

Testing Higgs self-couplings at the LC

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Outline

- Motivation
- Self-couplings of the SM Higgs particle
- Self-couplings of the MSSM Higgs particles
- Conclusions

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Motivation

Higgs mechanism production of masses via spontaneous symmetry breaking (SSB)

- ▶ particles acquire their masses through the interaction with a scalar field
- ▶ self-interaction of the scalar field \leadsto non-zero field strength in the ground state \leadsto SSB
- ▶ $v = 246 \text{ GeV} \neq 0$ induced by the typical form of the Higgs potential
- ▶ weak iso-doublet scalar field $\xrightarrow{\text{SSB}}$ Higgs particle

How to establish the Higgs mechanism experimentally?

- (I) Discovery of the Higgs particles
 \Downarrow
- (II) Yukawa and gauge couplings
 \Downarrow
- (III) Determination of the Higgs self-couplings
 \Downarrow

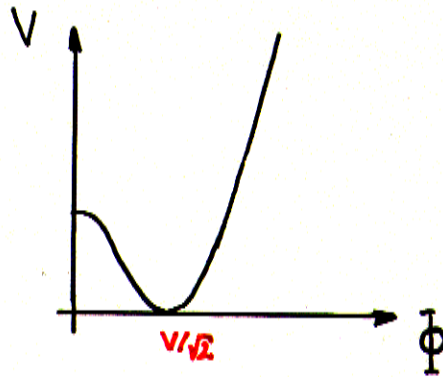
Experimental verification of the creation of particle masses via the Higgs mechanism

Standard Model

$$V(\Phi) = \lambda \left(\Phi^\dagger \Phi - \frac{v}{2} \right)^2$$

$$v = 246 \text{ GeV}$$

$$\Phi = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v+H \end{pmatrix} \sim$$



$$V(H) = \frac{1}{2} M_H^2 H^2 + \frac{M_H^2}{2v} H^3 + \frac{M_H^2}{8v^2} H^4$$

Higgs mass

$$M_H = \sqrt{2\lambda} v$$

trilinear Higg self-coupling

$$\lambda_{HHH} = 3M_H^2 / M_Z^2$$



quadrilinear Higgs self-coupling:

$$\lambda_{HHHH} = 3M_H^2 / M_Z^4$$



(units $\lambda_0 = 33.8 \text{ GeV} / \lambda^2$)

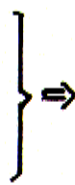
(a) trilinear coupling:

via Higgs pair production

(b) quadrilinear coupling:

via triple Higgs production

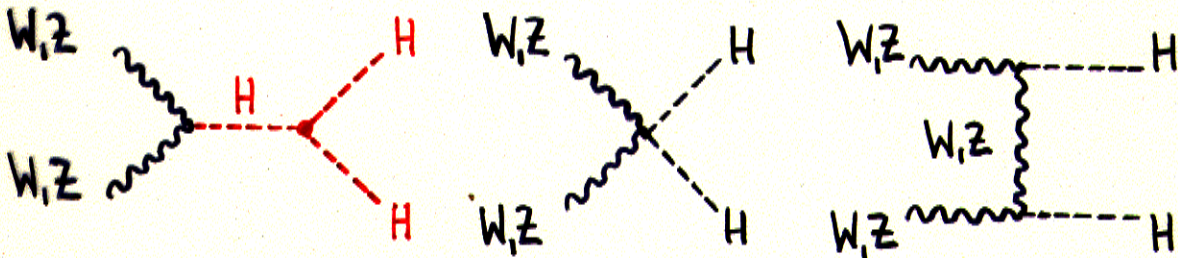
measurement of the Higgs self-couplings
and
reconstruction of the Higgs potential



establish the scalar
sector of the **Higgs mechanism**
experimentally

Determination of the trilinear Higgs coupling

WW-(ZZ-) fusion



Independent helicity amplitudes

$$\hat{d}_{LL} = \frac{2\sqrt{2}G_F M_W^2}{(1-\beta_W^2)} \left\{ (1+\beta_W^2) \frac{\lambda_{HHH}}{(\hat{s}-M_H^2)/M_Z^2} + (1+\beta_W^2) + \frac{1}{\beta_W \beta_H} \left[\frac{1-\beta_W^4 + (\beta_W - \beta_H x)^2}{x-x_W} + (x \rightarrow -x) \right] \right\}$$

$$\hat{d}_{LT} = \frac{G_F \sqrt{M_W^2 (1-x^2)} \hat{s}}{\beta_W} \left[\frac{\beta_H x - \beta_W}{x-x_W} - (x \rightarrow -x) \right]$$

$$\hat{d}_{+-} = \frac{\sqrt{2}G_F M_W^2 \beta_H (1-x^2)}{\beta_W} \left[\frac{1}{x-x_W} + (x \rightarrow -x) \right]$$

$$\hat{d}_{++} = 2\sqrt{2}G_F M_W^2 \left\{ \frac{\lambda_{HHH}}{(\hat{s}-M_H^2)/M_Z^2} + 1 + \frac{1}{2\beta_W \beta_H} \left[\frac{(1-x^2)\beta_H + 8M_W^2/\hat{s}}{x-x_W} + (x \rightarrow -x) \right] \right\}$$

$$x = \cos\theta, x_W = (1-2M_H^2/\hat{s})\beta_H/\beta_W, \beta = (1-4M_W^2/\hat{s})^{1/2}$$

high energy limit:

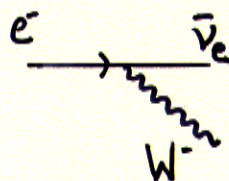
$$\hat{\sigma}_{LL} \rightarrow \hat{\sigma}_{\infty} = \frac{M_W^2 G_F^2}{2\pi} \sim \text{constant}$$

$$\hat{\sigma}_{LT} \rightarrow \frac{M_H^2}{2\hat{s}} \frac{M_H^2 - 2M_W^2}{\hat{s}} \left[\ln \frac{\hat{s}}{M_H^2} - 3 \right] \sim \text{scaling mod } \ln \hat{s}$$

$$\hat{\sigma}_{\pi\pi} \rightarrow \frac{M_H^2}{4\hat{s}} \hat{\sigma}_{\infty} \sim \text{scaling}$$

Process $e^+e^- \rightarrow W^+W^- \rightarrow \bar{\nu}_e \nu_e HH$

Equivalent particle approximation: W bosons partons in e^+e^- , W bosons on-shell



W_L-spectrum : $f_{W/e}^L(x) = \frac{g^2}{16\pi^2} \frac{1-x}{x}$ high-energy limit

Kanz, ...
Jankin

$x = E_W/E_e$

Cross section for the process $e^+e^- \xrightarrow{WW} \bar{\nu}_e \nu_e HH$:

$$\sigma = \int \frac{1}{4M_W^2/s_{ee}} d\tau \left(\frac{d\mathcal{L}}{d\tau} \right)_{WW/ee} \hat{\sigma}_{WW \rightarrow HH}(\hat{s} = \tau s_{ee})$$

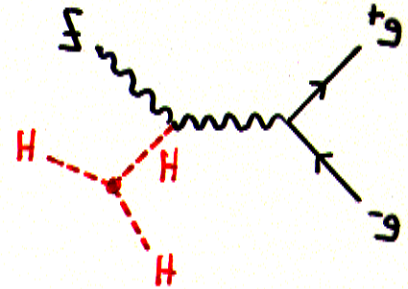
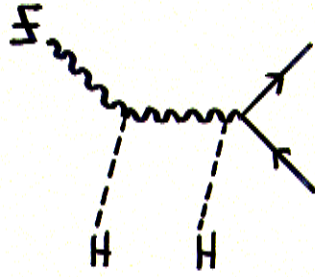
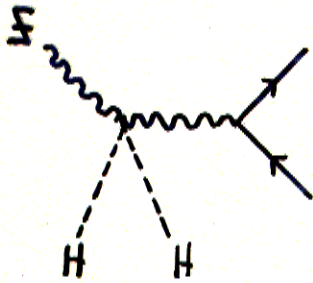


$$\left(\frac{d\mathcal{L}}{d\tau} \right)_{WW/ee} = \int \frac{1}{\tau} \frac{dx_2}{x_2} f_{W/e}(x_2) f_{W/e}\left(\frac{\tau}{x_2}\right)$$

High energy limit:

$$\sigma_{\infty}(e^+e^- \xrightarrow{WW} \bar{\nu}_e \nu_e HH) \approx \left(\frac{\alpha}{4\pi \sin^2 \theta_W} \right)^2 \left[\frac{1}{2} \ln^2 \left(\frac{4M_H^2}{s_{ee}} \right) + 2 \ln \left(\frac{4M_H^2}{s_{ee}} \right) + 3 \right] \hat{\sigma}_{\infty}$$

Double Higgs-strahlung in e⁺e⁻ collisions



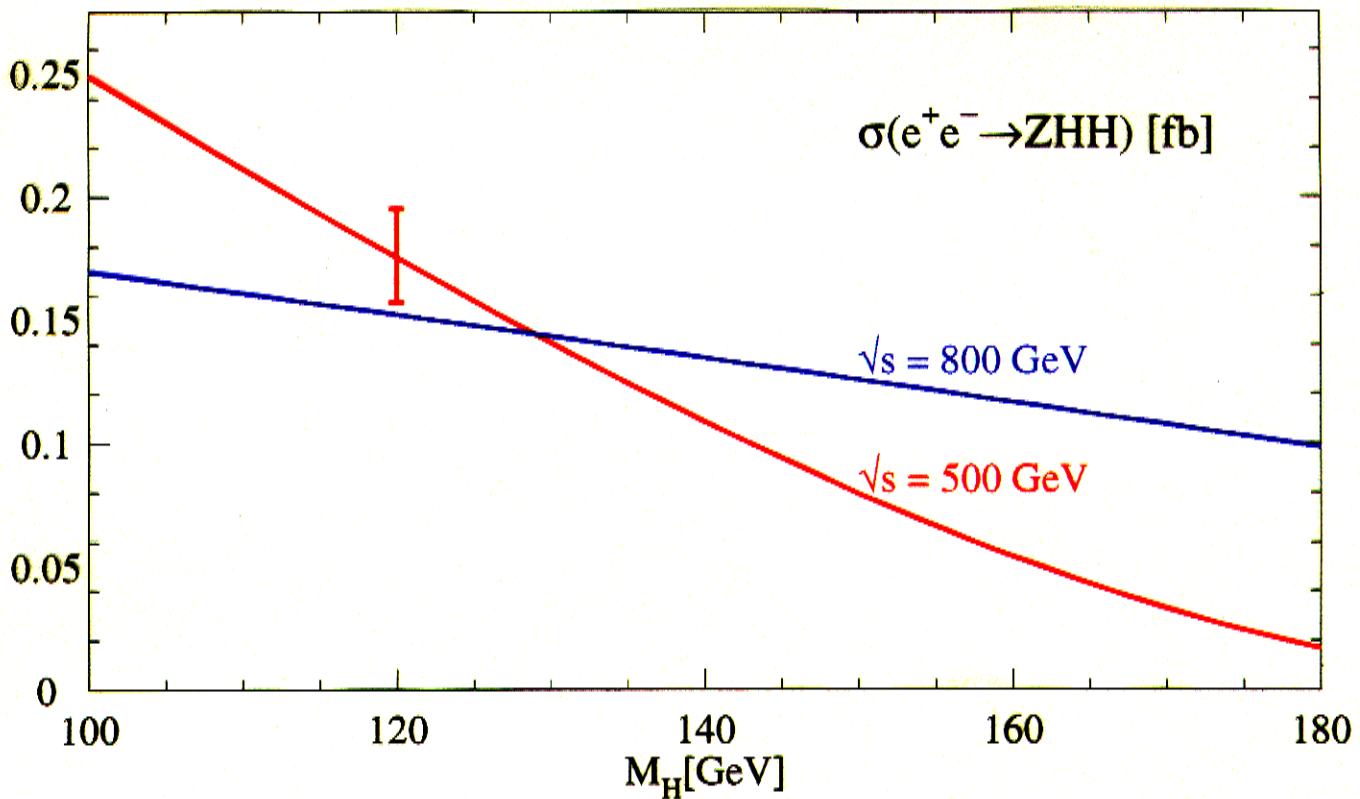
$$\sqrt{s_{HHH}} \left\{ \frac{M_Z^2 [(\gamma + \gamma')^2 + 8\gamma^2]}{4s^2 [1 + x + x^2 + \frac{1}{s}]} \right\} \frac{1}{(s - M_Z^2)} \frac{(2M_Z^2 (\gamma^2 + \gamma'^2))}{2s^2 \sqrt{s} \pi^2} = \frac{d\sigma(e^+e^- \rightarrow e^+e^- H H)}{d\Omega dx^2}$$

+ radiation contributions

+ interference terms ($\sim \sqrt{s_{HHH}}$)

$$x^2 = M_Z^2, \quad E = \sqrt{s} \\
 \sqrt{s} = M_Z^2$$

SM double Higgs-strahlung: $\sqrt{s} = 500 \text{ GeV}, 800 \text{ GeV}$



- ▶ $\sigma \sim 0.02 \dots 0.25 \text{ fb} \approx 40 \dots 500 \text{ events for } \int \mathcal{L} = 2000 \text{ fb}^{-1}$
- ▶ polarized e^+, e^- beams $\sim \sigma^{\text{pol}} = 2\sigma^{\text{unpol}}$
- ▶ σ shows scaling behaviour
- ▶ I variation of $\sigma(ZHH)$ for $\Delta\lambda/\lambda = 0.2$
- ▶ $\sqrt{s} = 500 \text{ GeV}$ good choice for $M_H = 120 \text{ GeV}$: σ large
sensitivity to λ_{HHH} large

Final states and background

- Final states:
- (i) $M_H \lesssim 140 \text{ GeV}$: $Zb\bar{b}b\bar{b}$
 - (ii) $M_H \gtrsim 140 \text{ GeV}$: ZWW^*WW^*

For $M_H \lesssim 140 \text{ GeV}$:

Miller, Moretti

▷ Parton level analysis: background under control but signal rates are small.

$$[M_H = 110 \text{ GeV}, \sqrt{s} = 500 \text{ GeV}, \int \mathcal{L} = 1 \text{ ab}^{-1} : N_S = 26, N_B = 1]$$

▷ Hadron level analysis → talk by P. Gay

Quadrilinear coupling λ_{HHHH}

processes involving λ_{HHHH}

triple Higgs-strahlung : $e^+e^- \xrightarrow{Z^*} ZHHH$

WW triple Higgs fusion : $e^+e^- \xrightarrow{WW} \bar{\nu}_e \nu_e HHH$

however: $\sigma_{HHH} \approx 10^{-3} \sigma_{HH}$ because

- ▷ quadrilinear coupling is suppressed with respect to the trilinear coupling
- ▷ one more particle in the final state

Quadrilinear coupling not measurable for the time being.

MSSM

Supersymmetry + no anomaly \Rightarrow 2 complex Higgs doublets

5 physical states:

$$h \quad : \quad M_h \approx 135 \text{ GeV}$$

$$H, A, H^\pm \quad : \quad M_i = \mathcal{O}(v) \dots 1 \text{ TeV}$$

Haber...
 Carena...
 Zhang...
 Heinemeyer...

6 CP-invariant neutral trilinear Higgs couplings

trilinear Born couplings

one-loop leading m_t^4 -approximation

$$\lambda_{hhh} = 3 \cos 2\alpha \sin(\beta + \alpha) + 3 \frac{\epsilon}{M_Z^2} \frac{\cos \alpha}{\sin \beta} \cos^2 \alpha$$

$$\lambda_{Hhh} = 2 \sin 2\alpha \sin(\beta + \alpha) - \cos 2\alpha \cos(\beta + \alpha) + 3 \frac{\epsilon}{M_Z^2} \frac{\sin \alpha}{\sin \beta} \cos^2 \alpha$$

$$\lambda_{HAh} = -2 \sin 2\alpha \cos(\beta + \alpha) - \cos 2\alpha \sin(\beta + \alpha) + 3 \frac{\epsilon}{M_Z^2} \frac{\cos \alpha}{\sin \beta} \sin^2 \alpha$$

$$\lambda_{HHH} = 3 \cos 2\alpha \cos(\beta + \alpha) + 3 \frac{\epsilon}{M_Z^2} \frac{\sin \alpha}{\sin \beta} \sin^2 \alpha$$

$$\lambda_{hAA} = \cos 2\beta \sin(\beta + \alpha) + \frac{\epsilon}{M_Z^2} \frac{\cos \alpha}{\sin \beta} \cos^2 \beta$$

$$\lambda_{HAA} = -\cos 2\beta \cos(\beta + \alpha) + \frac{\epsilon}{M_Z^2} \frac{\sin \alpha}{\sin \beta} \cos^2 \beta$$

$$\tan \beta = v_2 / v_1$$

Radiative corrections one-loop leading m_t^4 approximation parametrized by

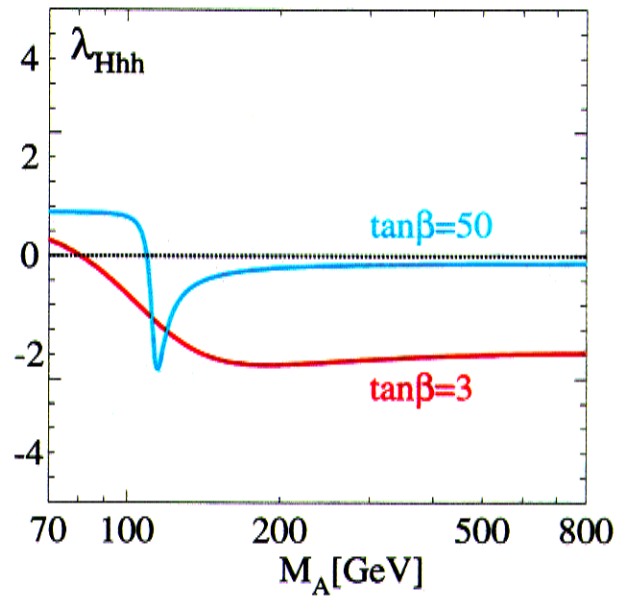
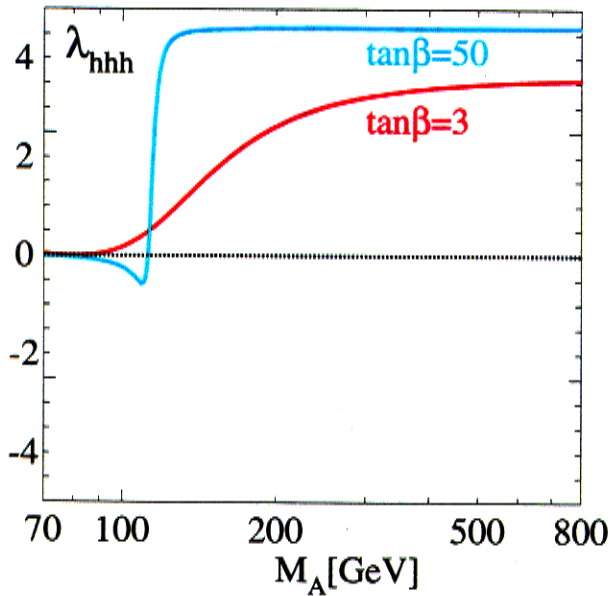
$$\epsilon \approx \frac{3 G_F m_t^4}{\sqrt{2} \pi^2 \sin^2 \beta} \ln \left(1 + \frac{M_S^2}{m_t^2} \right)$$

Trilinear couplings $\lambda_{hhh}, \lambda_{Hhh}$

Carena, Quiros, Hagner
Carena, Espinosa, Quiros, Hagner
Djouadi, Kalinowski, Spira

subsequent analysis: dominant one-loop and two-loop corrections to MSSM Higgs masses and couplings
 corrections involve mixing parameters A and μ

$\lambda_{hhh}, \lambda_{Hhh}$ (no mixing):



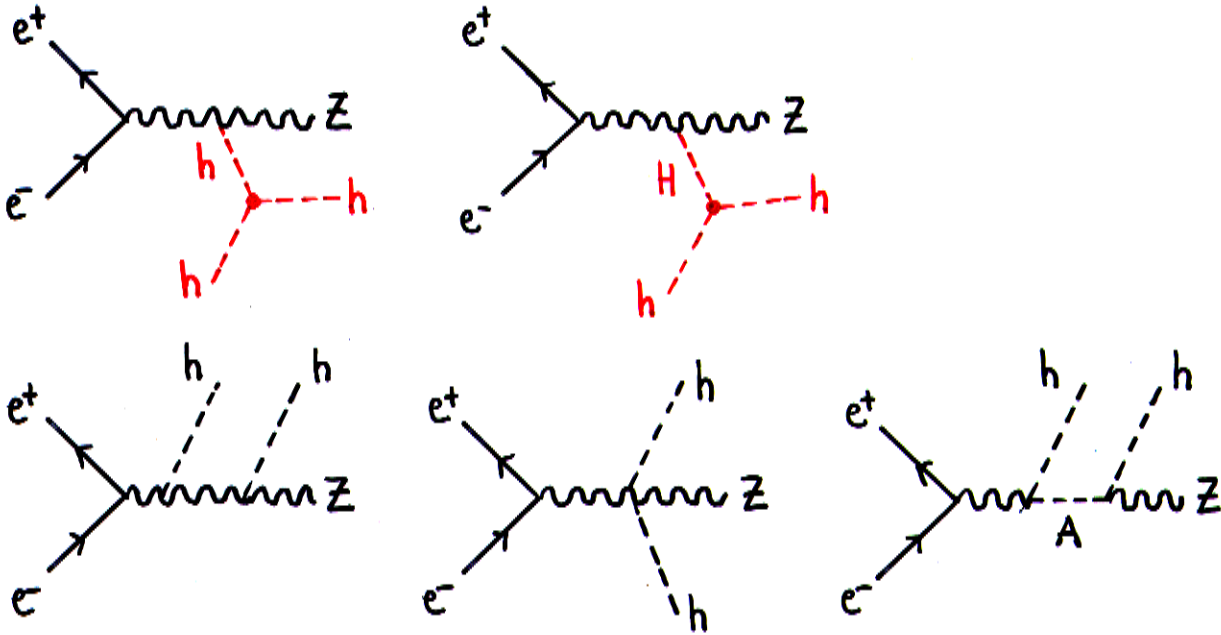
Note: $\lambda_{hhh}, \lambda_{Hhh}$ can become zero

Determination of the trilinear Higgs couplings

Example: hh final state

(i) WW/ZZ fusion

(ii) double Higgs-strahlung $e^+e^- \rightarrow Zhh$:



$$\frac{d\sigma(e^+e^- \rightarrow Zhh)}{dx_1 dx_2} = \frac{G_F^3 M_Z^6 (v_e^2 + a_e^2)}{384 \sqrt{2} \pi^3 s} \frac{1}{(1 - \mu_Z)^2} \left\{ \frac{M_Z^2 [(y_1 + y_2)^2 + 8\mu_Z]}{4s} * \right.$$

$$\left[\frac{\sin(\beta - \alpha)}{y_3 + \mu_Z - \mu_h} \lambda_{h h h} + \frac{\cos(\beta - \alpha)}{y_3 + \mu_Z - \mu_H} \lambda_{H h h} \right]^2$$

+ radiation contributions

+ interference terms

}

sensitive to $\lambda_{h h h}$ and $\lambda_{H h h}$

(iii) triple Higgs production $e^+e^- \rightarrow Ahh$

Trilinear Higgs self-couplings in double and triple Higgs production

λ	double Higgs production				triple Higgs production			
	Zhh	ZHh	ZHH	ZAA	Ahh	AHh	AHH	AAA
hhh	x				x			
Hhh	x	x			x	x		
HHh		x	x			x	x	
HHH			x				x	
hAA				x	x	x		x
HAA				x		x	x	x

- ▶ combination of couplings in Higgs-strahlung isomorphic to WW fusion
- ▶ cross sections large enough \Rightarrow system solvable for all λ 's up to discrete ambiguities "bottom-up approach"
- ▶ in practice not all cross sections large enough \Rightarrow compare the theoretical predictions with experimental results for of the cross sections the accessible channels "top-down approach"
- ▶ MSSM: $\lambda(hAA), \lambda(HAA)$ are small \Rightarrow can be left out of the analysis

Sensitivity areas

- ▶ sensitivity areas defined in the $[M_A, \tan\beta]$ plane
- ▶ sensitivity criteria

$$(i) \sigma[\lambda] > 0.01 \text{ fb}$$

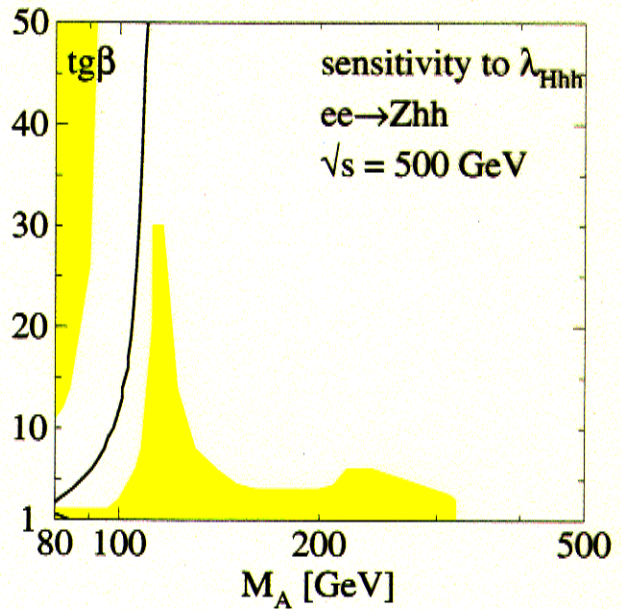
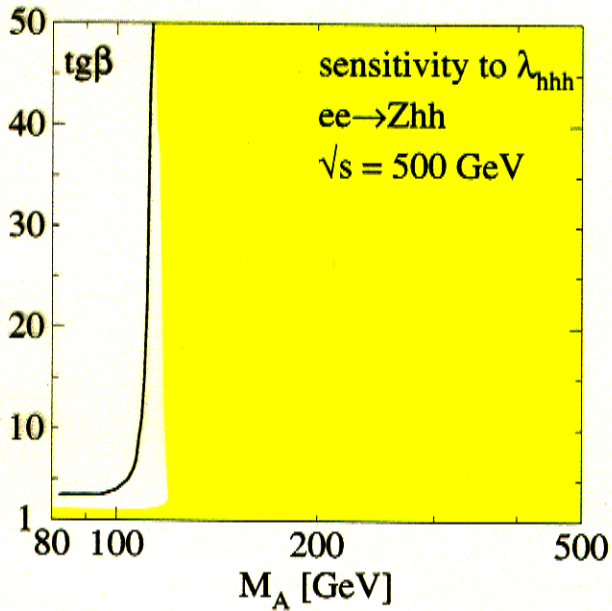
$$(ii) \text{eff}\{\lambda \rightarrow 0\} > 2 \text{ st.dev. for } \int \mathcal{L} = 2ab^{-1}$$

no mixing included

Sensitivity areas for $\lambda_{hhh}, \lambda_{HHh}$

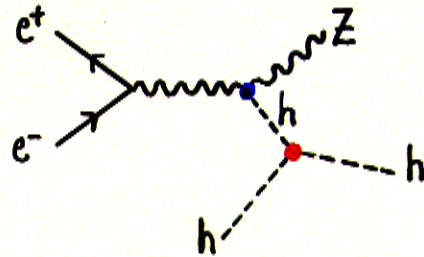
processes sensitive to λ_{hhh} : Zhh, Ahh

λ_{HHh} : Zhh, ZHh, Ahh



regions of no sensitivity: couplings $\lambda \sin(\beta - \alpha), \lambda \cos(\beta - \alpha)$ are small

for example:



$\sim \lambda_{hhh} \sin(\beta - \alpha)$

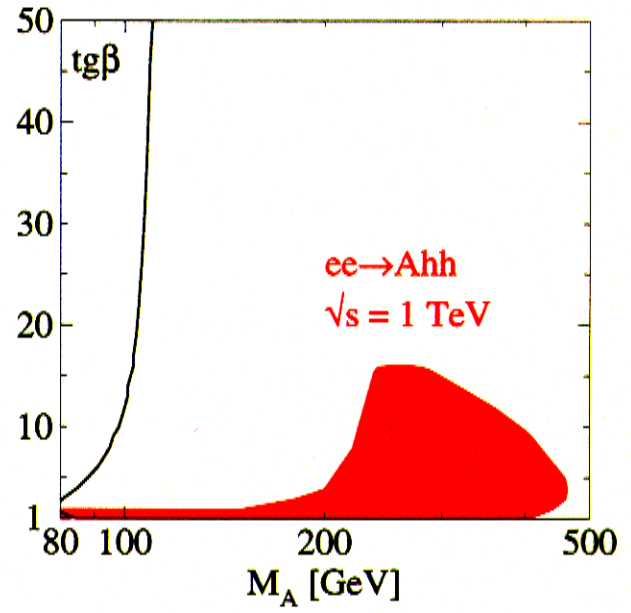
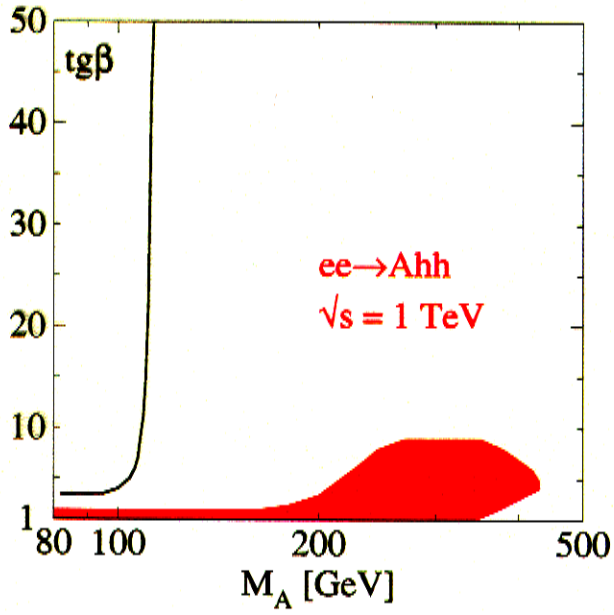
large M_A : sensitivity criteria not fulfilled due to

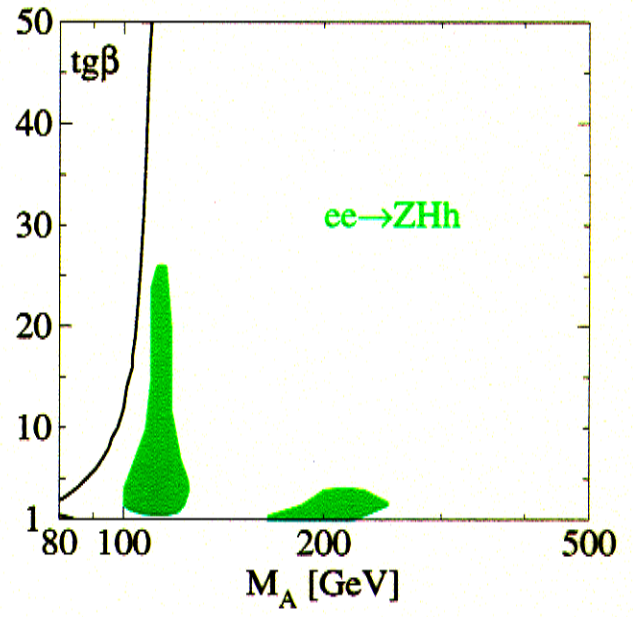
- * phase space effects
- * suppression of the H, A propagators for large masses

sensitivity areas for λ_{HHh} in ZHh, ZHH

λ_{HHH} in ZHH

are smaller





Conclusions

Standard Model:

- * Double Higg-strahlung and WW double Higgs fusion are sensitive to λ_{HHH} in the intermediate Higgs mass region
- * For $M_H = 120 \text{ GeV}$ $\sqrt{s} = 500 \text{ GeV}$ is a good choice: sensitivity to λ_{HHH} large (ZH)H
- * Cross sections are small \Rightarrow high \mathcal{L} needed
- * $\delta\lambda_{HHH}/\lambda_{HHH} \lesssim 20\%$

MSSM trilinear Higgs self-couplings

- * The processes Zhh, ZHh, Ahh are sensitive to $\lambda(hhh), \lambda(Hhh)$ in parts of the parameter space $\tan\beta - M_A$
- * Sensitivity areas for $\lambda(HHh), \lambda(HHH)$ are smaller.

\Rightarrow Trilinear Higgs self-couplings are accessible at e^+e^- linear colliders \leadsto
First step in order to establish the Higgs mechanism experimentally.