

# THEORETICAL PERSPECTIVES FOR LC

## 1. INTRODUCTION

## 2. CENTRAL FOCUS

- Higgs mechanism and also symmetry breaking
- Supersymmetry
- Space-time structure

## 3. PLATFORM

- Electroweak and strong gauge symmetries
- The top quark

## 4. CONCLUSIONS

## MATERIAL :

ECFA / DESY TESLA TDR Reports

<http://www.desy.de:8088/HEP/desy-rep.html>

The case for a 500 GeV  $e^+e^-$  Linear Collider

J. Bagge et al, hep-ex/00.07.022

Linear Collider Physics

P. Derwent et al, FNAL LC Study Group

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Physics Opportunities of  $e^+e^-$  Linear Colliders

H. Murayama and M.E. Peskin, Ann. Rev. N.P. Sci 46(1996)533

hep-ph/96.06.003

Physics with  $e^+e^-$  Linear Colliders

E. Accomando et al, Phys. Rep. C299(1998)1

hep-ph/97.05.442

Possible Accelerators at CERN beyond LHC

J. Ellis, Lund 1999 Proceedings, hep-ph/99.11.440

Physics with  $e^+e^-$  Linear Colliders at High Luminosity

P.M. Zewar, Cargèse Lectures, hep-ph/00.03.221

# 1. INTRODUCTION

LC target: (1) high-precision coverage of energy range above LEP2 up to  $\sim 1\text{TeV}$

scale of ebs SB:  $v \sim 246\text{ GeV}$  }  
complementarity to LHC }

(2) energy frontier and high-precision coverage of multi-TeV range in après-LHC era

energy range:  $\sim 5\text{TeV}$  }  
[complementarity to LHC - phase 2 ...] }

Physics: Higgs mechanism / alternative ebs SB

Supersymmetry: SUSY breaking  
reconstruction of fund. theory

Space-time structure: exploring extra dimensions

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Gauge symmetries of the forces / extended symmetries

Profile of top quark

Comprehensive and high precision coverage of energy range above LEP2 to multi TeV  $\rightarrow$  extrapolations of physics to areas eventually far above those which can be reached directly.

## MACHINE DESIGNS :

	$\sqrt{s}$	$\int \mathcal{L}$
$\gamma$ LC/NLC//TESLA	500 GeV 1 // 0.8 TeV	500 $\text{fb}^{-1}$ 1 $\text{ab}^{-1}$
CLIC	500 GeV 3 to 5 TeV	500 $\text{fb}^{-1}$ 1 $\text{ab}^{-1}$

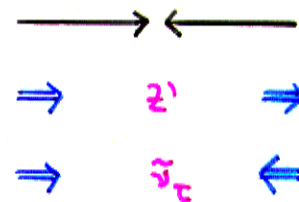
F

## POLARIZATION :

$$P[e^-] \sim 80\%$$

## DIAGNOSTICS

$$P[e^+] \sim 40/60\%$$

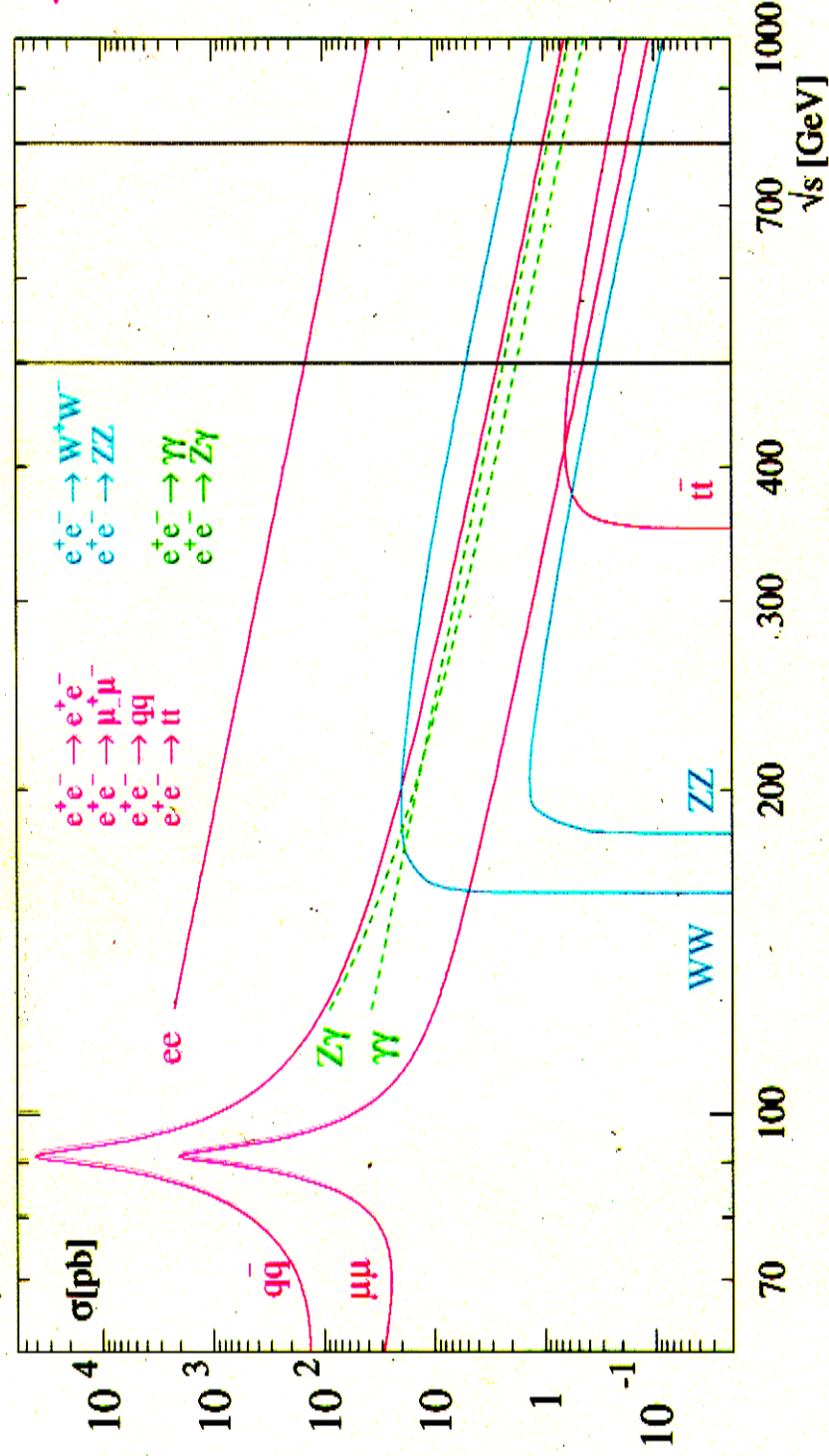


## SATELLITE MODES :

	$\sqrt{s}$	$\int \mathcal{L}$
Giga Z	91.187 GeV	$2 \times 10^9 \text{ Z}$
$e^-e^-$	100%	20%
$e\gamma$	90%	40%
$\gamma\gamma$	80%	40%

Linear colliders offer not only high-precision instruments for  $e^+e^-$  physics at per-mille level, but also a variety of additional experimental opportunities for dedicated problems.

Plot of  $\sigma$



## 2a) HIGGS MECHANISM

Theorem: asymptotic unitarity of gauge theories:

$f_{22} \leq 1 \rightarrow$  "light" fund. Higgs boson:  $q\bar{q} \sim m\bar{m}$

$\rightarrow$  WW strongly interacting:  $s > 4\pi\sqrt{3}/G_F = (1.2 \text{ TeV})^2$

### HIGGS MASS:

Standard Model:

$$M_H \leq 200 \text{ GeV}$$

LEP/SLC

Elect. Radiative

(i) radiate elec corrections LEP/SLC/...



$$M_H = 86^{+48}_{-32} \text{ GeV}$$

$$\leq 194 \text{ GeV } 95\% \text{ CL}$$

[missing 2-loop bosonic corrections ...

very likely not significant]

F

(ii) direct search LEP2:

$$M_H > 113 \text{ GeV}$$

$$M_H \approx 115 \text{ GeV}$$

clarification:

next year?

several years?

(iii) stability of prediction?

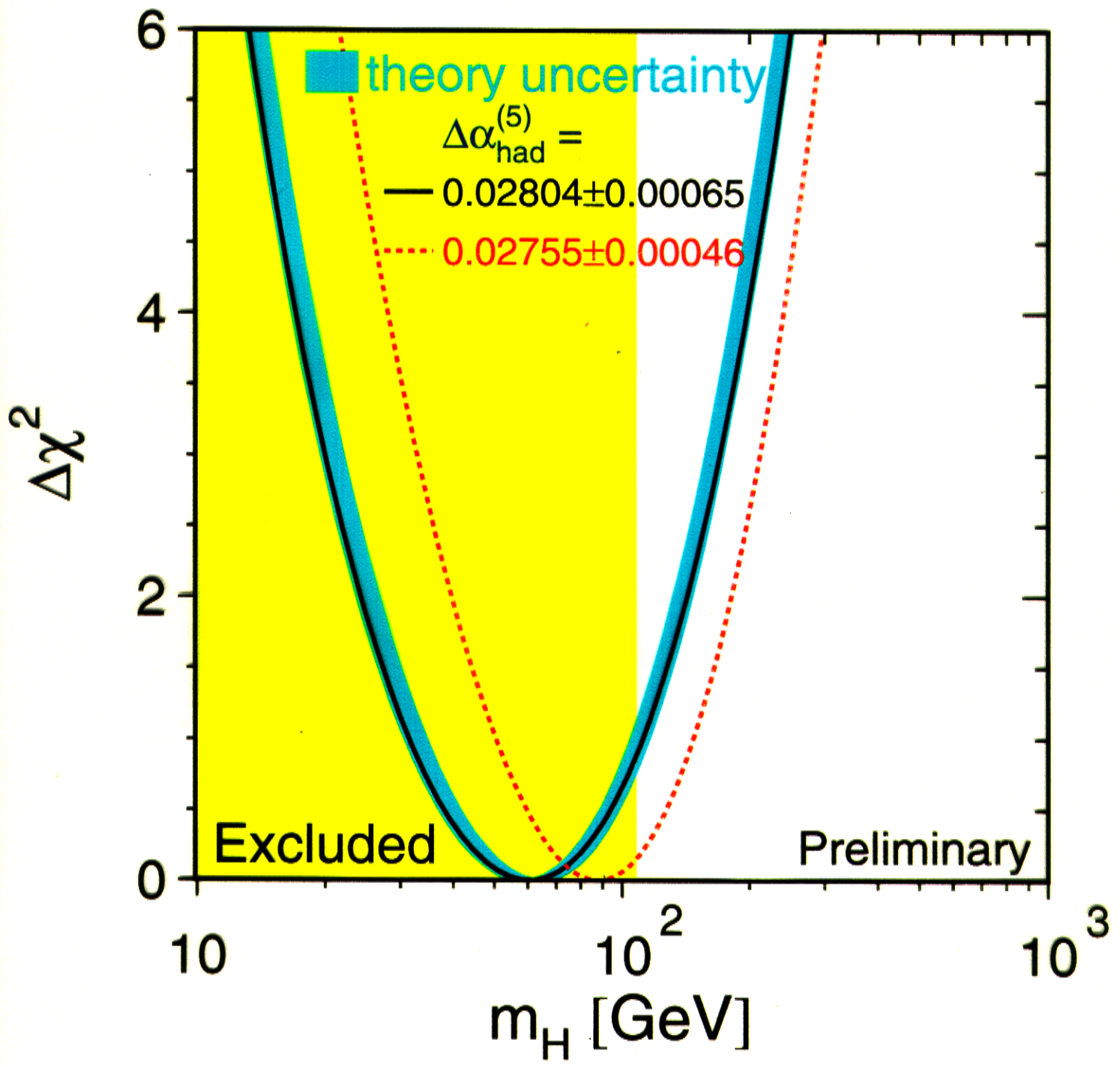
$$\blacksquare \mathcal{L} = \mathcal{L}_{SM} + \sum \frac{c_i}{\Lambda^2} \mathcal{O}_i \Rightarrow S, T, U : M_H \leq 400 \text{ GeV}$$

F

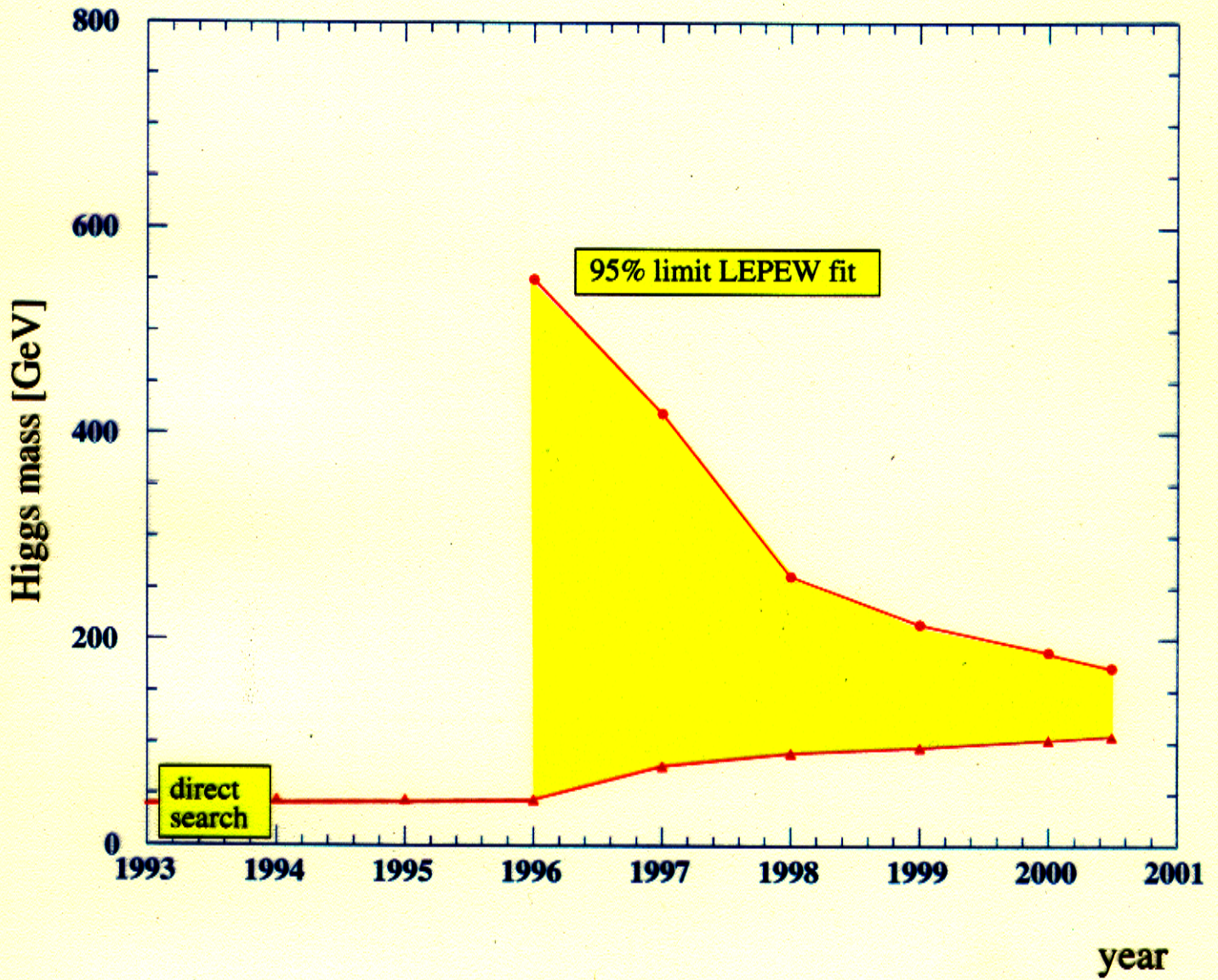
$$\blacksquare \text{no fundamental Higgs} : \Lambda_x \leq 3 \text{ TeV}$$

Bagger et al

LEPEWW6



Behrke





Dimensions six operators	$m_h = 100$ GeV		$m_h = 300$ GeV		$m_h = 800$ GeV	
	$c_i = -1$	$c_i = +1$	$c_i = -1$	$c_i = +1$	$c_i = -1$	$c_i = +1$
$\mathcal{O}_{WB} = (H^\dagger \tau^a H) W_{\mu\nu}^a B_{\mu\nu}$	10	9.7	6.9	—	6.0	—
$\mathcal{O}_H =  H^\dagger D_\mu H ^2$	5.5	4.5	3.7	—	3.2	—
$\mathcal{O}_{LL} = \frac{1}{2} (\bar{L} \gamma_\mu \tau^a L)^2$	8.1	5.9	6.3	—	—	—
$\mathcal{O}'_{HL} = i(H^\dagger D_\mu \tau^a H)(\bar{L} \gamma_\mu \tau^a L)$	8.8	8.3	6.6	—	—	—
$\mathcal{O}'_{HQ} = i(H^\dagger D_\mu \tau^a H)(\bar{Q} \gamma_\mu \tau^a Q)$	6.6	6.9	—	—	—	—
$\mathcal{O}_{HL} = i(H^\dagger D_\mu H)(\bar{L} \gamma_\mu L)$	7.6	8.9	—	—	—	—
$\mathcal{O}_{HQ} = i(H^\dagger D_\mu H)(\bar{Q} \gamma_\mu Q)$	5.7	3.5	—	3.7	—	—
$\mathcal{O}_{HE} = i(H^\dagger D_\mu H)(\bar{E} \gamma_\mu E)$	8.8	7.2	—	7.1	—	—
$\mathcal{O}_{HU} = i(H^\dagger D_\mu H)(\bar{U} \gamma_\mu U)$	2.4	3.3	—	—	—	—
$\mathcal{O}_{HD} = i(H^\dagger D_\mu H)(\bar{D} \gamma_\mu D)$	2.2	2.5	—	—	—	—

Table 1: 95% lower bounds on  $\Lambda/\text{TeV}$  for the individual operators and different values of  $m_h$ .

Saikat  
Sharma

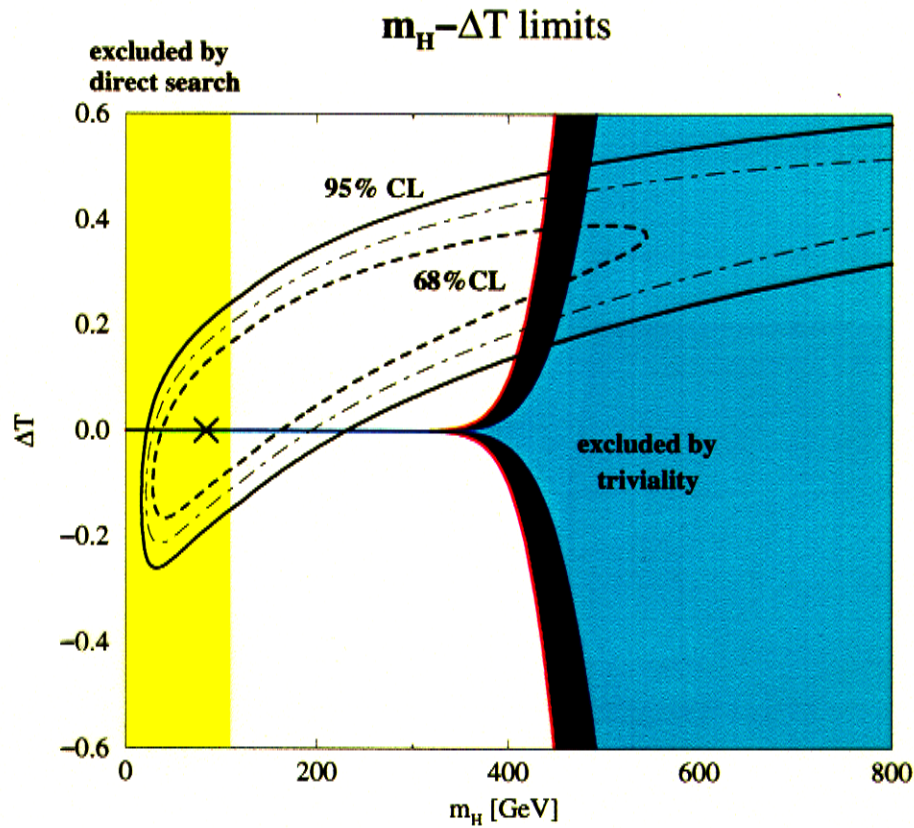


Figure 1: 68% and 95% CL bounds in the  $(m_H, \Delta T)$  plane allowed by a fit to precision electroweak data [1, 2]. The best fit “standard model” value is shown by the cross on the  $\Delta T = 0$  line. (Also shown by the dot-dash curve is the contour corresponding to  $\Delta\chi^2 = 4$ , whose intersection with the line  $\Delta T = 0$  - at approximately 190 GeV - corresponds to the usual 95% CL upper bound quoted on the Higgs boson mass in the standard model.) The light region to the right is excluded by eqn. 1.3 for  $b\kappa^2 = 4\pi$ . The dark region denotes the additional area excluded for  $b\kappa^2 = 4\pi^2$ . The positive branches of the curves bounding these regions are lower bounds for  $\Delta T$  in the top-seesaw and composite higgs models described in the text. Any  $(m_H, \Delta T)$  with positive  $\Delta T$  and to the left of the appropriate triviality curve can be realized in the corresponding model.

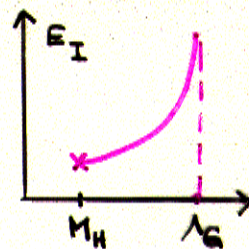
*Chivukula et al*

GUT:

$$M_H \approx 180 \text{ GeV}$$

unification also  $\oplus$  Thoug:

$$\text{no thg scale} \Rightarrow \sin^2 \theta_w = 0.2 \dots$$



SUSY Higgs:

$$M(\tilde{h}^0) \approx 180 \text{ GeV}$$

Higgs spectrum: MSSM:  $m(\tilde{h}^0) \approx 135 \text{ GeV}$

gener.: ext. to  $M_{\text{GUT}}$

Carone et al.

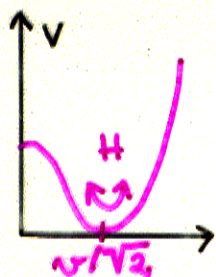
Summary:

precision data  
 $\oplus \sin^2 \theta_w$

most naturally accounted for  
light Higgs mass

## SM HIGGS MECHANISM

task: establish Higgs mechanism sui generis for generating masses of fundamental particles



(1) Higgs excitation  $\equiv$  Higgs boson  
must be discovered

LEP2  
Tevatron  
LHC

(2) generating masses by interaction  
with Higgs field: couple  $\sim$  mass

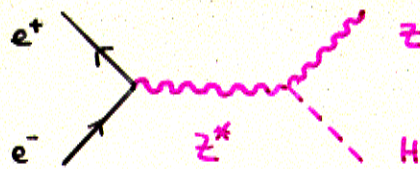
[LHC]  
LC

(3) Higgs field  $v/\sqrt{2}$  generated by Spont. Sym. Break:  
reconstruction of Higgs potential

LC

(1)

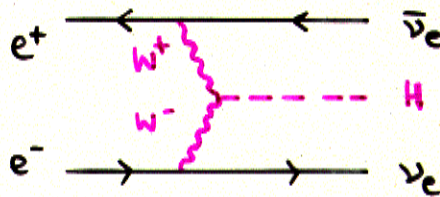
**Higgs-strahlung:**



$\sigma \sim \alpha^2/s$

$M_H \text{ mod.}$

WW fusion:



$\sigma \sim \alpha^3/M_W^2$

$M_H \text{ large}$

F:  $\sqrt{s} \sim 300 \text{ GeV} / \text{fb} = 500 \text{ fb}^{-1}$

$M_H \sim \text{intermed. mass range}$

**$10^5$  Higgs bosons**

F: almost background-free

**particle param.:**

mass

50 MeV

lifetime -  $BR_i / \Gamma_i$  [ $i = WW/\gamma\gamma$ ]

5-16%

spin-parity / CP

*hilar, Para Hagiman ea*

- $HZZ, HWW$  :
- $Hff$  [ $b, \tau, c \dots$ ]:
- $Htt$  :

prod. / decay

$Z/W$

decays

$b/W$

$b/\tau$

$e^+e^- \rightarrow t\bar{t}H$

$b/c$

*Djanadi ea  
Deuron ea  
Jushe ea*

(3)  $V = \lambda [\varphi^2 - \frac{1}{2} v^2]^2 = \lambda v^2 H^2 + \lambda v H^3 + \frac{\lambda}{4} H^4$

mass  $M_H^2 = 2\lambda v^2$

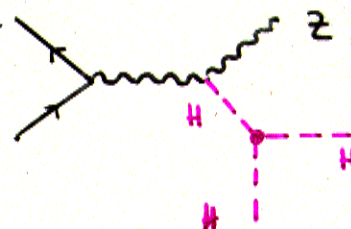
kilin. / quadril. cpl.

**HHH:**

double Higgs-strahlung

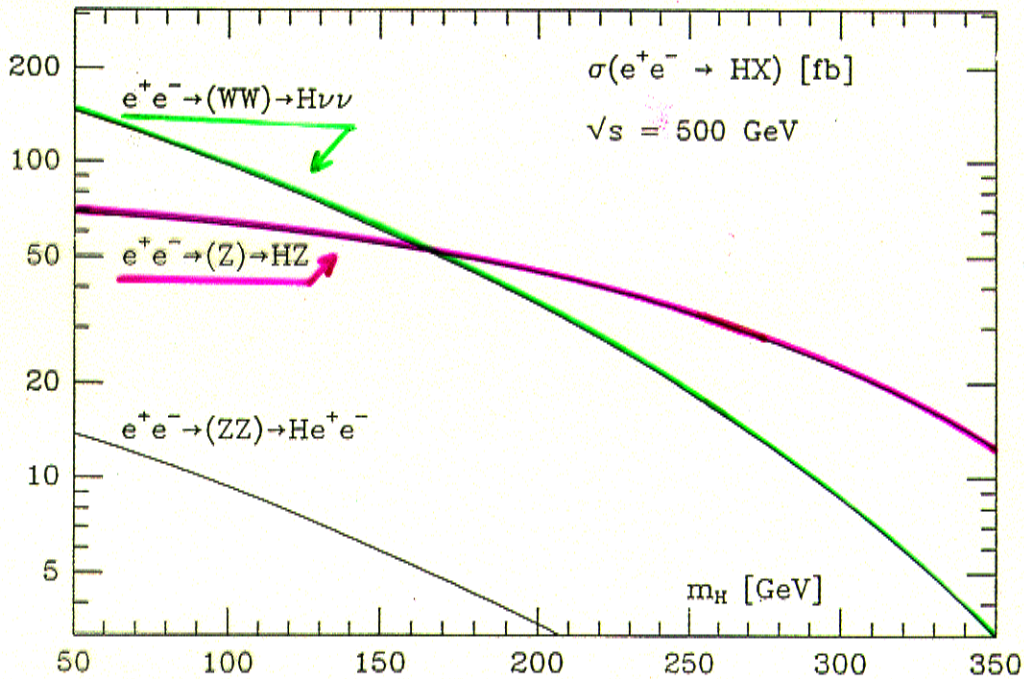
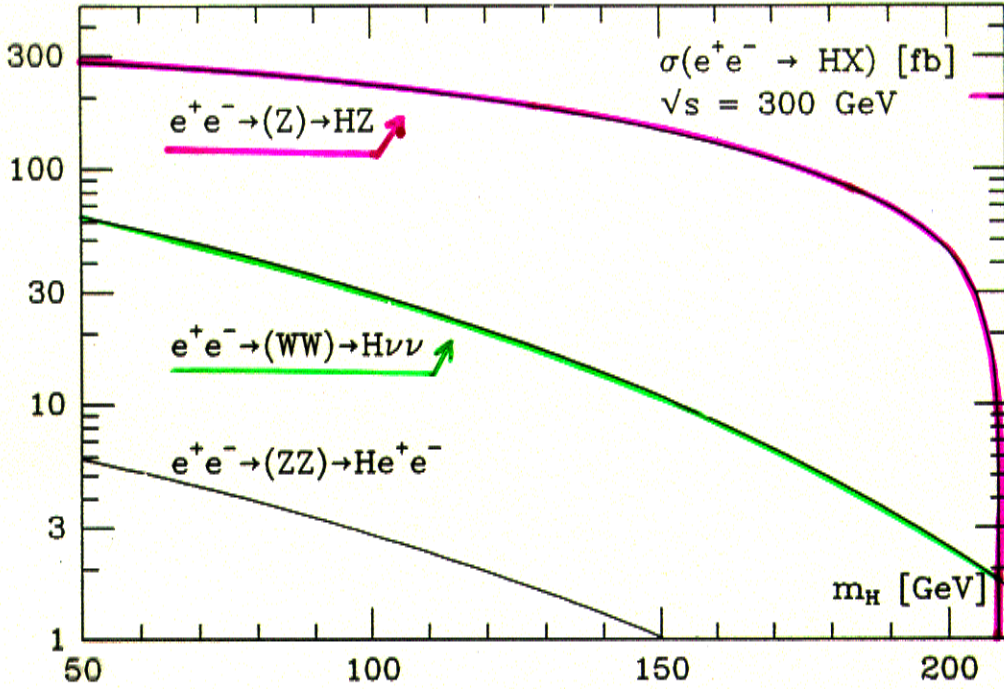
$\sigma \approx \text{few } 10^{-1} \text{ fb}$

$\Delta\lambda/\lambda \approx 18\%$



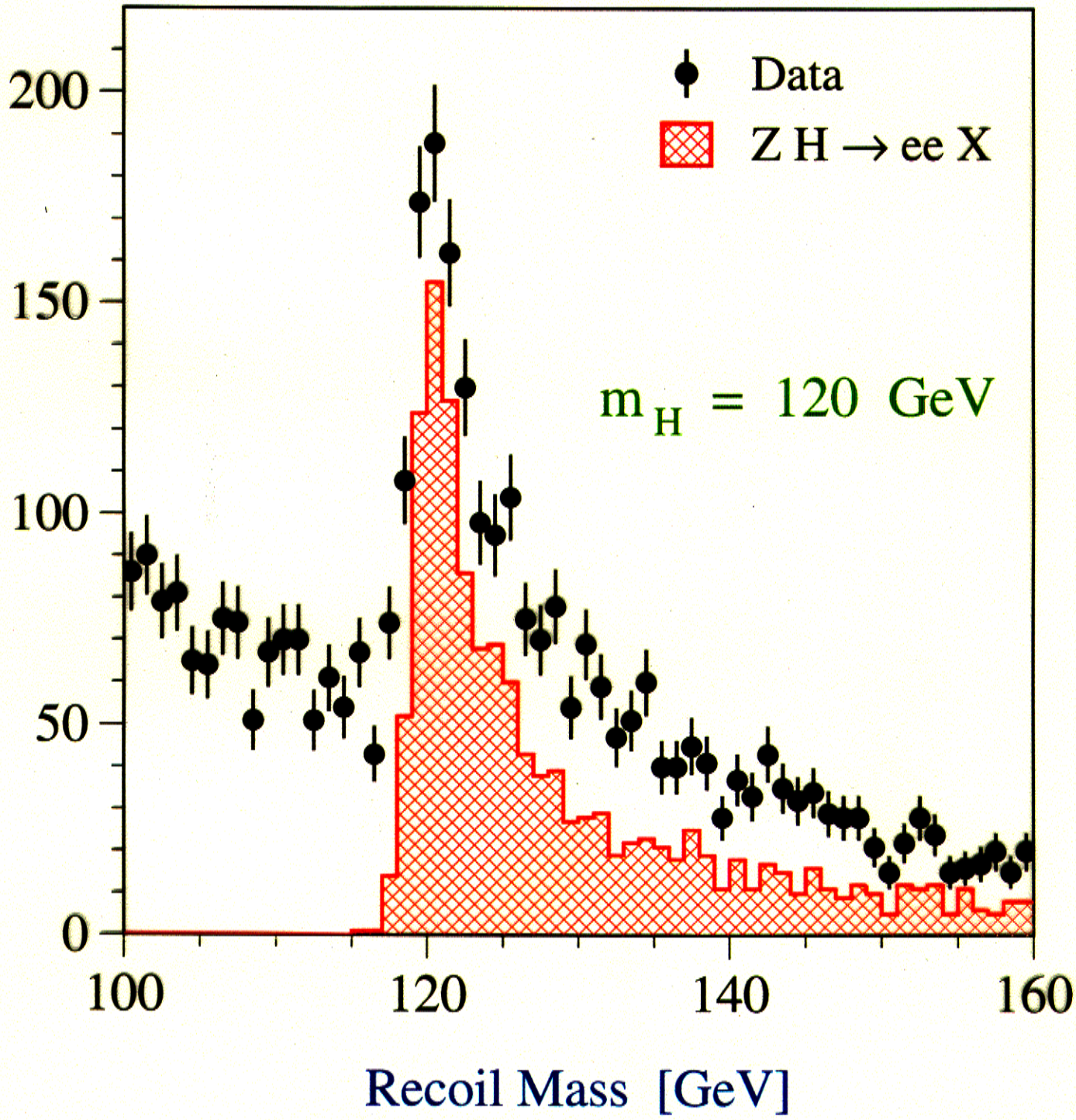
Dionadi et al

$\int \mathcal{L} = 500 \text{ fb}^{-1}$

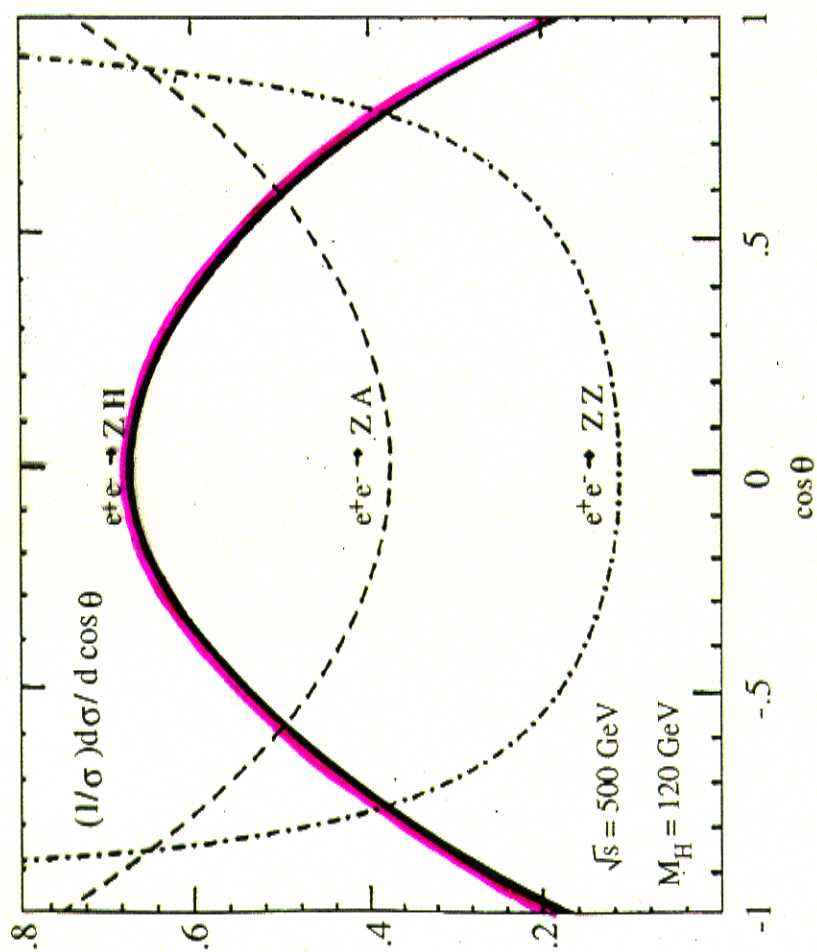


Jarvis - Abri  
Lohmann

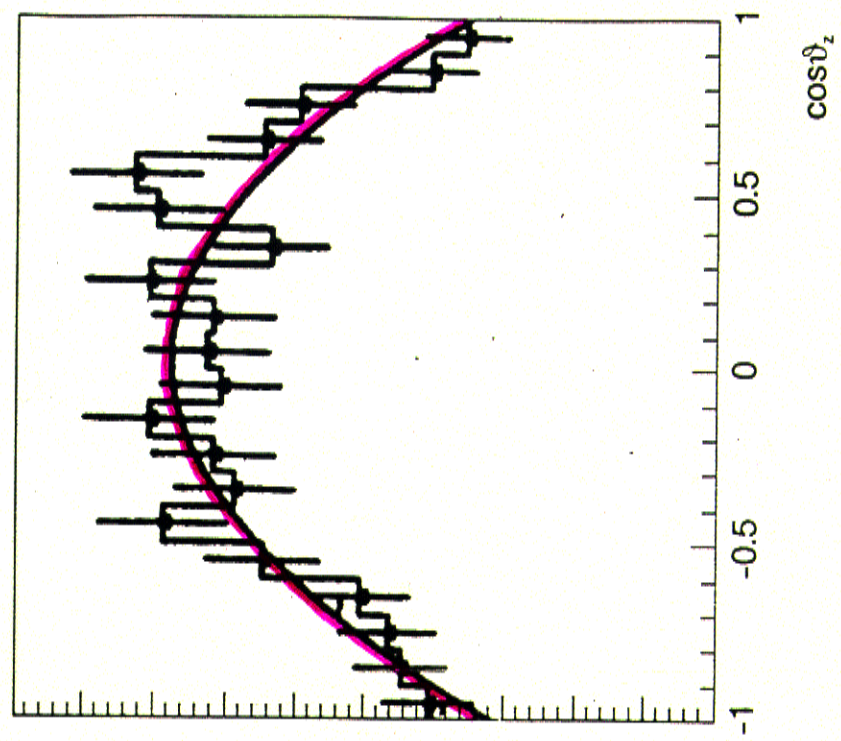
Number of Events / 1 GeV



Uwille et al



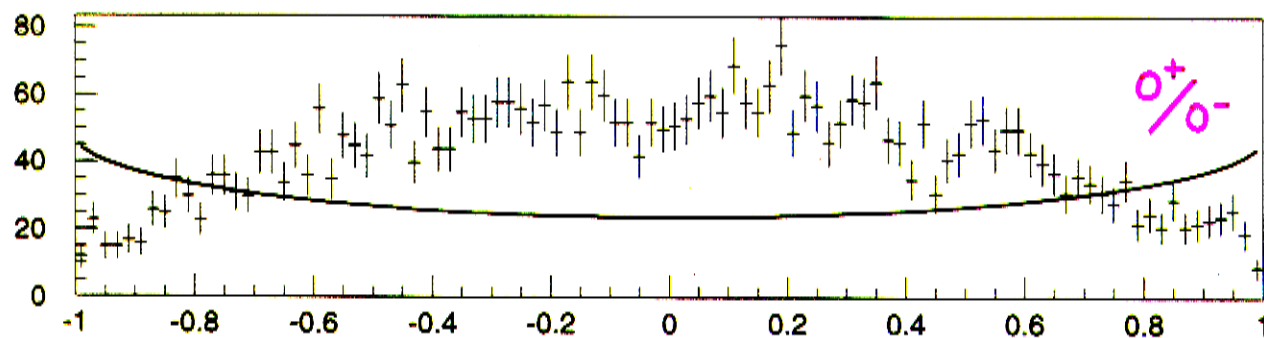
JLC



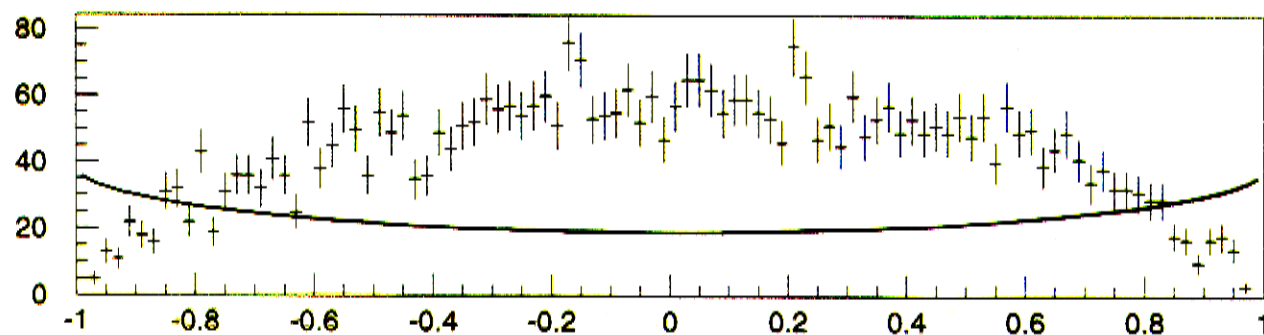
$e^+e^- \rightarrow ZH$

A. PARR

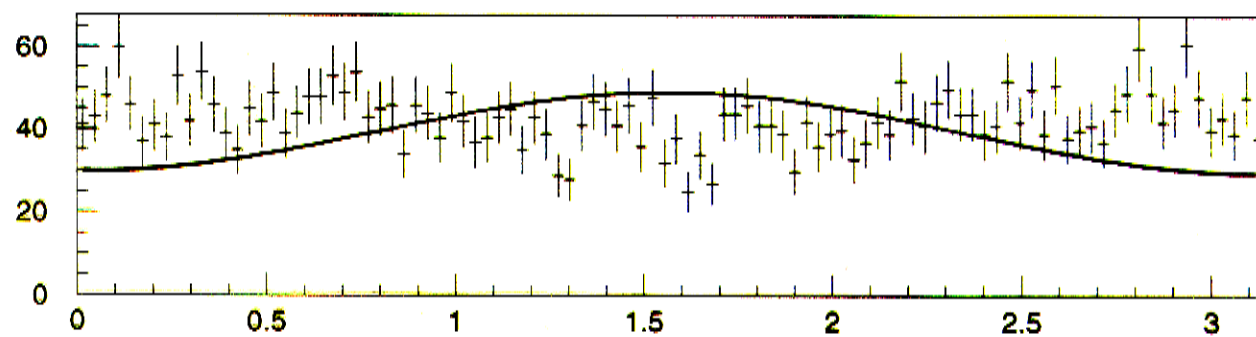
Fit of a pseudoscalar hypothesis



$Z$  :  $\cos(\theta)$ , scalar



$Z \rightarrow f$  :  $\cos(\theta_{\text{star}})$ , scalar

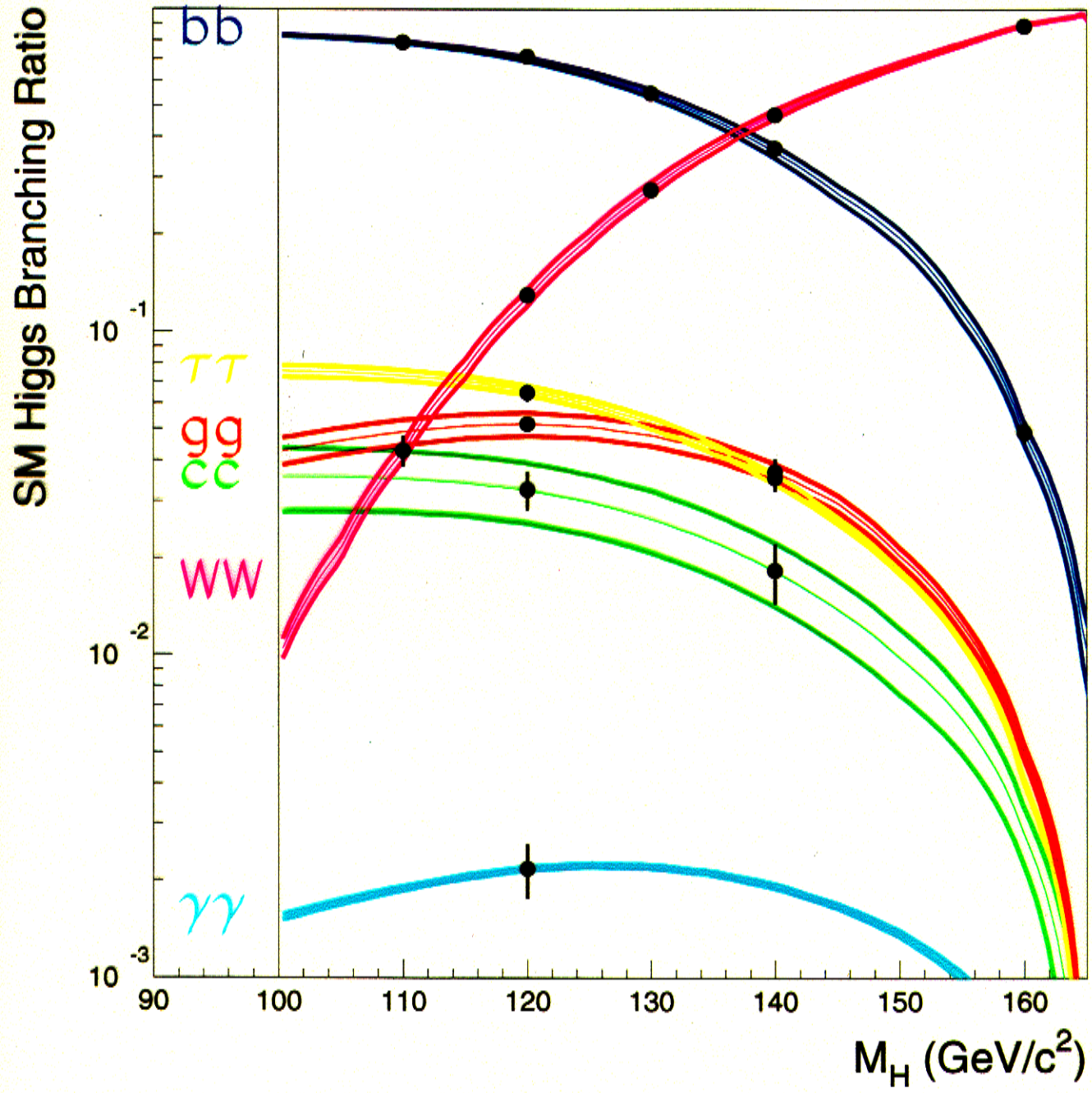


$Z \rightarrow f$  :  $\phi_{\text{star}}$ , scalar



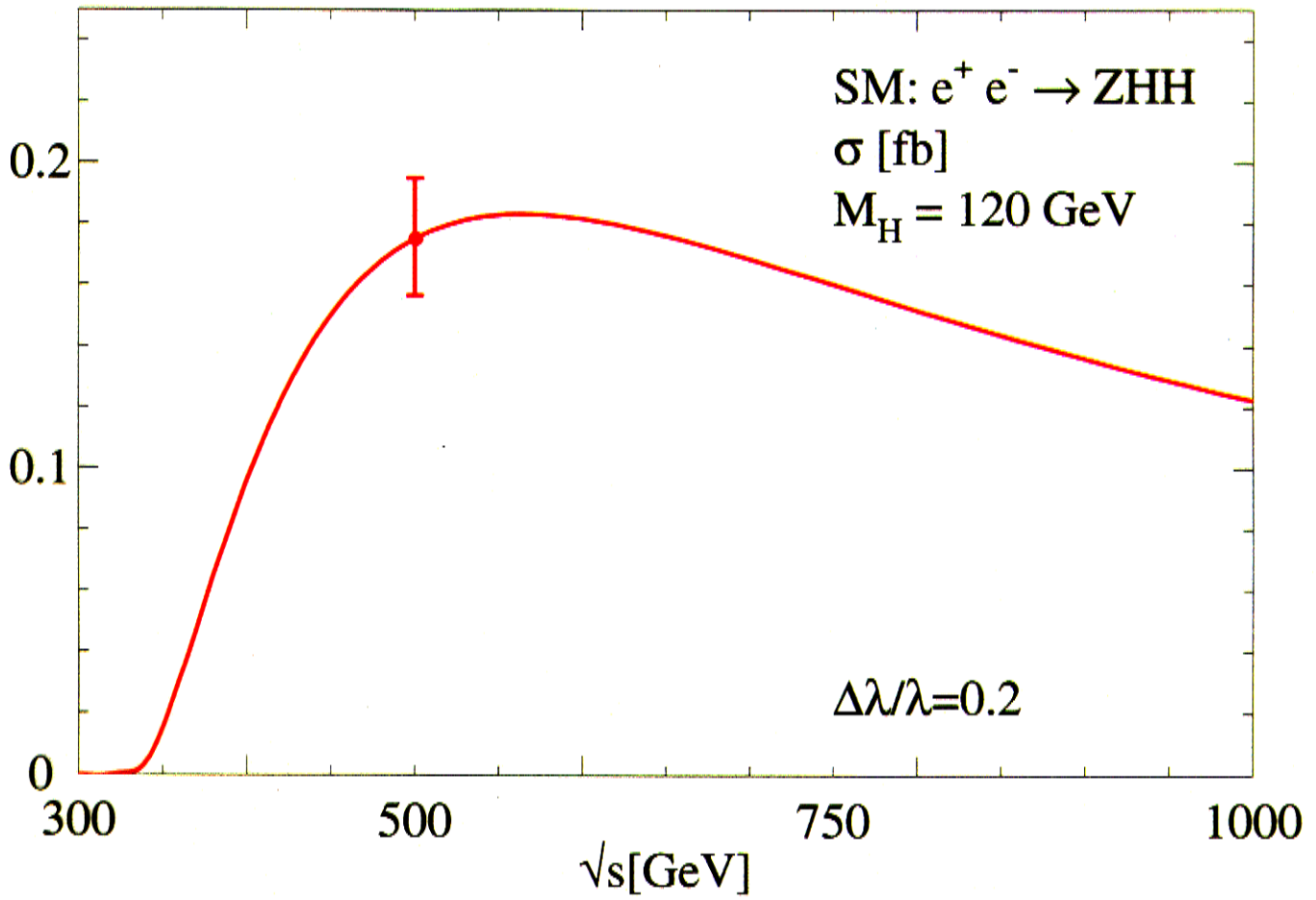
Bataglia

LC - 500 fb<sup>-1</sup>



Channel	$\delta(BR(H \rightarrow X)/BR)$	
	CDR Vtx.	Improved Vtx.
$H^0/h^0 \rightarrow bb$	$\pm 0.024$	$\pm 0.024$
$H^0/h^0 \rightarrow c\bar{c}$	$\pm 0.135$	$\pm 0.083$
$H^0/h^0 \rightarrow gg$	$\pm 0.055$	$\pm 0.055$
$H^0/h^0 \rightarrow \tau^+\tau^-$	$\pm 0.060$	
$H^0/h^0 \rightarrow WW^*$	$\pm 0.054$	

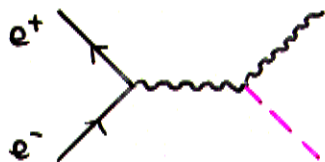
*Wählleitner  
Gay, Lutz*



# SUSY HIGGS BOSONS

spectrum:  $h^0$   $\leq$  135/180 GeV } param.:  
 $H^0, A^0, H^\pm, \dots$   $\sim$   $\mathcal{O}(v) - \mathcal{O}(TeV)$  }  $M_A, \tan\beta$

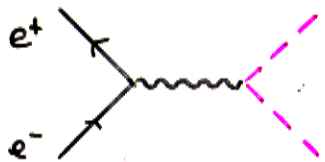
Higgs-Production:



$$\sigma(Zh) = \sigma_0 \times \sin^2 \beta \alpha$$

$$\sigma(ZH) = \sigma_0 \times \cos^2 \beta \alpha$$

pair production:



$$\sigma(AA) = \sigma_0 \lambda \times \cos^2 \beta \alpha$$

$$\sigma(AH) = \sigma_0 \lambda \times \sin^2 \beta \alpha$$

mutual  $\sin^2/\cos^2$  coefficients

$M_A$  small  $\leftrightarrow$   $\cos^2$  large

$Zh/AA$  cov. ps: h found

$Zh/ZH$  cov. ps: indep. dec.

heavy  $H, A, H^\pm$ : pair production in  $e^+e^- \rightarrow HA$  and  $H^+H^-$  **F**

LHC probe.  $> 200-500$  GeV **F**

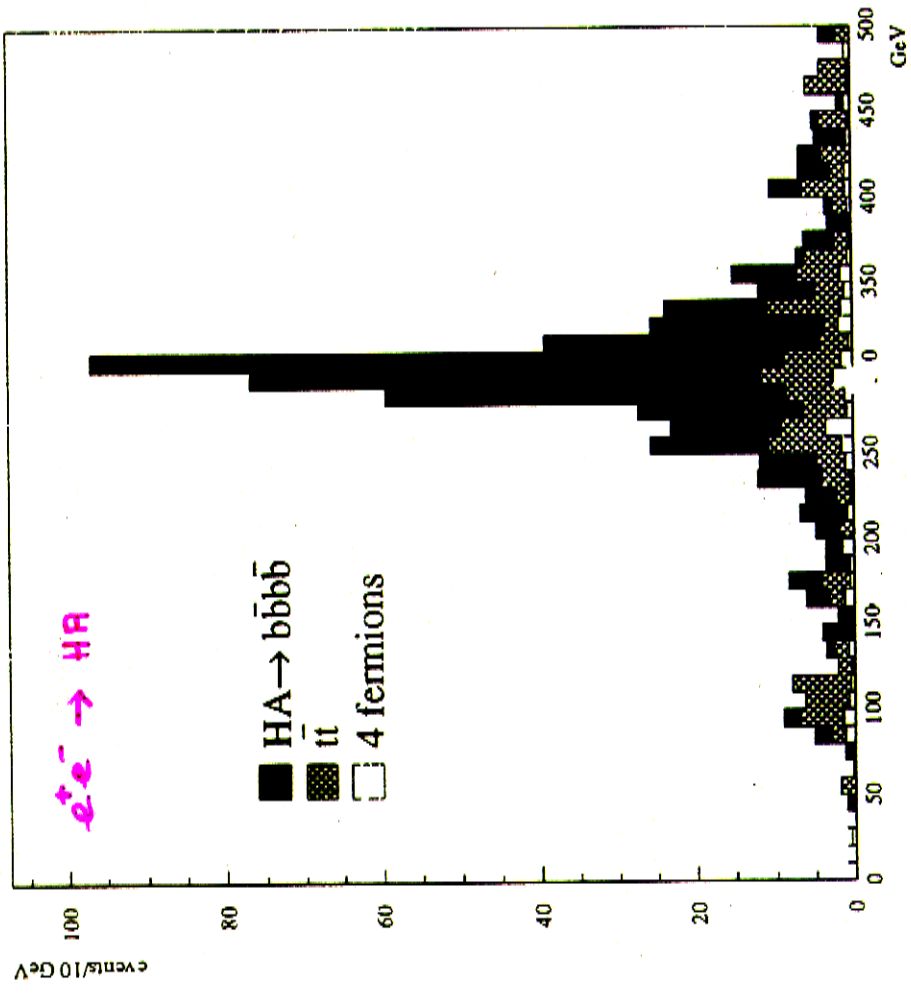
CLIC acc. up to 2.5 TeV

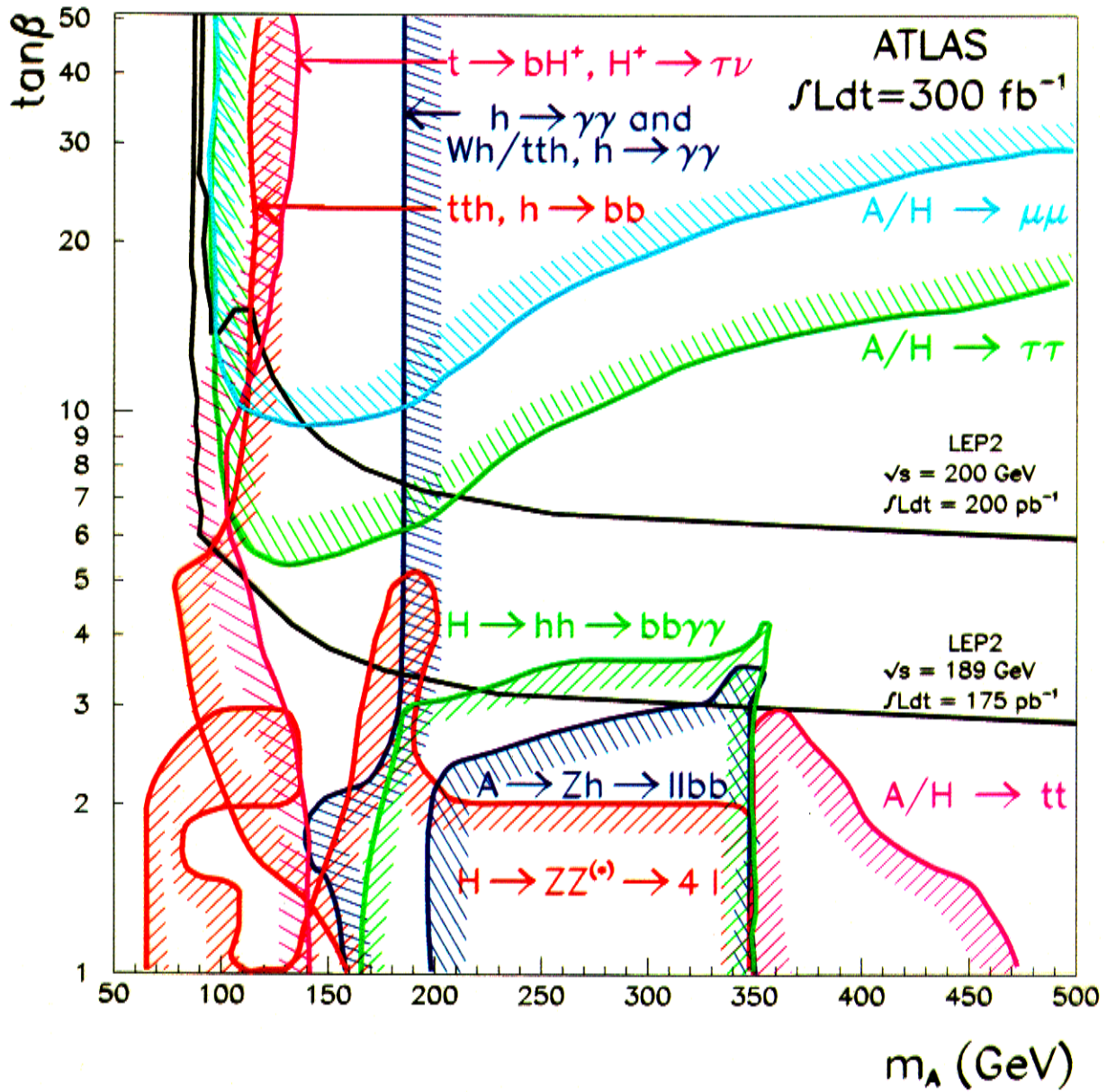
single production in  $gg \rightarrow A, H$ :

LHC dead zone covered **F**

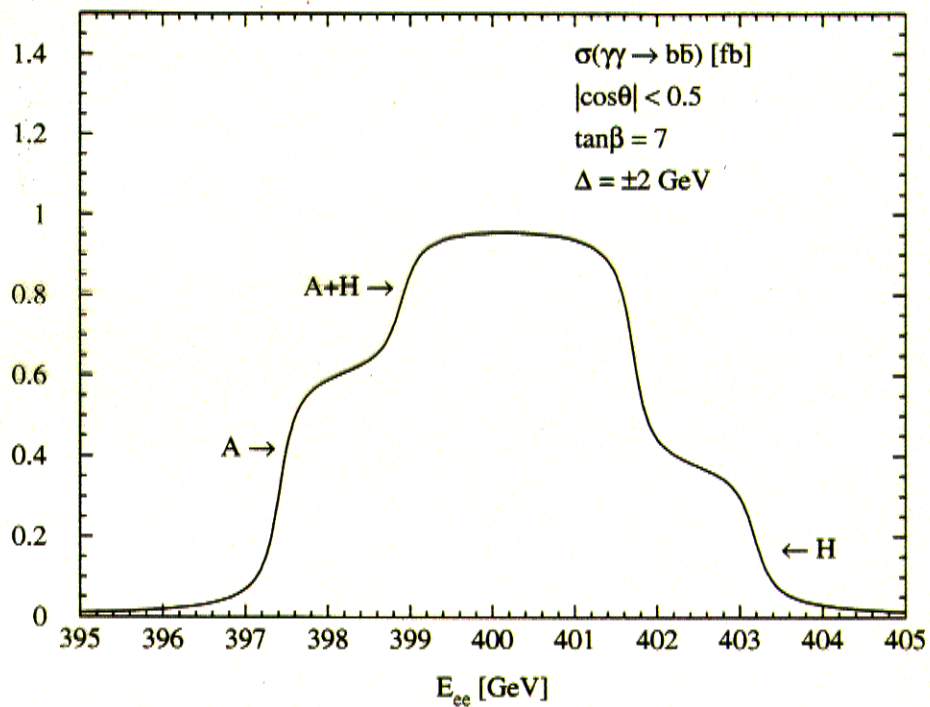
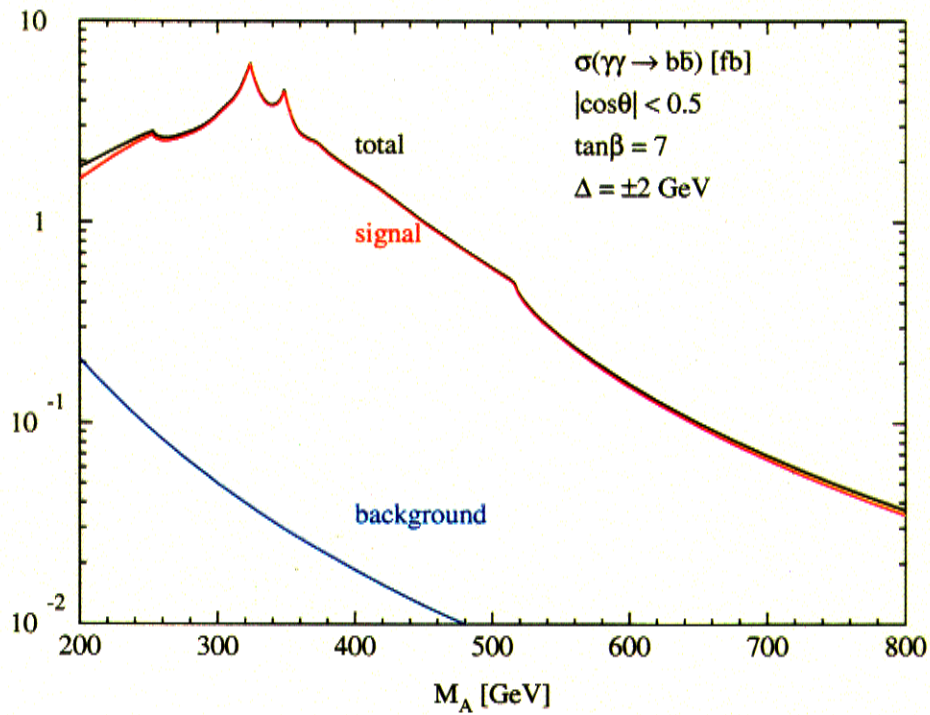
Andreas

Trojan





Müllerbauer  
Krauss, Spira, &



EXTENDED HIGGS SECTOR : no-lose theorem for discovery :

Ellwanger et al  
Espinoza, Gunion

lightest

↓  
second lightest ~ lightest

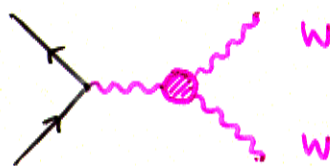
↓  
...

**STRONG ELW SYMMETRY BREAKING**

dynamical elw symmetry breaking : new strong interactions  $\Lambda_*$   
chiral sym : spont. broken  
Goldstone bosons ~  $W_L$  states

(a) anom. trilin. W cplg :

Ohl et al



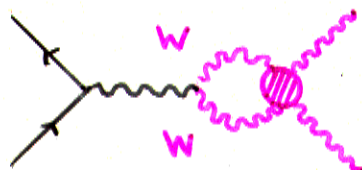
$\sqrt{s} = 500 \text{ GeV}$

$\Lambda_* \lesssim 3 \text{ TeV}$

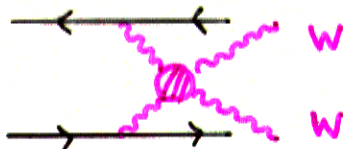
(b) anom. quadril. W cplg :

Barlow

Zoor et al



$M_Z \lesssim 2.5 \text{ TeV}$



$\sqrt{s} = 800 \text{ GeV}$

$\Lambda_* \lesssim 2.5 \text{ TeV}$

(c) resonance production :

in CLIC range

F

(d) pseudo-Goldstone bos. :

Casalbuoni et al.

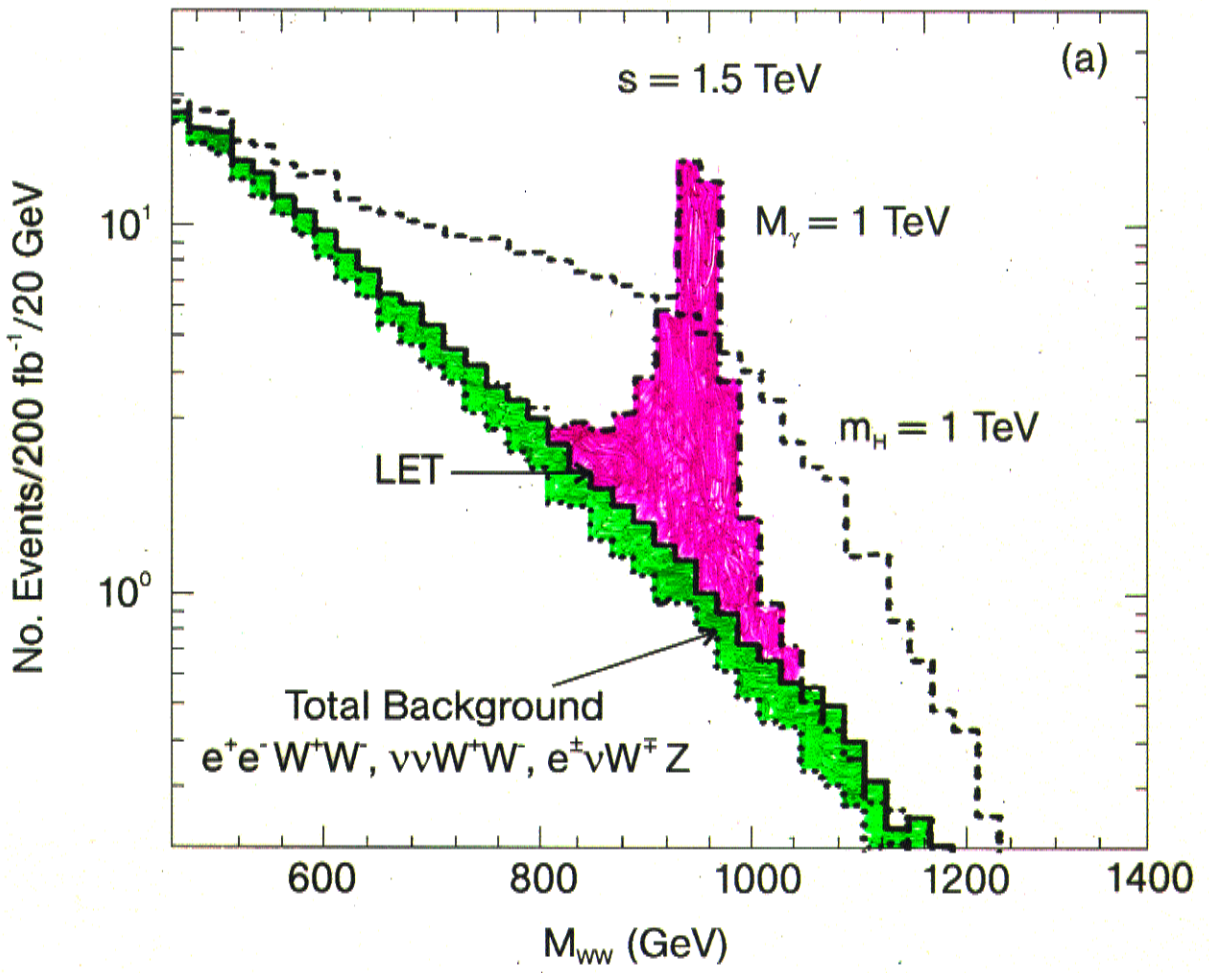
$\gamma\gamma \rightarrow P^0$   
 $e^+e^- \rightarrow \gamma P^0$

$M(P^0) \lesssim 0.7 \sqrt{s}$

$\lesssim 400 \text{ GeV}$



Barger...



The strongly interacting W sector, as alternative to the fundamental Higgs mechanism, can be probed:

$\sqrt{s} = 500 \text{ GeV}$  : WW strong threshold region  $\Lambda_* \sim 3 \text{ TeV}$

$\sqrt{s} = 5 \text{ TeV}$  : establishing new resonances / mixg.

## 2b) SUPERSYMMETRY

SUSY: best motivated extension  
of Standard Model

✓  
HP

■ connection to gravity

■ grand unification:

$$\sin^2 \theta_w = 0.2335 \pm (17)$$

$$\text{EXP} = 0.2311 \pm (02)$$

### MASS SCALE:

■ generic solution of hierarchy problem / II :  $\tilde{M} \approx O(1 \text{ TeV})$

■ "fine tuning" of e/w precision param. :  $\tilde{X}^\pm \approx 300 - 500 \text{ GeV}$   
... Feng et al

■ estimates from CDM / mod. d. in SUGRA :  $\sqrt{s} \approx 1.2 \text{ TeV} \dots 2 \text{ TeV}$   
... Ellis et al ; Feng et al.

■ baryon asymmetry [mod. MSSM] :  $m_{\tilde{\tau}} \approx 150 \text{ GeV}$   
... Carena et al.  $\mu, M_2 \approx 400 \text{ GeV}$

SUSY DISCOVERY : LEP 2 ?

TeVatron

LHC :  $m(\tilde{q}, \tilde{g}) \lesssim 2 \text{ to } 3 \text{ TeV}$

$m(\tilde{\chi}) \lesssim 200 \text{ GeV}$

$m(\tilde{L}) \lesssim 350 \text{ GeV}$

direct

cascade:  $\uparrow$   
 $< m_{\tilde{g}}$

SUSY EXPLORATION :  $e^+e^-$  linear colliders

(1) Comprehensive reconstruction of entire SUSY spectrum

- masses
- production and decay
- spin - parity

↓

(2) extract the basic LE parameters :

- gaugino, higgsino, scalar mass parameters, etc.
- wave functions and mixings
- gauge - Yukawa couplings

↓

(3) analysis of SUSY breaking //

reconstruction of fundam. theory → high scale  $\sim$  gravity

LHC analyses : specific paths can be followed  
no comprehensive analysis

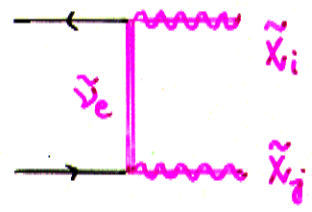
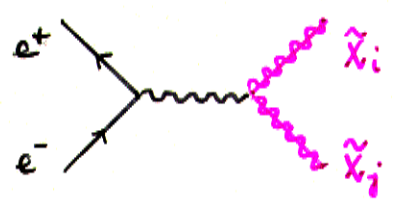
LC analyses : robust / very precise picture  
stable extrapol. to high scales

# SUPERSYMMETRIC PARTICLES

## Production :

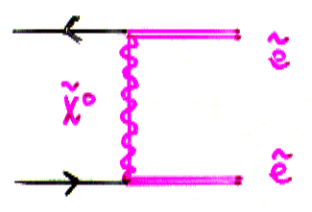
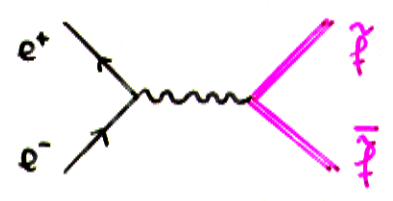
Markyn

- charginos / neutralinos



$$\sigma \sim \beta$$

- sleptons / squarks



$$\sigma \sim \beta^3$$

$$1/\beta$$

## DECAYS :

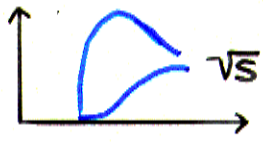
- $\tilde{X}_i \rightarrow W + \tilde{X}_1^0 \quad \oplus \quad n \text{ cascade}$
- $\tilde{l} \rightarrow l + \tilde{X}_1^0$
- $\tilde{q} \rightarrow q + \tilde{X}_1^0$

## MASSES :

special endpts  
in continuum



scan near prod  
threshold F



	end pt	thresh
$\tilde{X}_V$	200/300	40/500
$\tilde{l}$	200/300	70/600
$\tilde{q}$	$\sim 30 \text{ GeV}$	$\sim 1 \text{ GeV}$

## MIXING :

$$\tilde{X}_i = \alpha_{ij} \tilde{W}_j + \beta_{ij} \tilde{H}_j$$

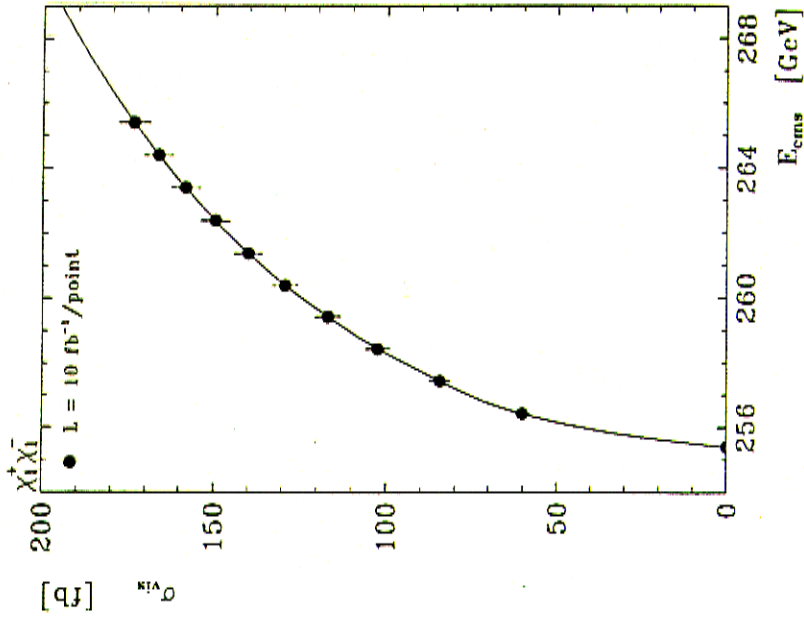
$$\tilde{t}_i = \alpha_{iL} \tilde{t}_L + \beta_{iR} \tilde{t}_R$$

etc.

prod  $e^\pm$  : F

Fung ea  
Kalinowski  
Uranl ea

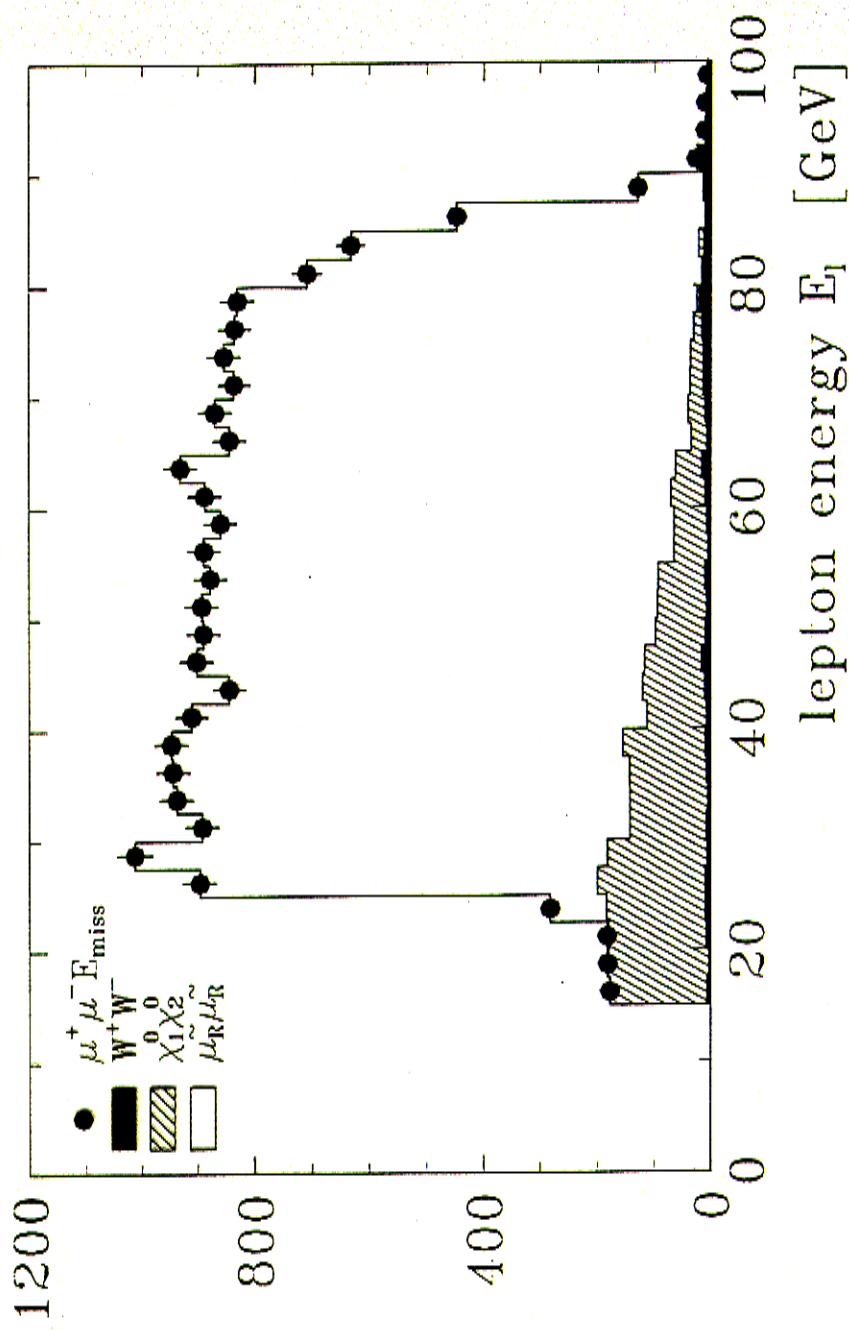
$$e^- e^+ \rightarrow \chi_1^- \chi_1^+$$



$$m_{\chi_1^\pm} = 127.7 \pm 0.04 \text{ GeV}$$

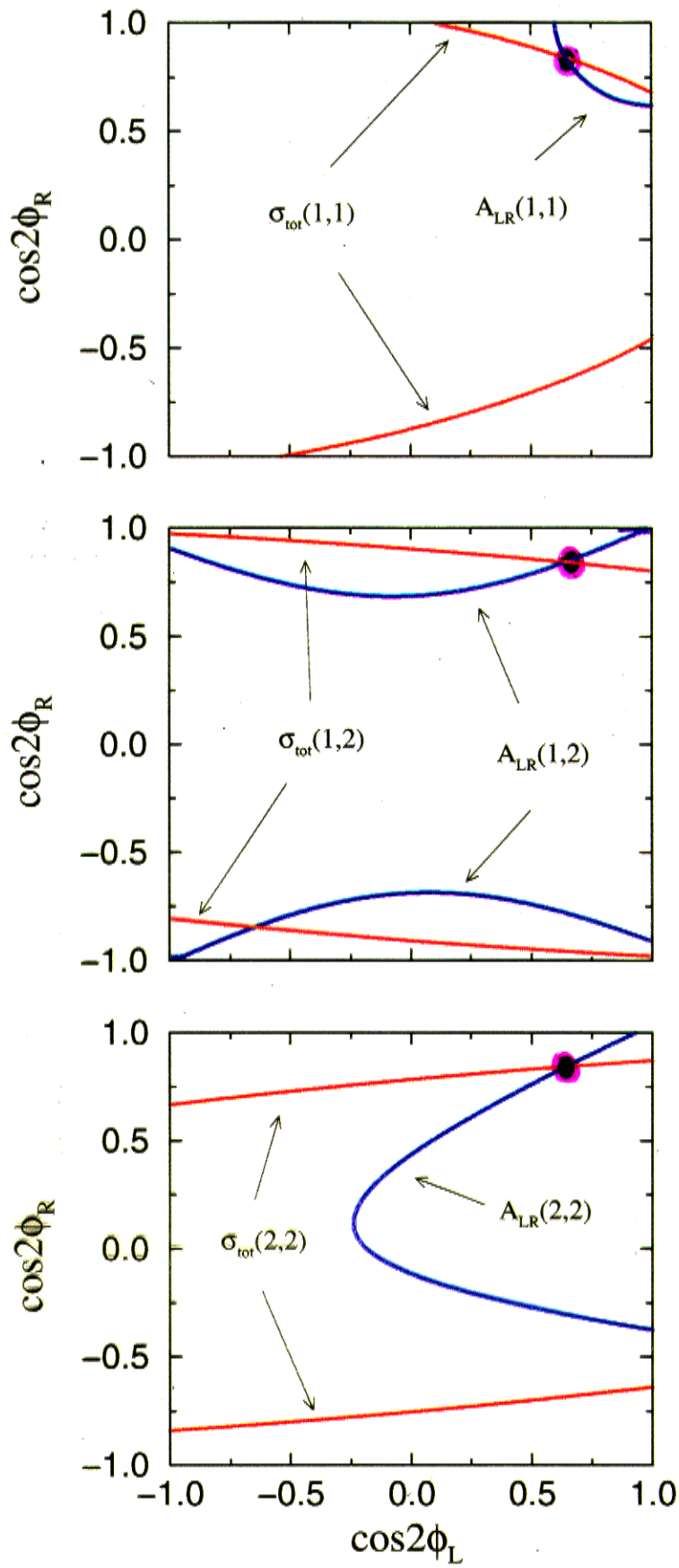
$$e^+ e^- \rightarrow \tilde{\mu}_R^+ \tilde{\mu}_R^-$$

*Marlyn*



$$m_{\tilde{\mu}_R} = 132.0 \pm 0.3 \text{ GeV} \quad m_{\chi_1^0} = 71.9 \pm 0.2 \text{ GeV}$$

Choi, Song,  
Djouadi, Z.



Information on parameters in  $\tilde{t}$  sector  
from direct production at high luminosity LC:

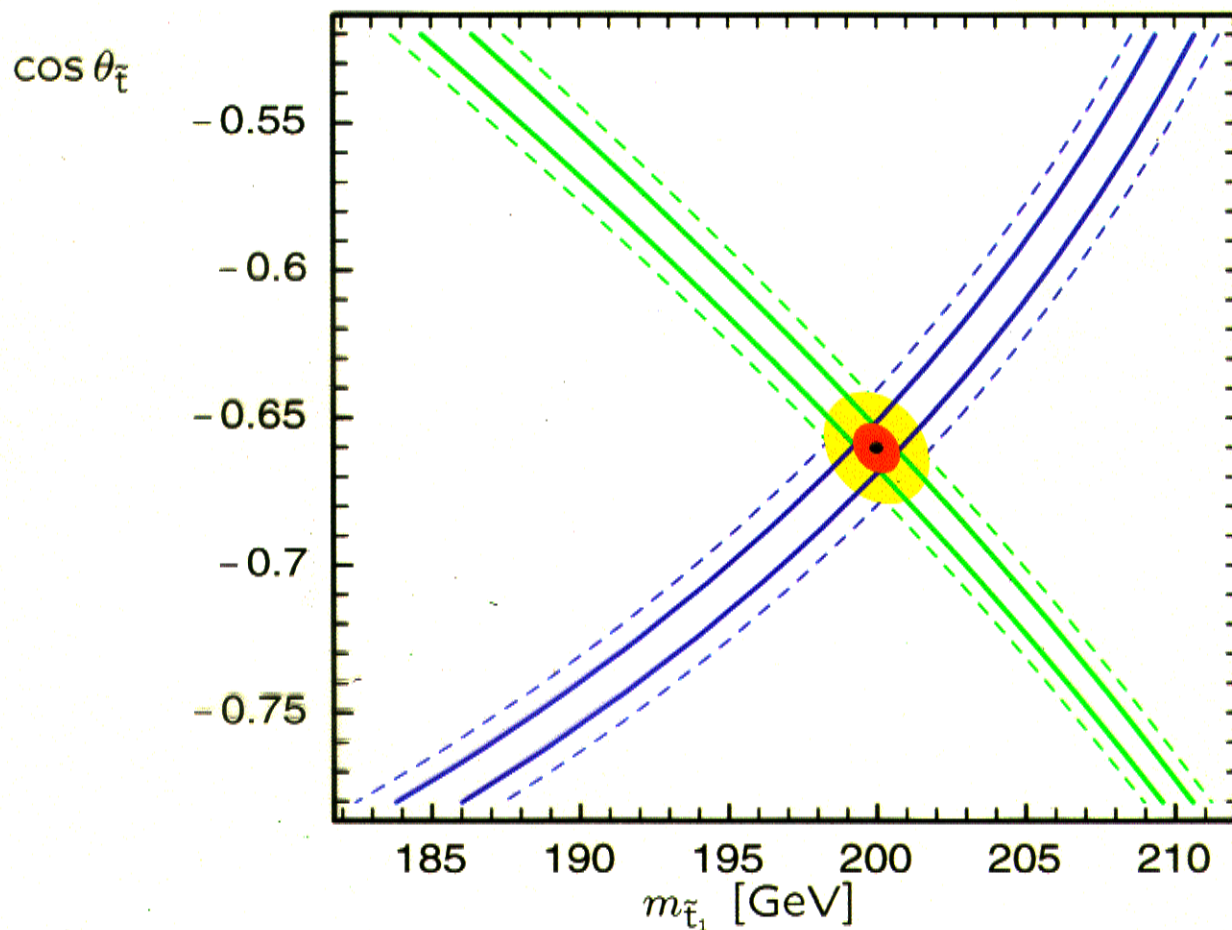
Determination of  $m_{\tilde{t}_1}$  and  $\theta_{\tilde{t}}$  in  $e^+e^- \rightarrow \tilde{t}_1\tilde{t}_1$   
with 90% polarized  $e^-$  beams,  $\sqrt{s} = 500$  GeV

[A. Bartl, H. Eberl, S. Kraml, W. Majerotto, W. Porod '99]

Two cases:  $\mathcal{L} = 100 \text{ fb}^{-1}$ ,  $\mathcal{L} = 500 \text{ fb}^{-1}$

$\mathcal{P}_L = -0.9$ :  $\sigma_L = 44.88 \text{ fb}$ ,  $\Delta\sigma_L = 1.73, 0.77 \text{ fb}$

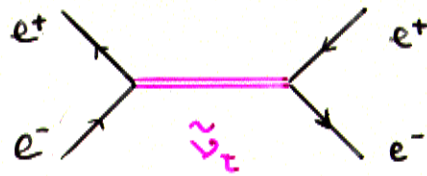
$\mathcal{P}_R = +0.9$ :  $\sigma_R = 26.95 \text{ fb}$ ,  $\Delta\sigma_R = 1.34, 0.6 \text{ fb}$



$m_{\tilde{t}_2} = 420 \text{ GeV}$ ,  $M = 200 \text{ GeV}$ ,  $\tan \beta = 4$ , ...

$\Rightarrow$  direct/indirect information is complementary  
very sensitive test of the model

## R-PARITY:



Bhabha scattering:  $\mathbb{R}$

$\mathbb{F}$

## BASIC SUSY LE PARAMETERS

$M_1, M_2, M_3$  gaugino param.

$\mu$  higgsino param

$m_0, \dots$  scalar param

$A$ 's higgs. superpot

Yukawa cplg  $\sim$  gauge cplg

...

$$M_2 / |\mu| = \frac{1}{2} [2(\chi_2 + \chi_1 - 2w) + (\chi_2 - \chi_1)(C_{2R} + C_{2L})]^{1/2}$$

$$M_1^2 = \sum \chi_i^2 - M_2^2 - \mu^2 - 2Z$$

$$\tan \beta = [4w + (\chi_2 - \chi_1)(C_{2R} - C_{2L})]^{1/2} / [-]^{1/2}$$

Badr, Kalinowski  
Nojima et al, PRL

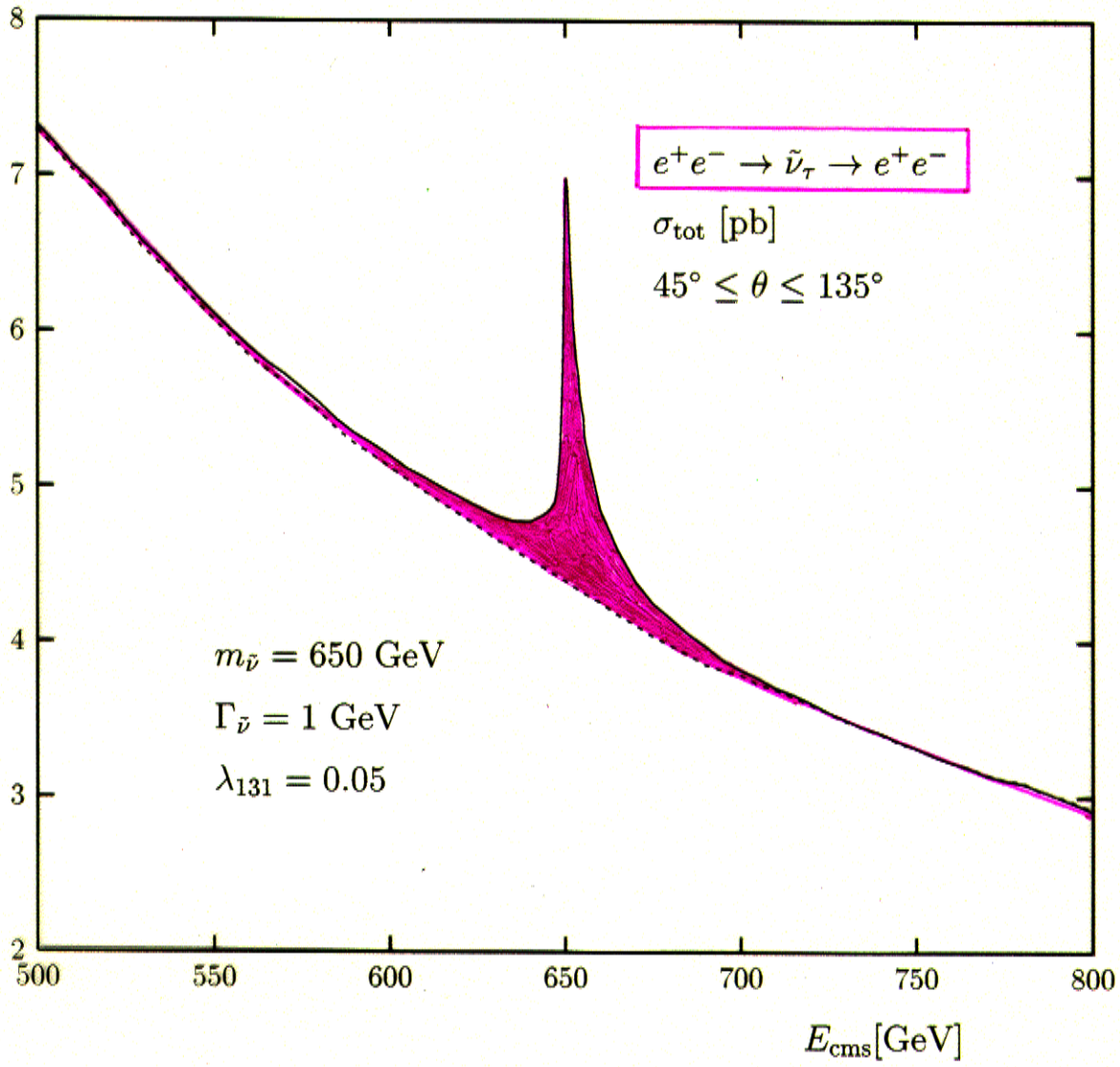
	measur. [RPR1]
$M_2$	$152 \pm 1.8 \text{ GeV}$
$M_1$	$72 \pm 3.2 \text{ GeV}$
$M_3$	$[452 \pm 10 \text{ GeV}]$
$\mu$	$316 \pm 0.9 \text{ GeV}$
$m_{0e}$	$237 \pm 0.1 \text{ GeV}$
$m_{0q}$	$460 \pm 0.6 \text{ GeV}$
$A_t$	$587 \pm 35 \text{ GeV}$
$\tilde{g}/g$	clus: 1 - 2%
$\tan \beta$	$3.0 \pm 0.7$

## SUSY BRKG MECH / RECONSTR. FUND. THEORY

physics potential: theor. unsolved most / need most fund. problem  
 clues on: gravity at small distances  
 extra space dimensions ...



RÜCKL  
SPIESBERGER  
et al.



realizations:

$m$  SUGRA

min supergravity

AMSB

$\tilde{g}$  MSB

gaugino med. SB

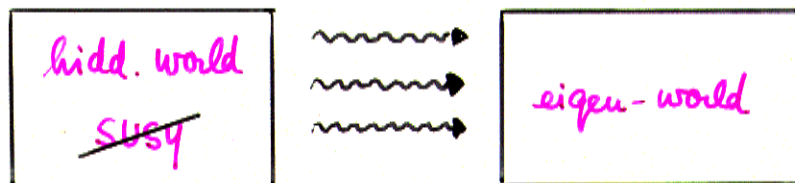
GMSB

gauge med. SB

SSSB

...

mechanisms:



$M_{PL} \sim 10^{19}$  GeV

$M_{M} \sim 10^6$  GeV

gravity  
gaugino  
gauge

(i) [Family] characteristic mass pattern:

Peskin

F

	gaugino $M_i$	scalar $m_f^2$
$m$ SUGRA	$\frac{\alpha_i}{\alpha_2} M_2$	$m_0^2 + \sum_i 2C_i \frac{\alpha_i^2 - \alpha_y^2}{b_i \alpha_2^2} M_2^2$
$\tilde{g}$ MSB	$\frac{\alpha_i}{\alpha_2} M_2$	without $m_0^2$ ✓
GMSB	$\frac{\alpha_i}{\alpha_2} M_2$	$\sum_i 2C_i \frac{\alpha_i^2}{\alpha_2^2} M_2^2$
AMSB	$\frac{b_i}{b_2} \frac{\alpha_i}{\alpha_2} M_2$	$\dots + \sum 2\eta_{fi} b_i \frac{\alpha_i^2}{\alpha_2^2} M_2^2$

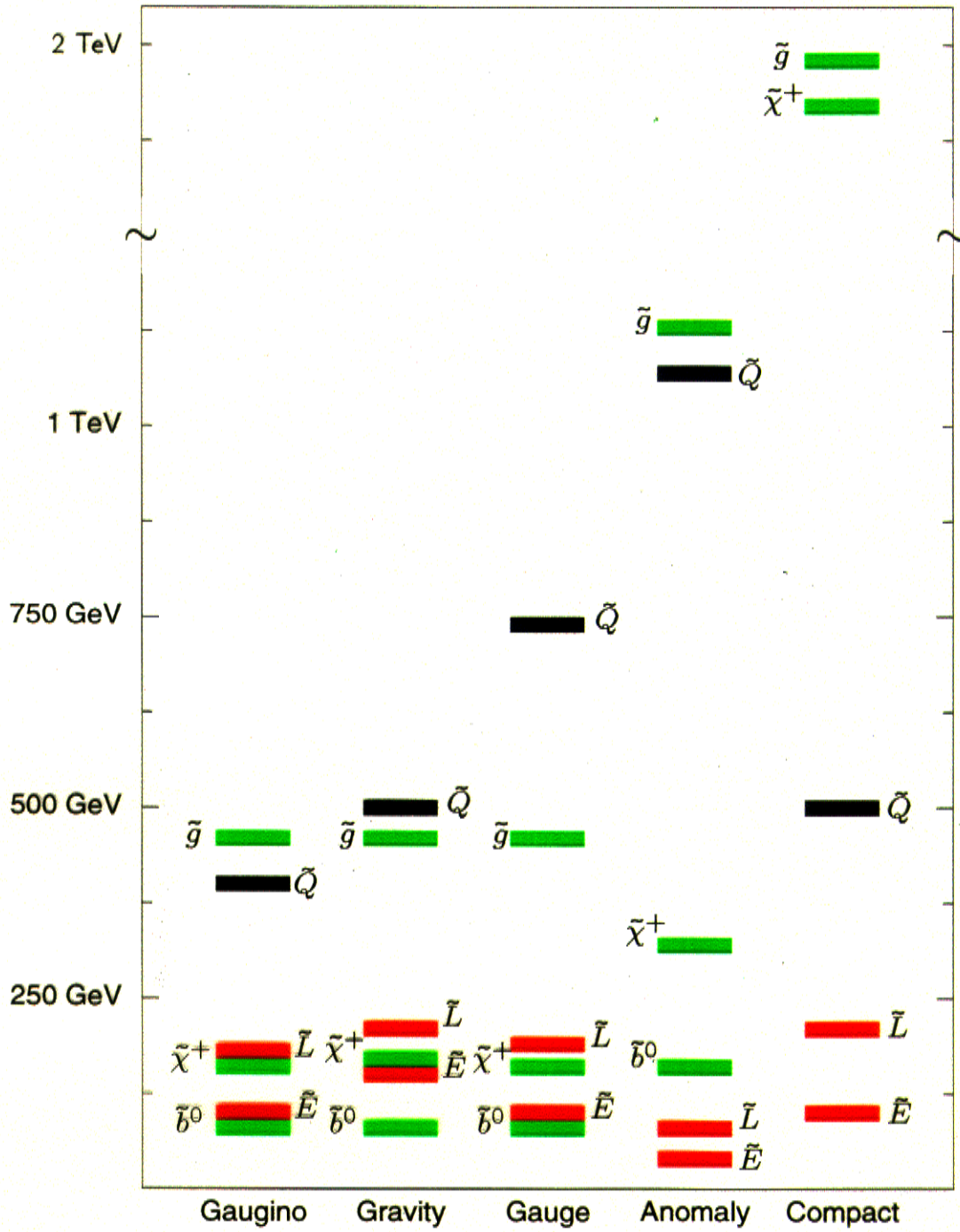
(ii) characteristic decay pattern:

Anthonio  
Gunion et al

GMSB :  $\tilde{\chi}_1^0 \rightarrow \gamma + \tilde{G} = \gamma + \cancel{E}$   
 $\tilde{\tau}_1 \rightarrow \tau + \tilde{G} = \tau + \cancel{E}$

AMSB :  $\tilde{\chi}_1^\pm \rightarrow \tilde{\chi}_1^0 + \gamma$   
 $\tilde{\chi}_1^\pm \rightarrow \tilde{\chi}_1^0 + \pi$  soft

*Peskin  
Prod. ea*



(iii) mSUGRA sum rules:

Tubano et al

F

masses decay modes production processes	}	5 parameters  <u><math>m_0, M_{1/2}, A_0, \tan\beta, \mu</math></u>
---	---	---

gaugino masses:  $M_1/M_2 = \frac{5}{3} \tan^2 \theta_w$

slepton/gaugino:  $m^2(\tilde{l}_L) - m^2(\tilde{l}_R) = \alpha M_{1/2}^2 - \frac{1}{2}(1-4s_w^2) C_{2F} M_2^2$

...

(iv) reconstruction of fund. SUSY theory:



bottom-up approach: much better discriminative  
 [ps - fix points]  
 than top-down [ $\sim$  LHC]

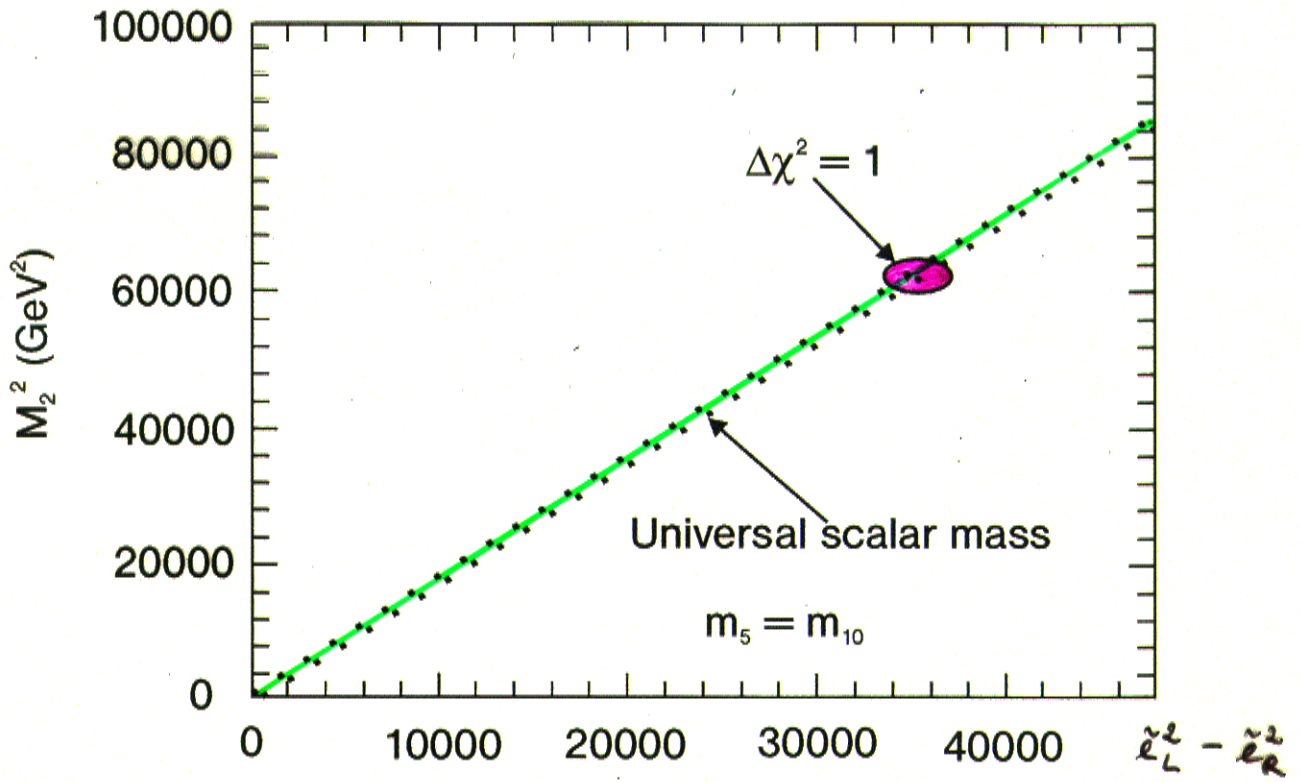
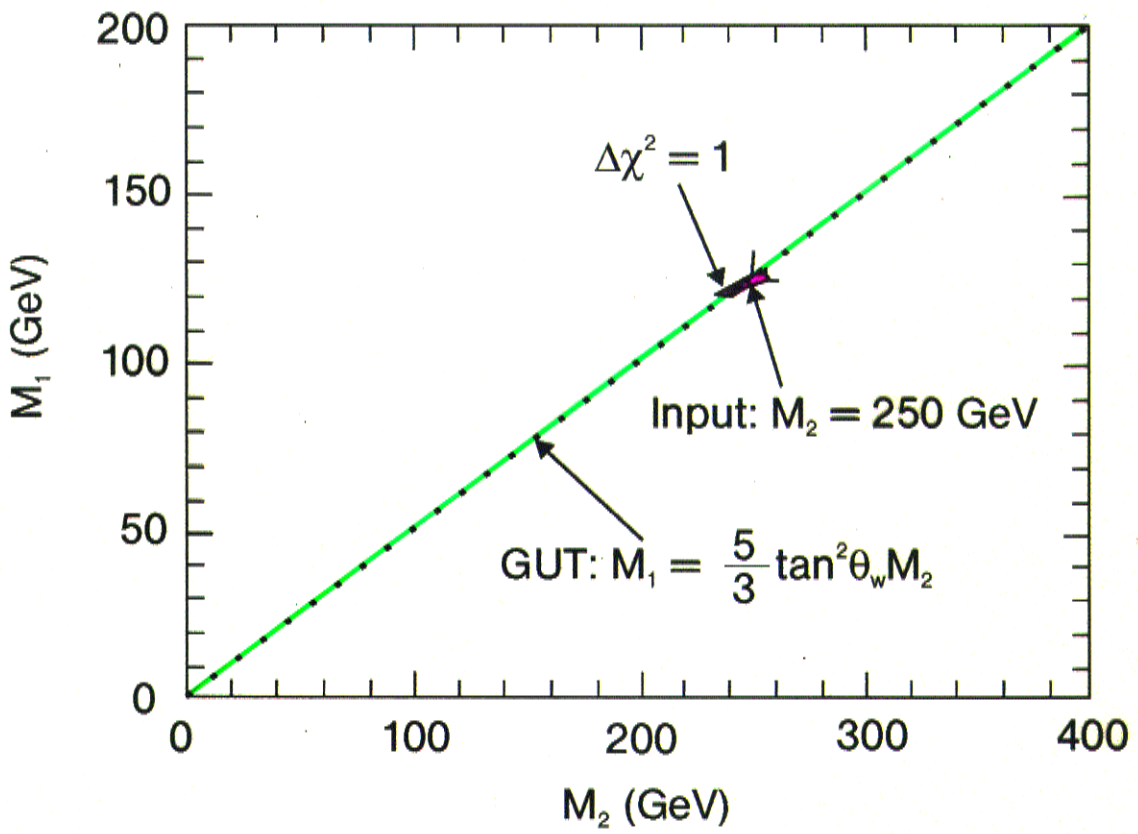
F: mSUGRA  $\rightarrow$   $\tilde{g}$ MSB  
 $\rightarrow$  GMSB

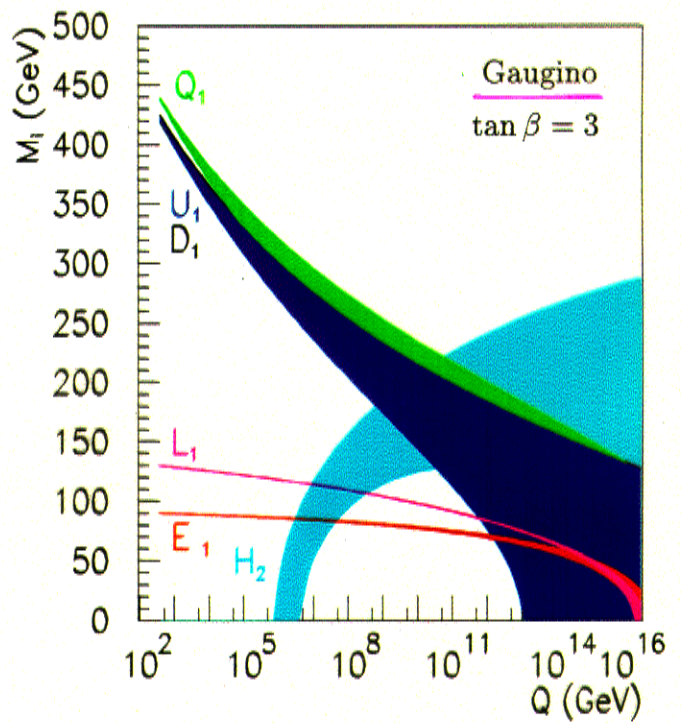
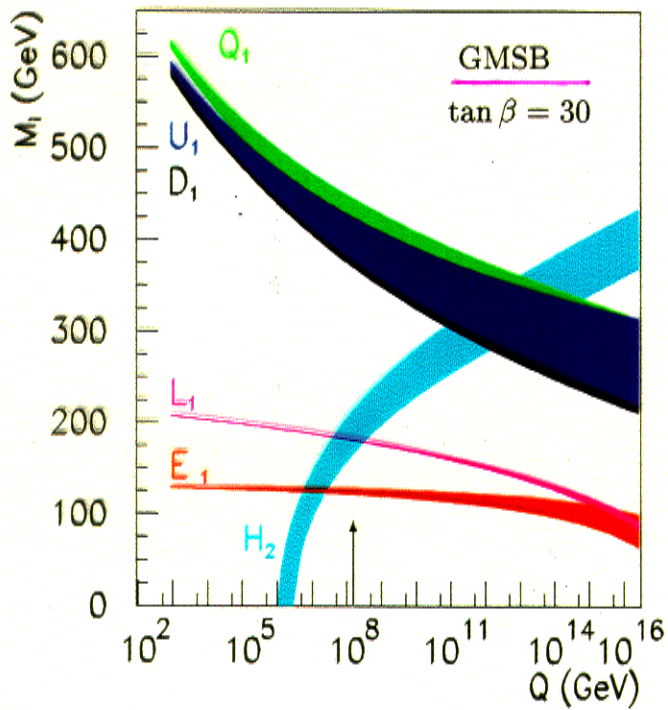
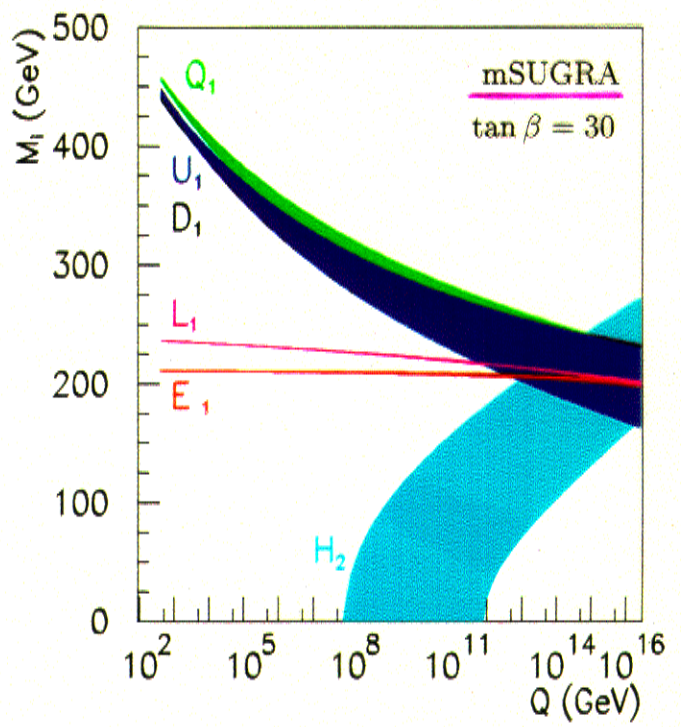
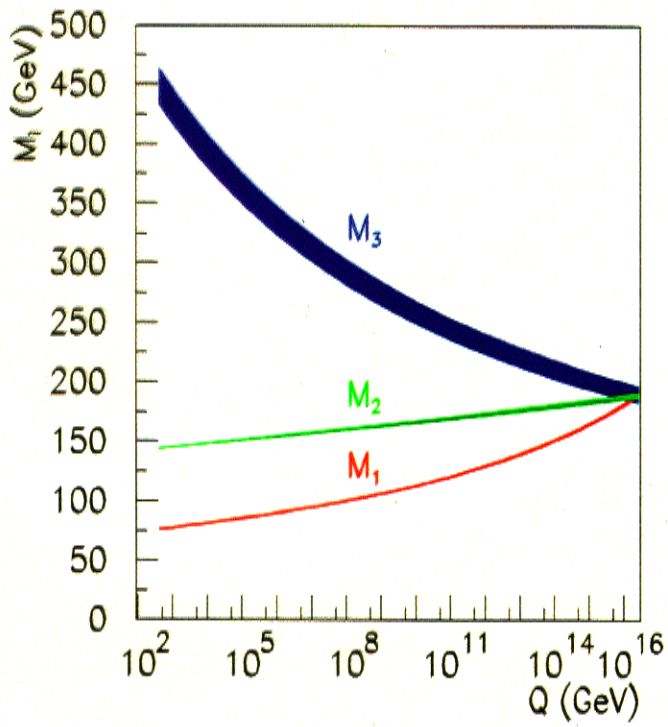
JLC/NLC/TESLA + CLIC  
 promise acc. results  
 at high scale

mSUGRA fit:

gaugino	$M_{1/2} = 200 \text{ GeV} \rightarrow 200.0 \pm 0.1 \text{ GeV}$
scalar	$m_0 = 160 \text{ GeV} \rightarrow 159.9 \pm 0.1 \text{ GeV}$

Tsukamoto et al





The high precision which can be achieved at  $e^+e^-$  colliders, opens perspectives on particle physics near the Planck scale.

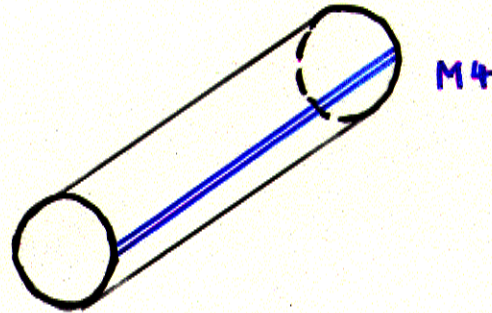
## 2c) EXTRA SPACE DIMENSIONS

Arkani-Hamed

- Motivation:
- consistency of string/M theory
  - $u \sim$  - unification GUT + gravity
  - removing hierarchy problem

### space-time structure:

compactified dimensions:  
 $M_S^{n+2} R^n = M_{PL}^2$

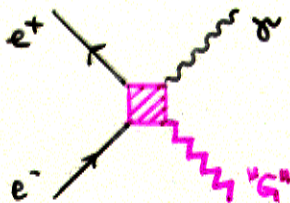


### The maxi / midi / mini parade:

maxi:  $M_S \sim \text{TeV}$      $R \sim \mu\mu \dots \mu\mu \dots$      $\therefore$  gravity in bulk

(i) missing  $E$ :  $e^+e^- \rightarrow \gamma + 'G(m)' = \gamma + E$

Peskin

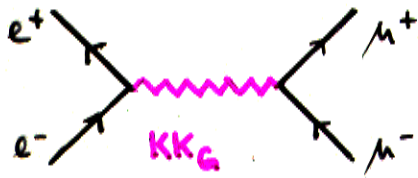


$n$	LHC / -2	J/N/T	CLIC
[2]	12.5 / <25>	7.7 TeV	<40 TeV>
4	7.5 / <15>	4.5 TeV	<22 TeV>
6	6 / <12>	3.1 TeV	<16 TeV>

(ii) Kaluza-Klein CI:

$e^+e^- \rightarrow f\bar{f}$

Hewett



contact interactions spin = 2

sensitivity  $M_s \sim 8 \rightarrow 40 \text{ TeV}$

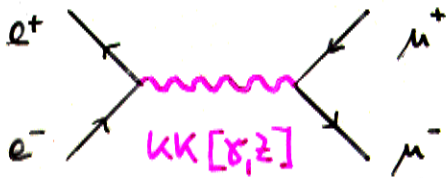
$\gamma\gamma \rightarrow W^+W^- : 12 \text{ TeV}$

Rizzo

mid:  $M_s \sim 10^7 \text{ GeV}$   $R \sim \text{TeV}^{-1}$  :: gauge field in bulk

KK gauge towers:

Antoniadis



JNT : spin 1 CI

CLIC : RESON. PEAK

F

mini:  $M_s \in M_{PL}$   $R \gtrsim M_{PL}^{-1}$  :: gravity in bulk

RS: loc. gravity on 2nd brane

graviton towers:

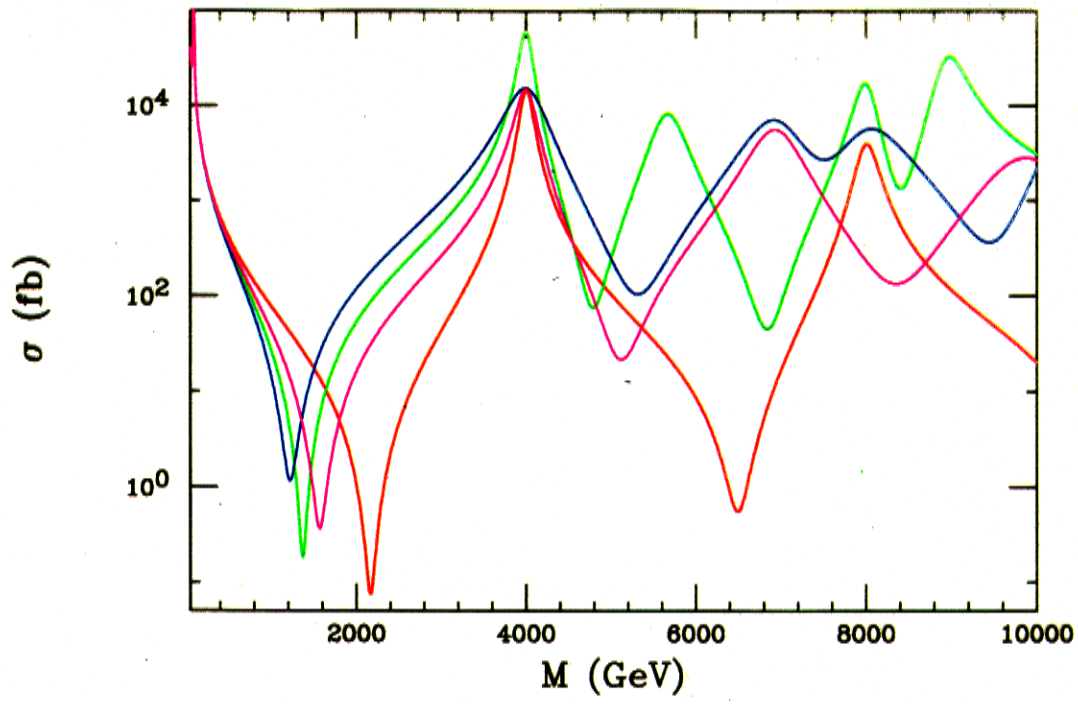
RESON. PEAK'S

F

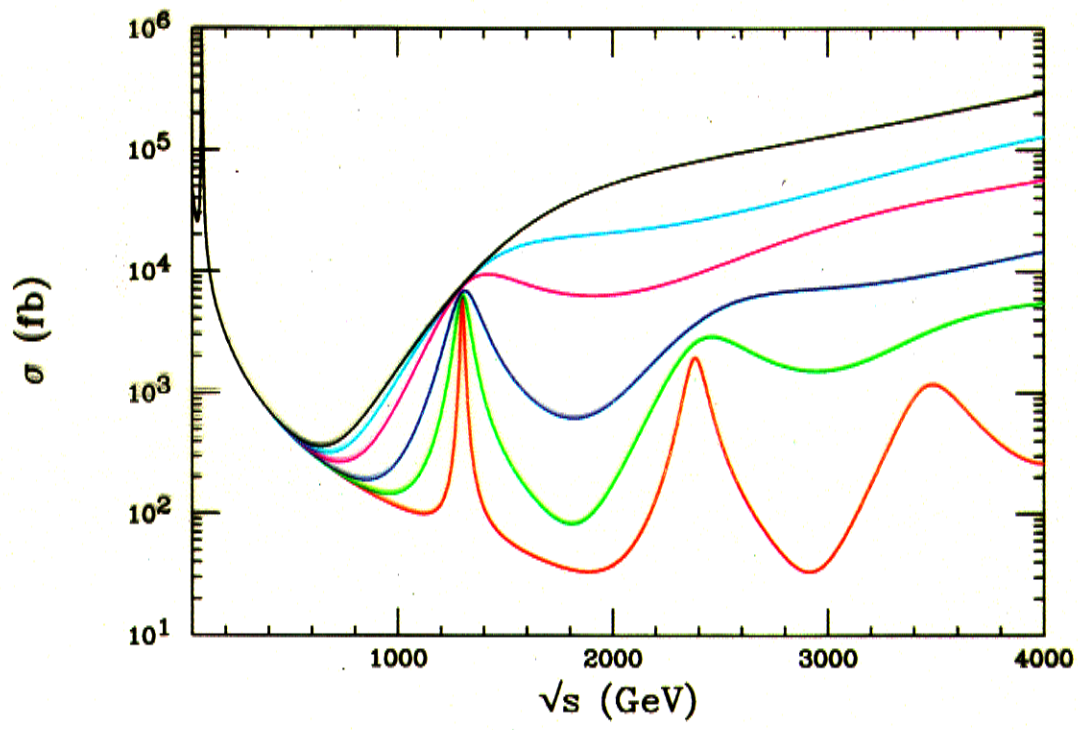
Rizzo

Through angular distributions, JLC/NLC/TESLA can give valuable information on physical nature of KK towers; CLIC goes to maximum limits.





Cross section for the process  $e^+e^- \rightarrow \mu^+\mu^-$  for several models with  $d = 2$  assuming  $M_1 = 4$  TeV. The red(green,blue,purple) curve corresponds to the  $S^1/Z_2(Z_2 \times Z_2, Z_{3,6}, S^2)$  compactifications.

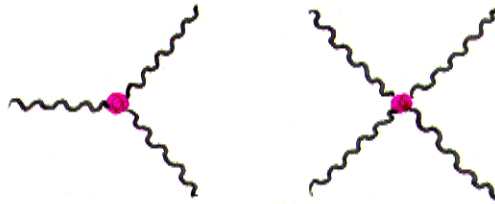


Cross section for  $e^+e^- \rightarrow \mu^+\mu^-$  including the exchange of KK gravitons, taking the mass of the first mode to be 1.3 TeV, as a function of energy. From top to bottom the curves correspond to  $c=1.0, 0.7, 0.5, 0.3, 0.2, 0.1$ .

### 3a) GAUGE THEORIES

a) SM = SU<sub>3</sub> × SU<sub>2</sub> × U<sub>1</sub> : forces are mediated by abelian and non-abelian gauge fields

SU<sub>2</sub> × U<sub>1</sub> self-interactions :



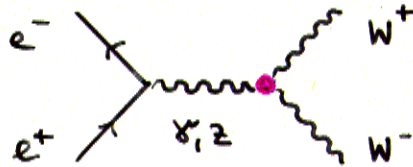
SM deviation  
 $\Delta \sim M_W^2 / \Lambda_*^2$

→ elw static param. :  
 $\mu_{W^+W^-}$  etc

monopole charge :  $e$   
 magn. dipole mom. :  $2 \times e / 2 M_W$   
 el. quadrip. mom. :  $-e / M_W^2$

Measurement:

$$\Delta G/G \sim \Delta \times g^2$$



LC500 :  $\alpha, \lambda$   
 $\Delta < 2-3 \times 10^{-4}$

F

### b) EXTENDED GAUGE SYMMETRIES

$$E_6 \rightarrow SO_{10} \times U_1 \rightarrow SU_5 \times U_1 \times U_1$$

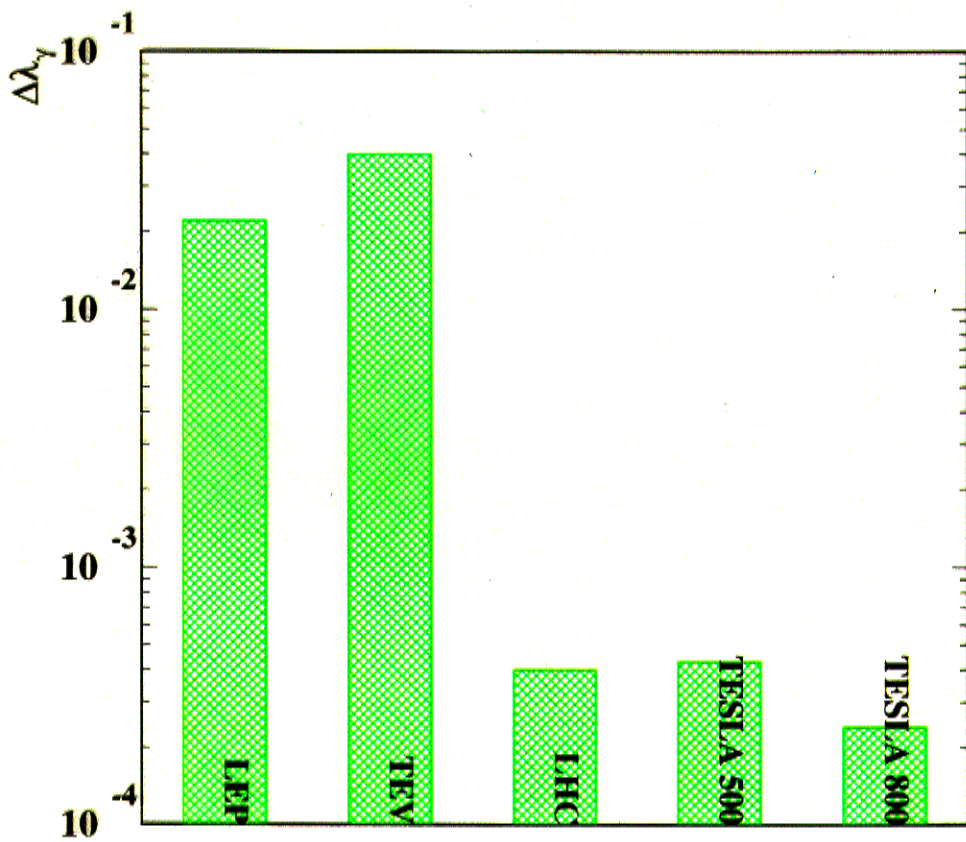
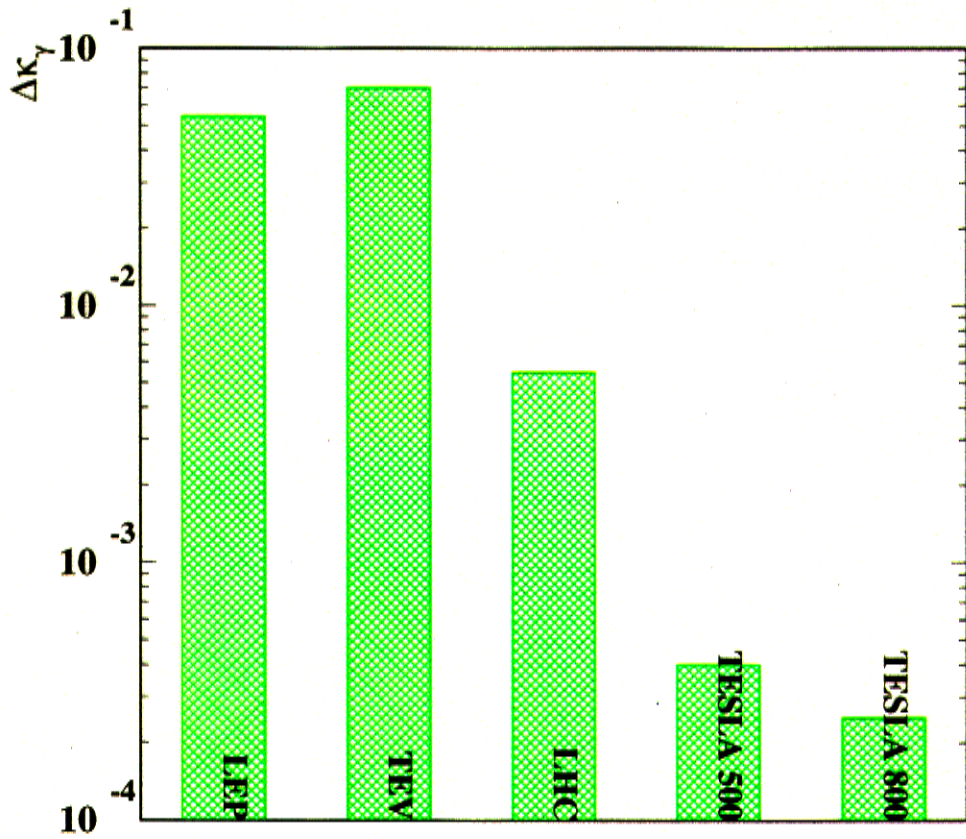
$$\rightarrow SU_3 \times SU_2 \times U_1 \times U_1'$$

•  $Z'$  with mass  $M(Z') \sim \Theta(\text{TeV})$

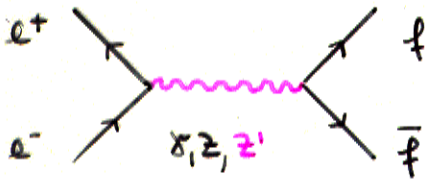
• 27 plet :

$\begin{bmatrix} \nu_e \\ e^- \end{bmatrix}_L$	$\nu_{eR}$ $e^-_R$	$\begin{bmatrix} N_E \\ E^- \end{bmatrix}_L$	$\begin{bmatrix} N_E \\ E^- \end{bmatrix}_R$	$m_{eL}$
$\begin{bmatrix} u \\ d \end{bmatrix}_L$	$u_R$ $d_R$	$D_L$	$D_R$	

*Höning et al.*



new gauge boson  $Z'$ :



$\sqrt{s}$	$E(6)$
500 GeV	5-7 TeV
800 GeV	8-11 TeV
5 TeV	$\sim 50$ TeV

LHC-2 :  $M_{Z'} \sim 5/10$  TeV

CHARGES :  
F

LC allows for measurement of  $U(1)'$  charges and opens sensitivity window to  $Z'$  masses in multi-TeV range.

c) QCD : running coupling  $\alpha_s(Q)$

"half-way to infinity"

$$\Delta \alpha_s(M_{Z'}^2) \rightarrow 0.001$$

...

F

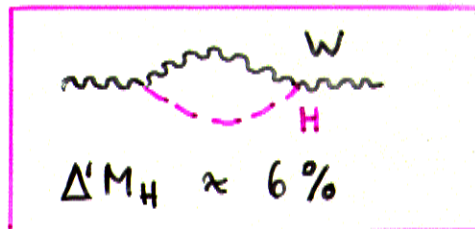
d) giga Z :  $2 \times 10^9$  Z bosons  $\sim 100 \times$  LEP1  
polarized  $e^+$  and  $e^-$  beams

moving

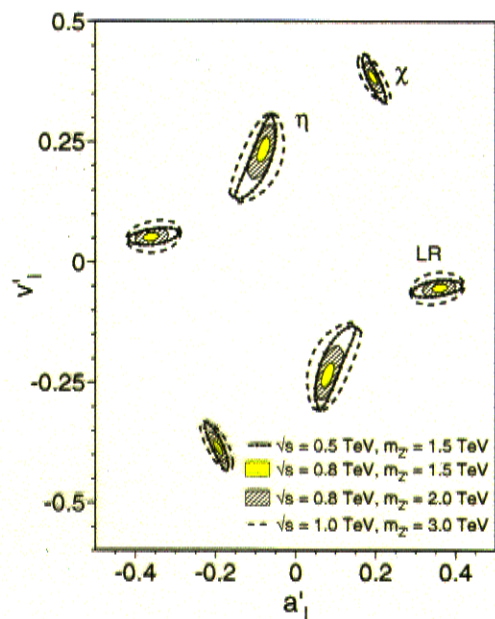
LR asymmetry : 
$$A_{LR} = \frac{2(1-4s_e^2)}{1+(1-4s_e^2)^2}$$

$$\Delta \sin^2 \theta_{eff,e} \approx 1 \times 10^{-5}$$

loop test of the Higgs field :



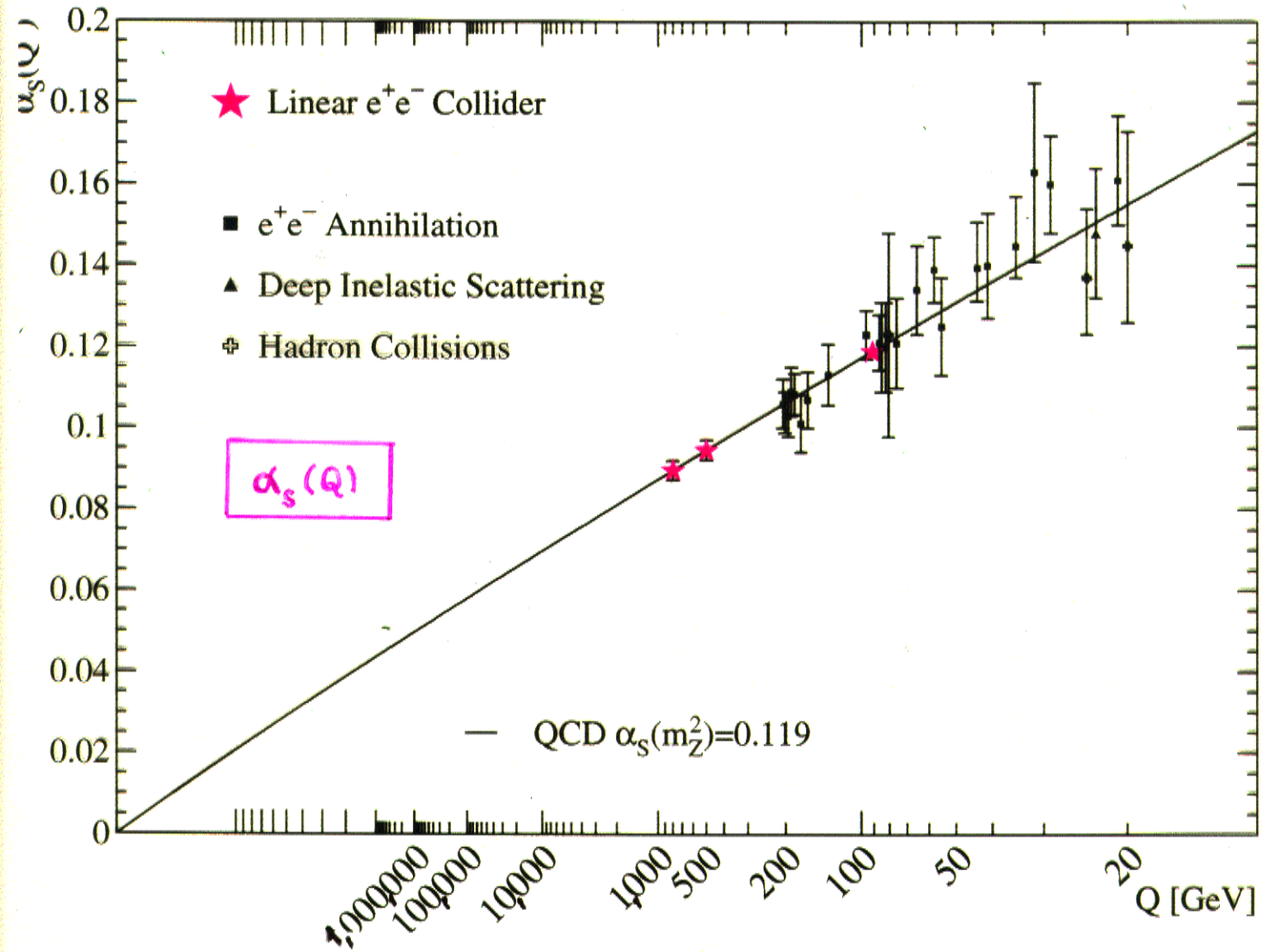
$$\Delta M_H \approx 6\%$$



Riemann

Figure 9: Resolution power for different  $m_{Z'}$  (95% CL) based on measurements of leptonic observables at  $\sqrt{s}=500 \text{ GeV}, 800 \text{ GeV}, 1 \text{ TeV}$  with a luminosity  $\mathcal{L}_{int} = 1000 \text{ fb}^{-1}$ . The leptonic couplings of the  $Z'$  correspond to the  $\chi, \eta$  or LR model.

Bethke  
Siebel



### 3.8) TOP QUARK

high-precision measur. of  $t$  properties: *mass*  
*stat. ehs param.*  
*decay parameters*

→ test of ehs symmetry brkg at qm level

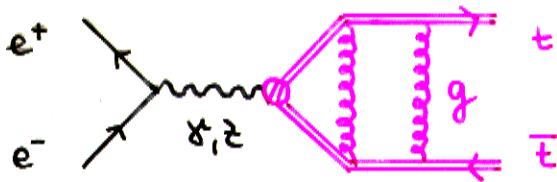
$$G_F, M_Z, \sin^2 \theta_W; M_t \rightarrow M_H$$

→  $M_t \sim v/\sqrt{2}$  maximal mass in SM fermion sector:

key rôle in flavor dynamics, ...

$M_t$

max precision:  $e^+e^- \rightarrow t\bar{t}$  excitation curve  
 near threshold



$$\Gamma_{t\bar{t}} \sim \beta_t \sim \sqrt{s - 4M_t^2}$$

⊖ width

⊕  $q$  ladders

F

Sumino  
Huang et al

$$\Delta M_t \lesssim 200 \text{ MeV}$$

$$\Delta M_t / M_t \lesssim 1\%$$

F

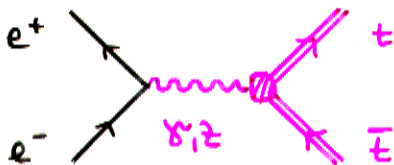
most precise mass in  $q$  sector

$$\Delta \Gamma_t / \Gamma_t \lesssim 0.05 \quad \text{S-P interf}$$

$$t\bar{t}g_{IR}$$

Klein  
on  
Orn

ELW



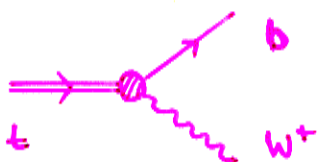
$$\text{mag. dipole mom.} \lesssim 1.1 \times 10^{-2}$$

$$\text{el. dipole mom.} \lesssim 4 \times 10^{-19} \text{ ecm}$$

Beunhler

Michel parameter:

$$V+A / V-A \lesssim 1.2 \times 10^{-2}$$



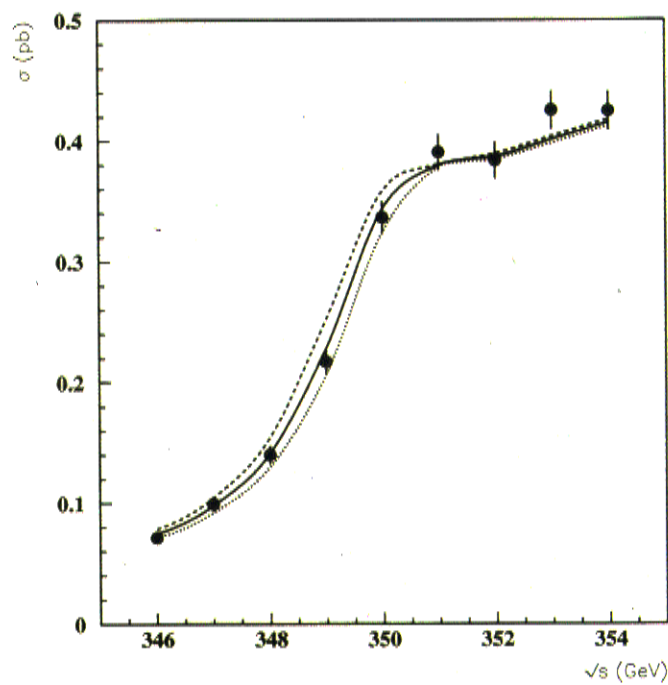


Figure 3.3.3: Excitation curve of  $t\bar{t}$  quarks including initial-state radiation and beamstrahlung [21]. The errors of the data points correspond to an integrated luminosity of  $\int \mathcal{L} = 100 \text{ fb}^{-1}$ . The dotted curves indicate shifts of the top mass by  $\pm 100$  MeV.



## 4. CONCLUSIONS

### 1.) Higgs mechanism and electroweak symmetry breaking

- essential elements of Higgs mechanism can be established;
- strong WW interactions can be studied throughout threshold region:  $\sqrt{s} \sim 3 \text{ TeV}$  at 500 GeV; at 5 TeV deep in resonance region;

### 2.) Supersymmetry

- spectrum can be analyzed comprehensively  $\sim 1 \text{ TeV}$ , method robust;
- SUSY breaking mechanism analyzed experimentally;
- reconstruction of fundam. theory at scale  $\sqrt{E} \sim M_{\text{Pl}}$  where particle physics  $\sim$  gravity;

### 3.) Extra space dimensions

- structure of space-time probed experimentally at short distances;

#### 4.) EW and Strong gauge theories

- non-abelian gauge symmetries of forces established at high accuracy;
- extended gauge symmetric theories can be explored in detail, at 5 TeV window to  $\sim 50$  TeV;

#### Top quark

- profile of key element to flavor physics can be studied with high precision

all phases of an  $e^+e^-$  linear collider project

$$\sqrt{s} = 500 \text{ GeV} / 1 \text{ TeV} // 5 \text{ TeV}$$

promise new deep insight into microscopic physics