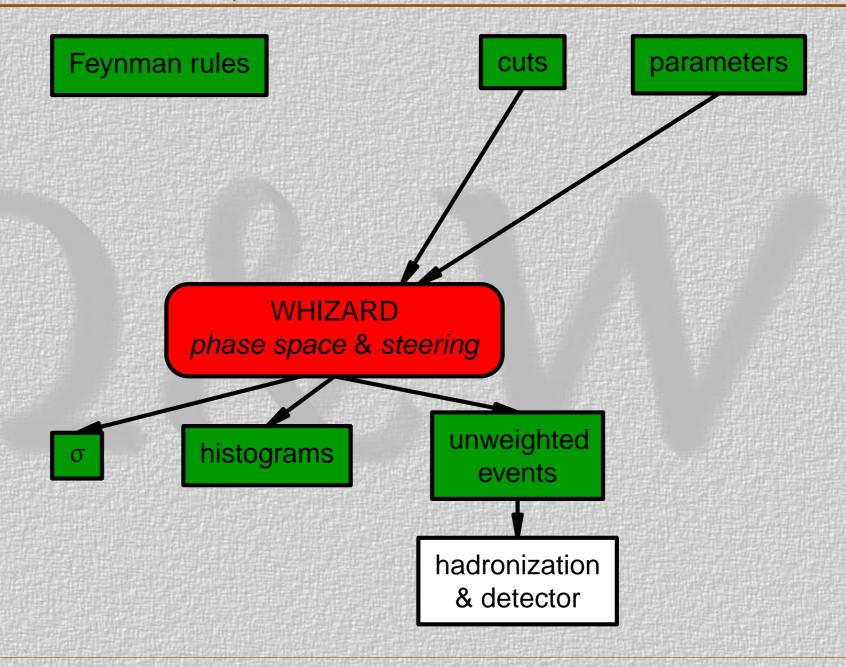
σ

histograms

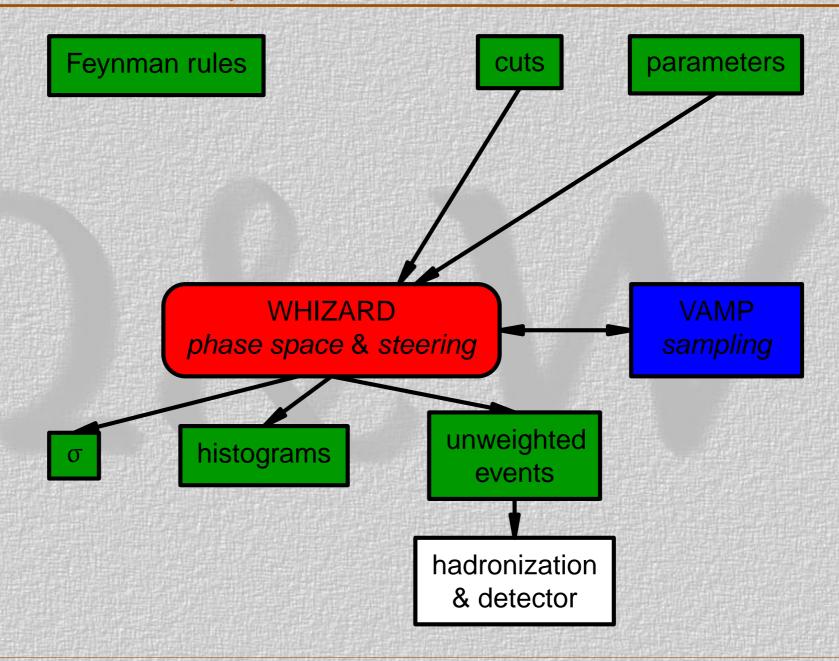
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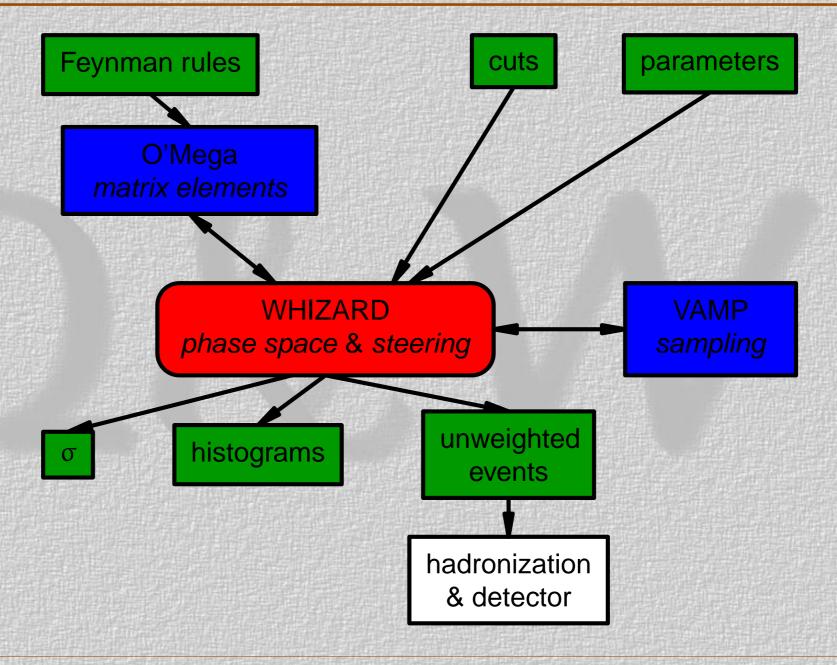




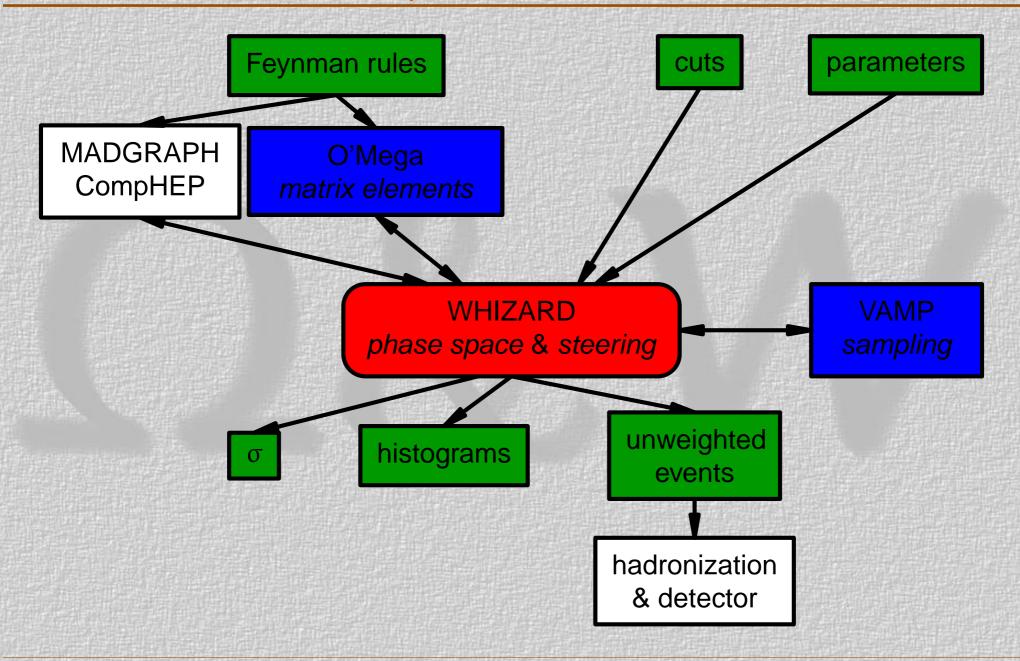
















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## Usage:

#### **Process file:**

ID	In	Out	Method
zh	e1,E1	Z,H	chep
ZWW	e1,E1	Z,W+,W-	chep
nnbb	e1,E1	n1,N1,b,B	mad
nnucsd	e1,E1	n1,N1,u,C,s,D	omega



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Compile: Makefile performs all necessary steps



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- ... Err/Exp too large



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```
Calls
             Integral[fb] Error[fb] Err[%] Err/Exp Eff[%]
! It
                                                          Chi2
! Adapting (var. weights): Generating 8 samples of 10000 events ...
        10000
              5.5642224E+01
                           1.23E+00
                                       2.21
                                              2.21* 7.58
  3
                           1.06E+00 1.80 1.80* 7.51
  4
        10000 5.9028368E+01
                           8.34E-01
                                     1.42 1.42* 9.82
        10000
             5.8586436E+01
                                      1.17 1.17* 12.18
  6
        10000
             5.8997829E+01
                           6.89E-01
        10000 5.8626448E+01 1.04E+00 1.78 1.78 10.78
                           5.12E-01 0.89
        10000 5.7737567E+01
                                              0.89* 17.50
                                              0.82* 19.50
        10000 5.7693393E+01
                           4.75E-01
                                      0.82
                            5.42E-01 0.93
                                              0.93 14.60
 10
        10000 5.8216141E+01
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(P)

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                                             0.82* 19.50
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                                             0.93 14.60
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- significantly larger efficiency and very good Err/Exp
  - Finally generate some events

```
! Integrating (fixed w.): Generating 2 samples of 10000 events ... 12 20000 5.8910540E+01 4.25E-01 0.72 1.02 11.64 0.05
```



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       Calls
                                                        Chi2
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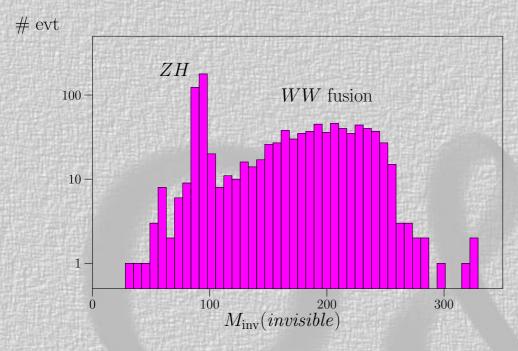
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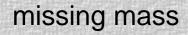
15 min for adaptation, 10 min for 10,000 unweighted events on a Pentium II 233 MHz.

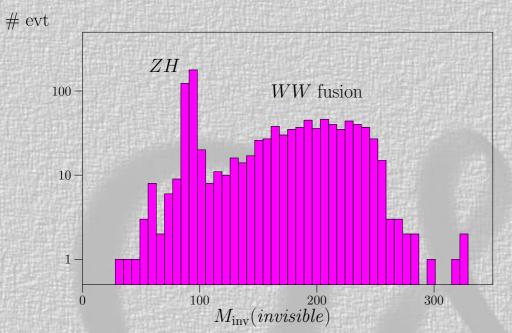


## missing mass

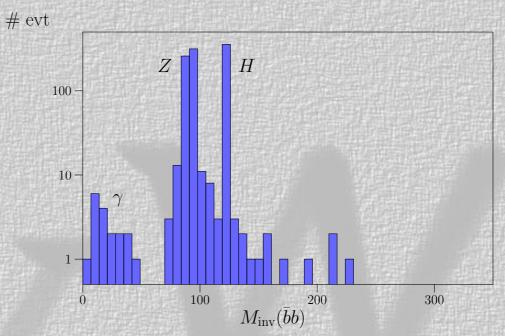




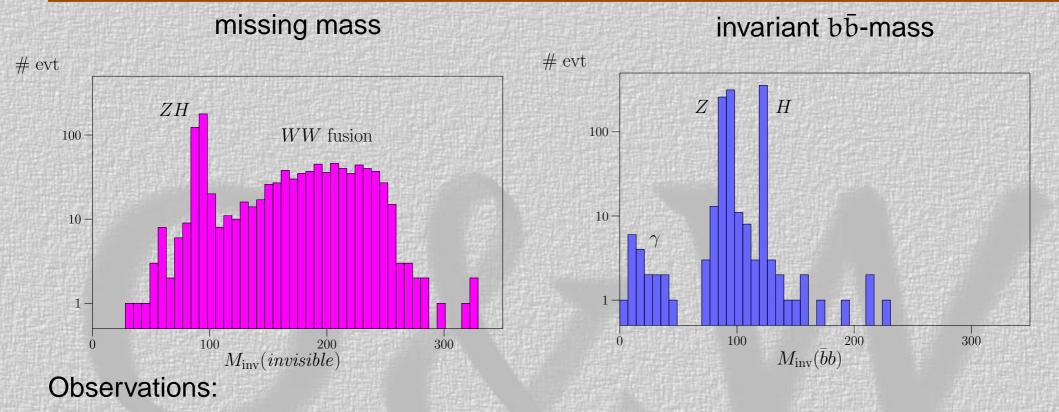




## invariant bb-mass

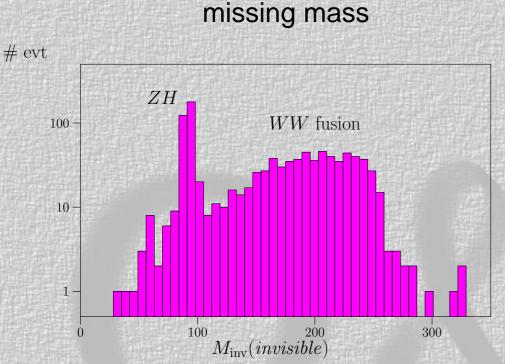




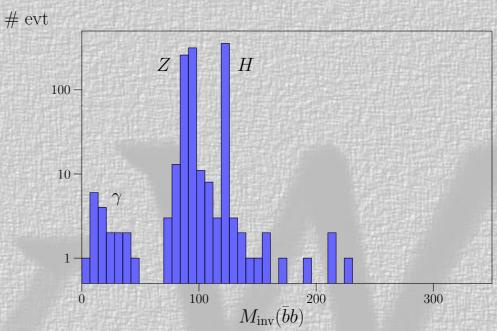


adaption typically takes a bit longer than event generation





### invariant bb-mass



#### **Observations:**

- adaption typically takes a bit longer than event generation
- adapted grids and weights can be saved and reloaded if the cuts and parameters are changed only slightly

### WHIZARD will be available from

http://www-ttp.physik.uni-karlsruhe.de/~kilian/whizard/soon.



	Further On Up The Road	19
1	Mission	2
2	O'Mega	5
3	WHIZARD	12
4	Further On Up The Road	20



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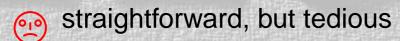
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