

# **Muon Colliders and Muon Storage Rings as a Source of Neutrino Beams**

**(For the Neutrino Factory and  
Muon Collider Collaboration)**

**presented by**

**Andrew M. Sessler**

- 1. Muon Collider Physics [Raja]**
- 2. Neutrino Physics [Shaevitz]**
- 3. Proton Source**
- 4. Targeting, Capture and Decay**
- 5. Cooling**
- 6. Acceleration**
- 7. Collider Ring or Storage Ring**
- 8. Example: The PJK Neutrino  
Factory**
- 9. Detector and Background [Raja]**
- 10. Neutrino Radiation Hazard**
- 11. R and D: Theory, Mucool,  
Target Experiment, Other  
Experiments**

## History of Muon Colliders

Muon Collider mentioned {  
Tinlot (1960)  
Budker (1969)  
Skrinsky (1971)  
Neuffer (1979)

Ionization Cooling

{Skrinsky & Parkhomchuk (1981)

High Luminosity {Neuffer(1985) & Palmer(1994)

Collaboration Formed (1995)

Charles M. Ankenbrandt et al. (Muon Collider  
Collaboration) Phys. Rev. ST Accel. Beams 2,  
081001 (1999) (73 pages)

### Future

Collaboration Home Page

[http://www.bnl.gov/cap/mumu/mu\\_home\\_page.htm](http://www.bnl.gov/cap/mumu/mu_home_page.htm)

Physics Potential of Muon Colliders, San Francisco,  
Dec. 15-17, 1999

Collaboration Meeting, Catalina, May 17-19, 2000

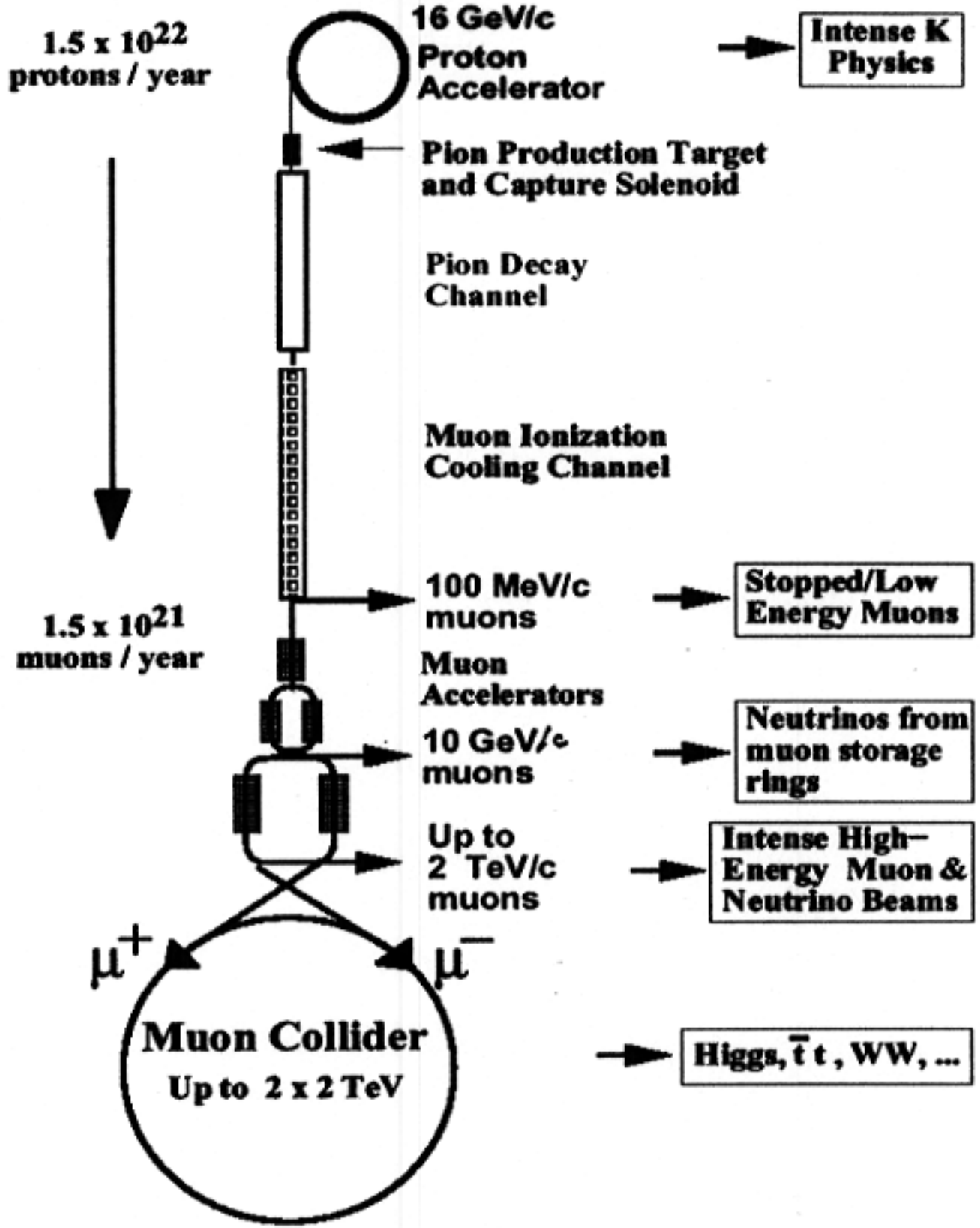
## **History of Muon Storage Rings as a Neutrino Source**

1. Concept proposed: DeRujula, A., S.L. Glashow, R.R. Wilson, G. Charpak, Phys. Rev. **99**, 341 (1983).
2. Quantified: Geer, S. Phys. Rev. D **57**, 6989 (1998).
3. Workshop on Front End Physics of a Muon Collider, Fermilab, 1997:
4. Workshop on the Potential for Neutrino Physics at Future Muon Colliders, Brookhaven, 1998.
6. Meeting in Berkeley, April, 1999.
6. Discussion at St. Croix, May, 1999.
7. ICFA/ECFA Workshop, NUFACT99, Lyon, July 5-9, 1999. (<http://lyopsr.in2p3.fr/nufact99/>)

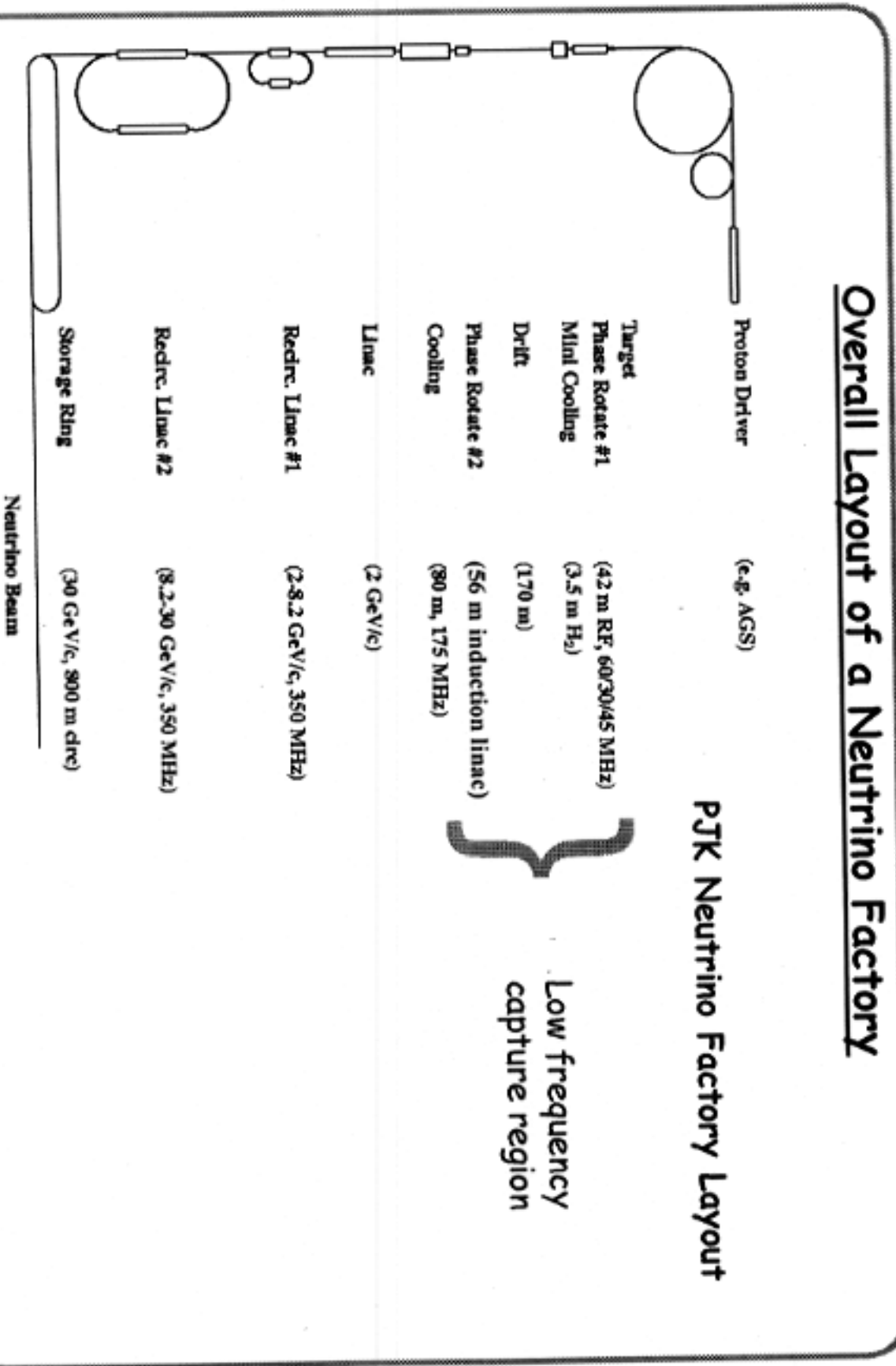
### **Future**

**Nufact00, Monterey, May 22-26, 2000**

# Muon Collider Schematic



# Overall Layout of a Neutrino Factory



Proton Driver

(e.g. AGS)

**PJK Neutrino Factory Layout**

Target

Phase Rotate #1

(42 m RF, 60/30/45 MHz)

Minl Cooling

(3.5 m H<sub>2</sub>)

Drift

(170 m)

Phase Rotate #2

(56 m induction linac)

Cooling

(80 m, 175 MHz)

Linac

(2 GeV/c)

Reduc. Linac #1

(2.8.2 GeV/c, 350 MHz)

Reduc. Linac #2

(8.2-30 GeV/c, 350 MHz)

Storage Ring

(30 GeV/c, 800 m circ)

Neutrino Beam

Low frequency capture region

## Basic Facts $\mu^- \rightarrow e^- + \nu_\mu + \bar{\nu}_e$

$$\frac{d^2 N_{\nu_\mu}}{dx d\Omega} = \frac{2x^2}{4\pi} [(3-2x) - (1-x)\cos\vartheta]$$

$$\frac{d^2 N_{\nu_e}}{dx d\Omega} = \frac{12x^2}{4\pi} [(1-x) - (1-x)\cos\vartheta]$$

$$\cos\vartheta = \hat{P}_\nu \cdot \hat{S}_\mu \quad x = \frac{2E_\nu}{m_\mu c^2}$$

$$\sigma_{\nu_n} = 0.67 * 10^{-38} E_\nu (\text{GeV}) \text{cm}^2$$

$$\sigma_{\nu_n} = 0.34 * 10^{-38} E_\nu (\text{GeV}) \text{cm}^2$$

### **OSCILLATIONS**

$$P(\nu_1 \rightarrow \nu_2) = \sin^2(2\vartheta) \sin^2 \frac{1.27(\Delta m^2)L}{E}$$

$\vartheta$  = Mixing angle

$$\Delta m^2 = m_1^2 - m_2^2 \text{ in } \left(\frac{\text{eV}}{c^2}\right)^2$$

L in km

E in GeV

## MIXING PARAMETERS

Assume only three neutrinos

$$\vartheta_{12}, \vartheta_{13}, \vartheta_{23}, \Delta^2 m_{12}, \Delta^2 m_{23}, \delta$$

$$\vartheta_{ij}: \nu_e \rightarrow \nu_\mu, \text{ etc.}$$

$$\sigma: \text{CP } \nu_e \rightarrow \nu_\mu \stackrel{?}{=} \bar{\nu}_e \rightarrow \bar{\nu}_\mu$$

$$\text{T } \nu_e \rightarrow \nu_\mu \stackrel{?}{=} \nu_\mu \rightarrow \nu_e$$

$$\bar{\nu}_e \rightarrow \bar{\nu}_\mu \stackrel{?}{=} \bar{\nu}_\mu \rightarrow \bar{\nu}_e$$

$$\text{CPT } \nu_e \rightarrow \nu_\mu \stackrel{?}{=} \bar{\nu}_\mu \rightarrow \bar{\nu}_e$$

$$\nu_\mu \rightarrow \nu_e \stackrel{?}{=} \bar{\nu}_e \rightarrow \bar{\nu}_\mu$$

*3 & 2 don't sum  
to  $\pi$  then  
sterile neutrinos*

In general, a 3x3 matrix, characterized by 6 parameters, describes the oscillation of the 3 neutrinos.

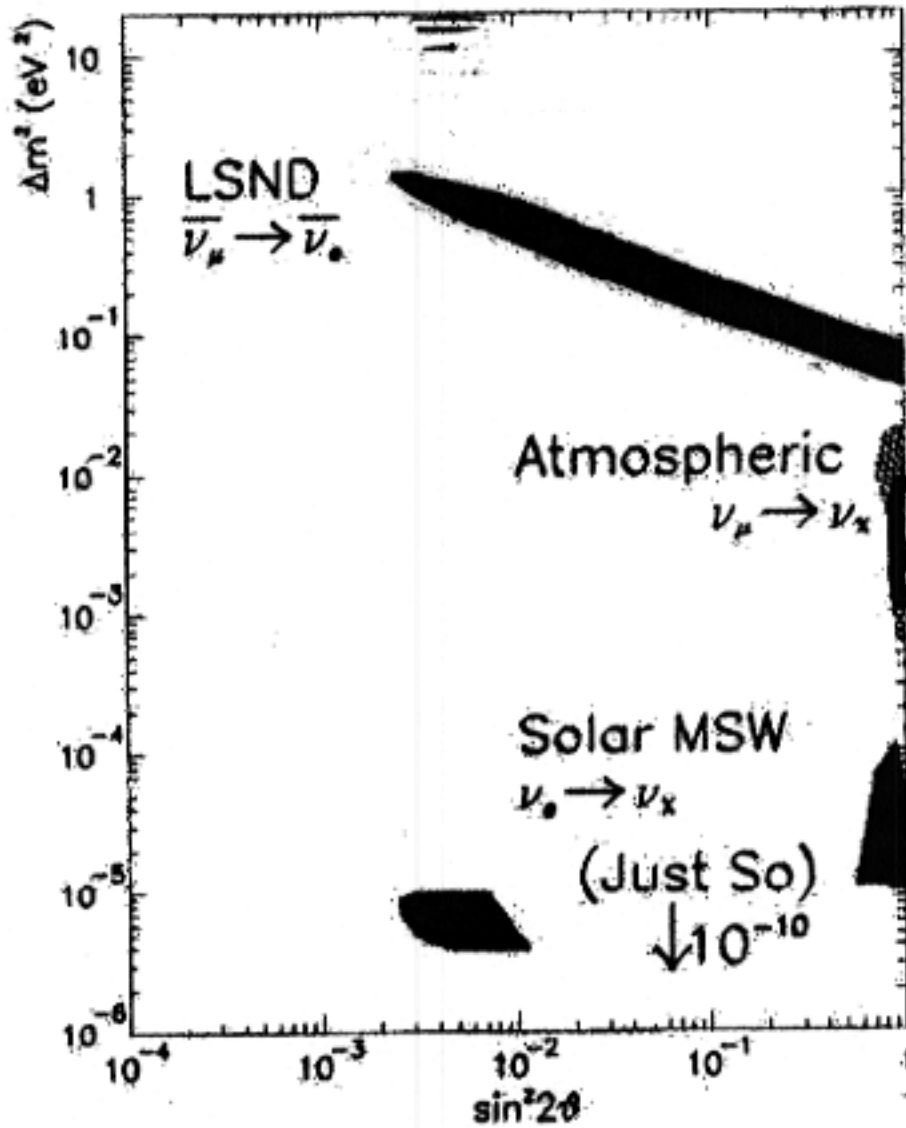
For  $\delta = 0$ :

$$P(\nu_e \rightarrow \nu_\mu) \sim \sin^2(\vartheta_{23}) \sin^2(2\vartheta_{13}) \sin^2\left(\frac{\Delta m_{13}^2 L}{4E}\right)$$

$$P(\nu_e \rightarrow \nu_\tau) \sim \cos^2(\vartheta_{23}) \sin^2(2\vartheta_{13}) \sin^2\left(\frac{\Delta m_{23}^2 L}{4E}\right)$$

$$P(\nu_\mu \rightarrow \nu_\tau) \sim \cos^4(\vartheta_{13}) \sin^2(2\vartheta_{23}) \sin^2\left(\frac{\Delta m_{23}^2 L}{4E}\right)$$

### 3 different mass-scales



From J. Conrad hep-ex/0609



## QUESTIONS

- Is a  $\nu$  factory feasible?
- At what cost?
- How soon?
- What R&D is needed?
- What do we want to know about neutrino masses and mixings  
now...      in 5 years...      in 10 years?
- Is a  $\nu$  factory the best (only) way to answer these questions?
- What range of beam parameters should the  $\nu$  factory provide?
- What detectors are needed to carry out the  $\nu$  factory physics program?

Probably known:  
 $\theta_{12}$  &  $\theta_{23}$   
 $\Delta m_{23}^2$   $\Delta m_{12}^2$

Left to learn =  
 $\theta_{13}$   $\delta$   
 $\Rightarrow$  Sign of  $\Delta m_{12}^2$



## Neutrino sources and muon colliders

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- Requires high power proton source/target and efficient capture, but many other parts are easier, and some are different.
  - ➔ No  $N_{\mu}^2$  dependence from luminosity-- bunches less intense, higher-frequency rf.
  - ➔ Transverse cooling factor 100 (vs  $10^4$ ), no longitudinal cooling.
  - ➔ Accelerator chain and storage ring must have large acceptance to minimize cooling requirements (but no small beta sections)
  - ➔ The ring may have unusual bow tie or triangle shape--and be tilted.

# PROTON SOURCE



## NEED:

- Proton Beam Power 2-4 MW
- Very short bunch: rms 1-2 nsec

## FNAL PROPOSAL: 4 MW

- Upgraded linac (.4 → 1 GeV)
- Higher field operation in Booster
- New Pre-Booster (16 GeV)

S. Holmes  
FNAL

## BNL PROPOSAL: 2 MW

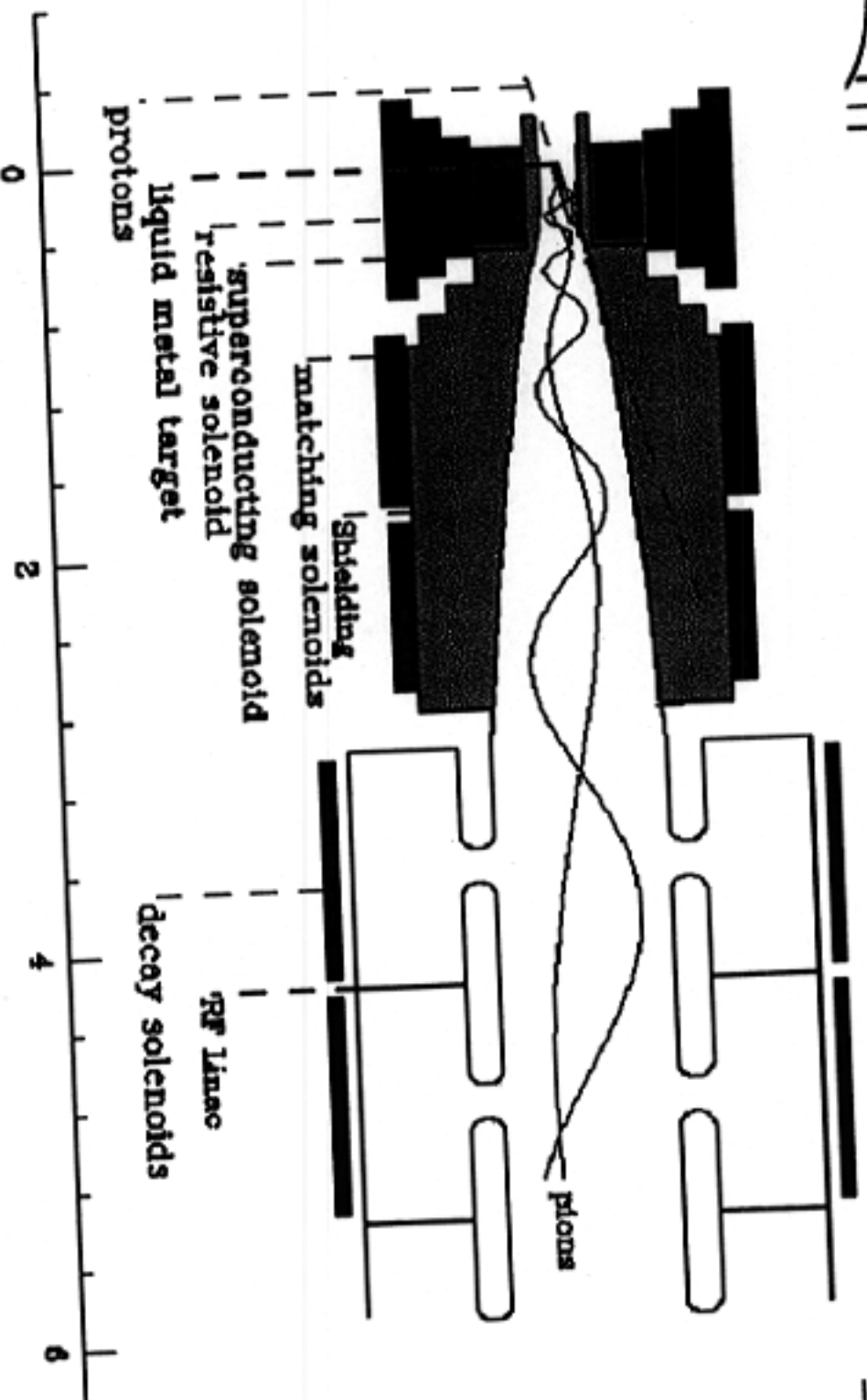
- Upgraded linac (.2 → .6 GeV)
- Increased AGS rep rate: 2.5 Hz

T. Roser  
BNL

• 1 MW if  $10^4$  @ 2.5 Hz



## Target and Capture



4MW, 16 GeV proton beam hits liquid metal target in 20T solenoid  
Pions and (then muons) captured in decay channel

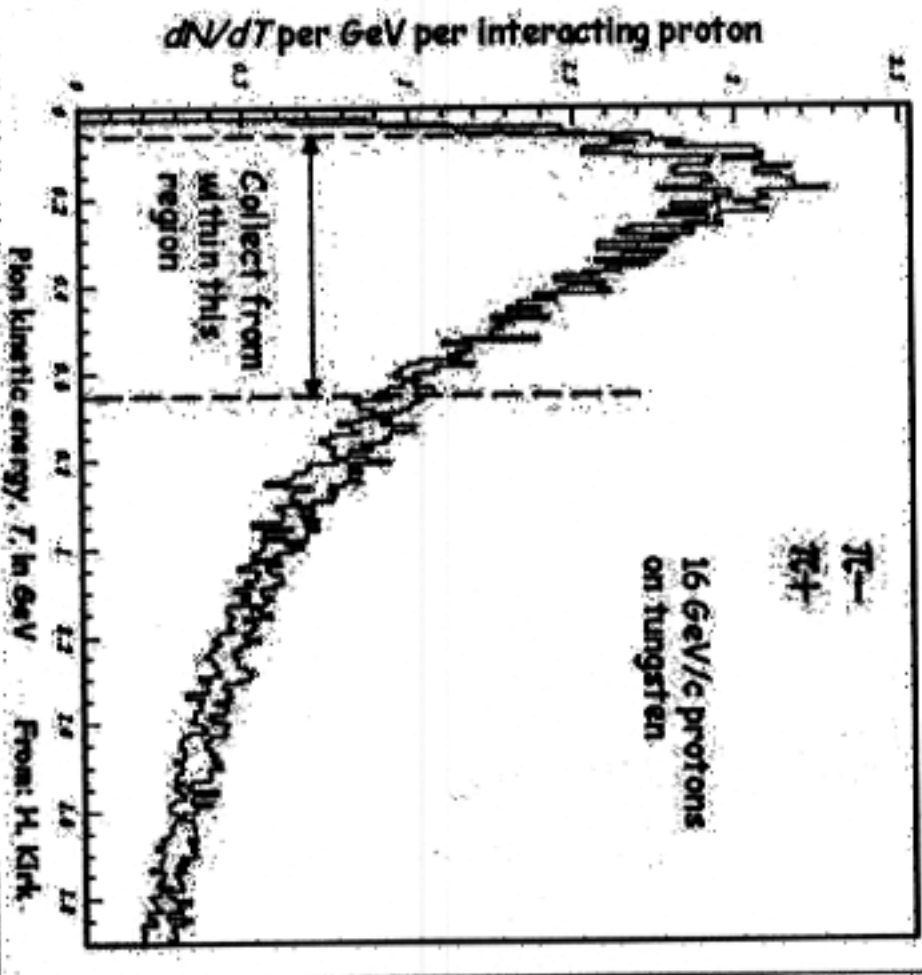
## Target and Production

MUTAC.21 July 1999 (dl)

We aim to collect and deliver to the first phase rotation channel 0.6 pions of each sign per proton of 16 GeV/c

In the region of low kinetic energy shown opposite this can be achieved by immersing the production target in a 20 T solenoid field of 70 mm radius. Pions of both signs having transverse momentum of up to 225 MeV/c are focused into the decay channel via the matching channel

Note that the pion velocity varies from 0.68 to 0.98

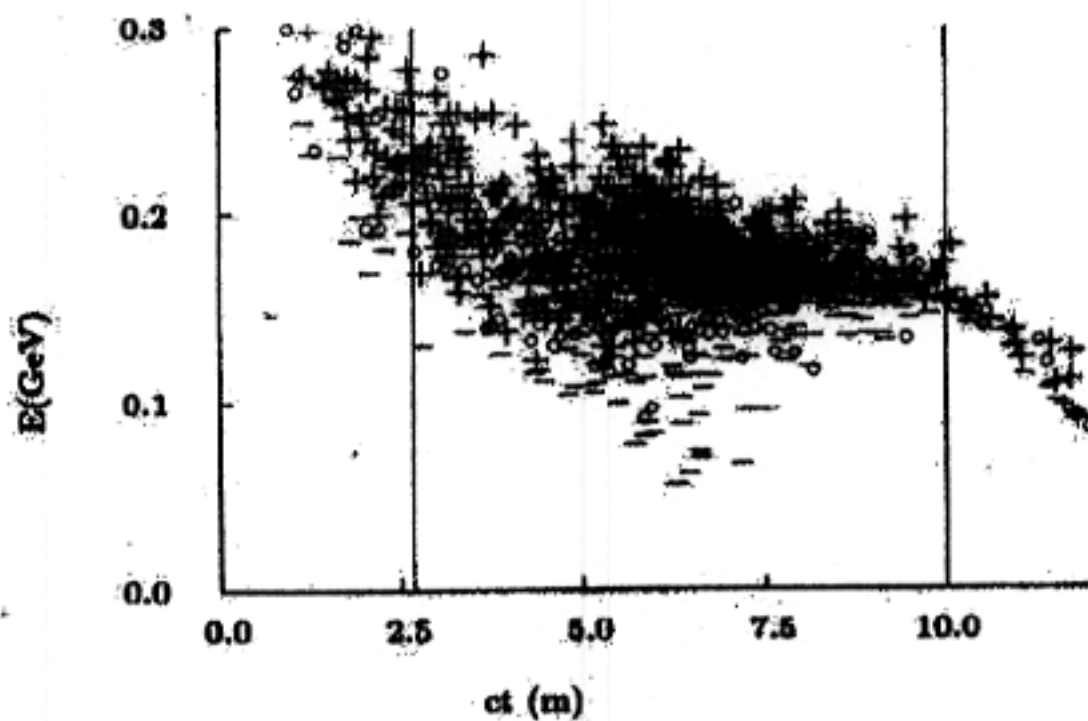


# Simulations of Capture and phase Rotations

Color and symbols indicate Polarization:

red +  $P > .3$   
green o  $.3 > P > -.3$   
black -  $-.3 < P$

After First Phase Rotation:  
 $\mu/\pi \approx 0.3$   $\delta_p \approx 15\%$

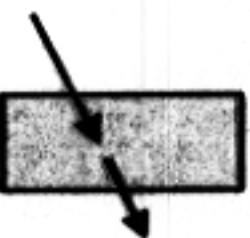




## Cooling of 6-D phase space

- Muons from the target are initially captured into a 6-D phase space volume that must be decreased by  $10^6$  before collision
- Cooling time must be of order  $\tau_\mu$  --distance of order  $c\tau_\mu \sim 660\text{m}$ .
- Ionization cooling (Skrinsky & Parhomchuk, 81). Basic Idea

Momentum reduced  $\delta p \parallel p$



Absorber

Momentum restored  $\delta p_z$

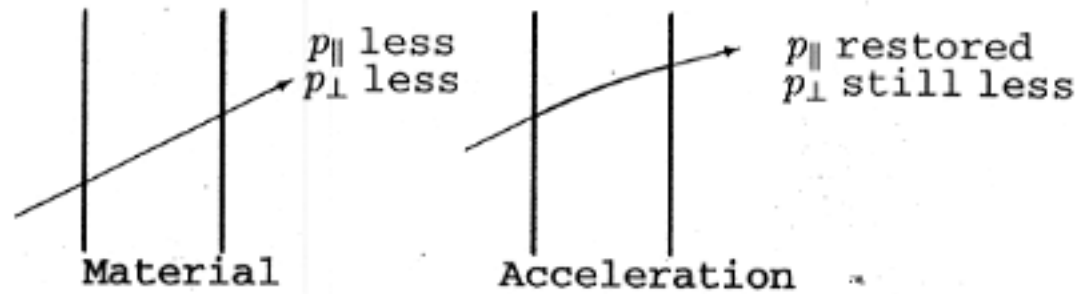


RF

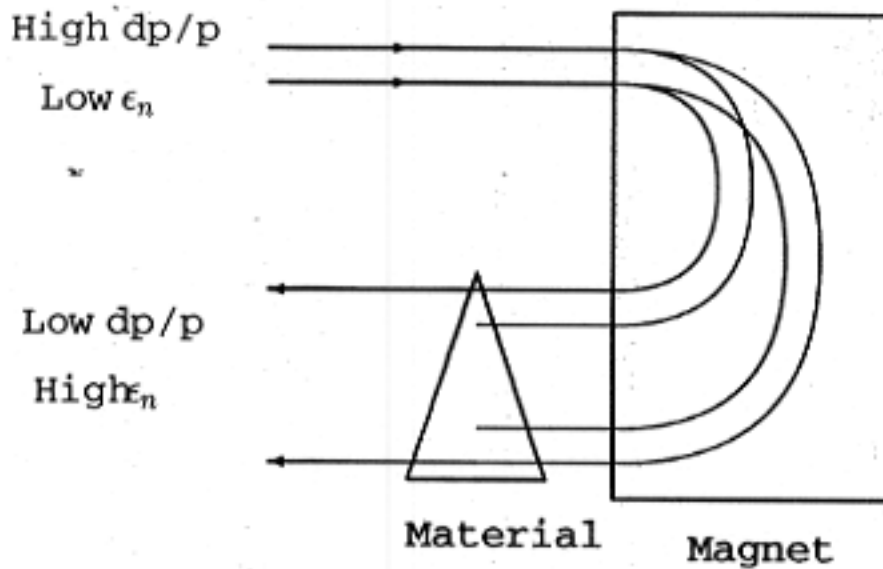
**Need to fight multiple scattering and longitudinal blowup**

# IONIZATION COOLING

- TRANSVERSE



- LONGITUDINAL COOLING





†

- Emittance rate of change

$$\frac{d\epsilon_n}{dz} = -\frac{\epsilon_n}{E\beta^2} \left\| \frac{dE}{dz} \right\| + 0.5\beta\gamma \frac{d\langle \theta^2 \rangle}{dz}$$

- MINIMUM EMITTANCE

$$\epsilon_n \approx \frac{0.5E_s^2 \beta_{\perp}}{m_{\mu}c^2 \beta} (L_R \|dE/dz\|)^{-1}$$

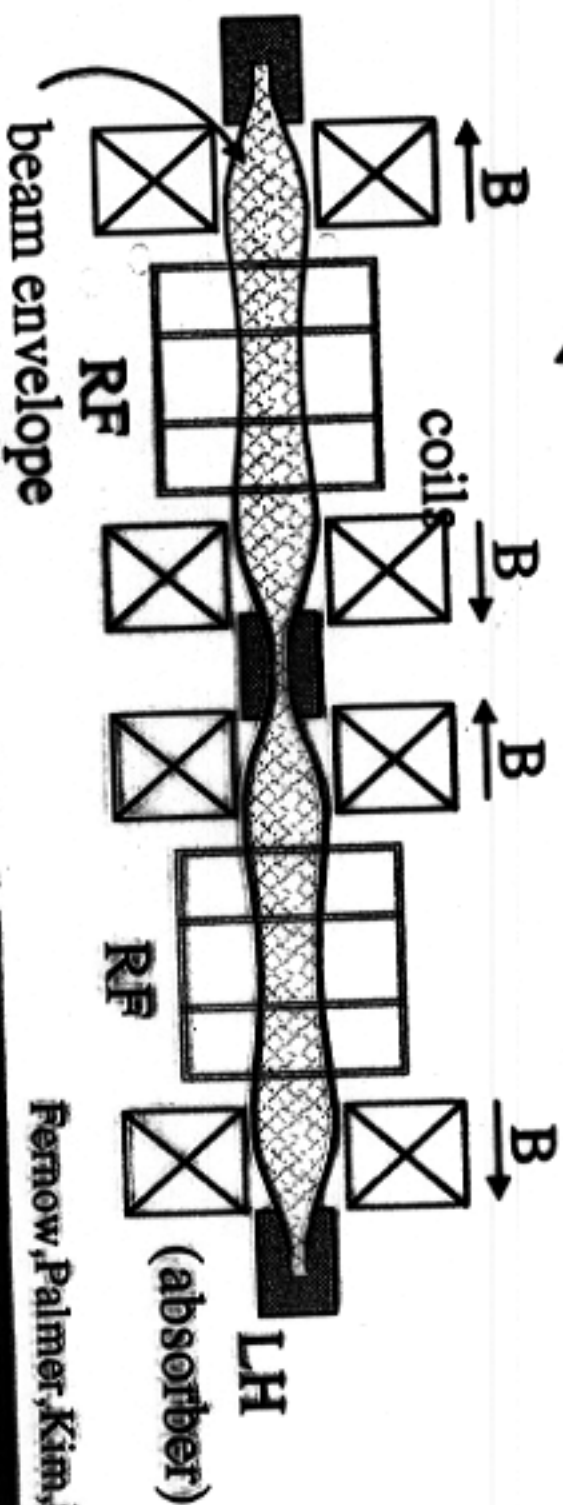
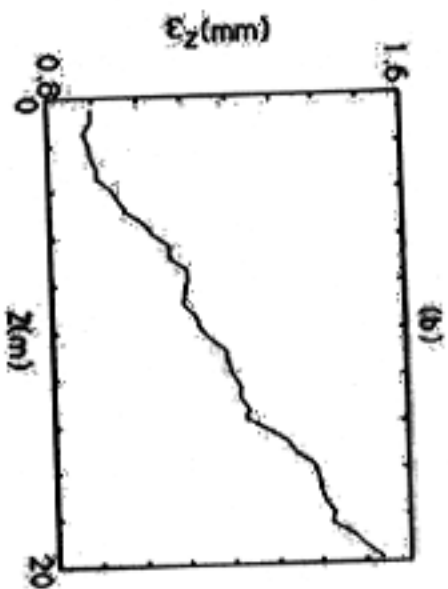
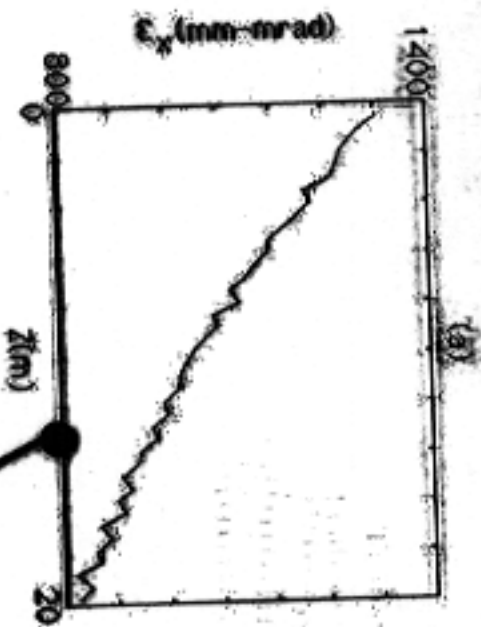
- Best material for cooling, Li, LiH, Be, H<sub>2</sub>

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⊕  $\mu^+ \mu^-$  COLLIDER



# Transverse Cooling Simulation



BERKELEY LAB

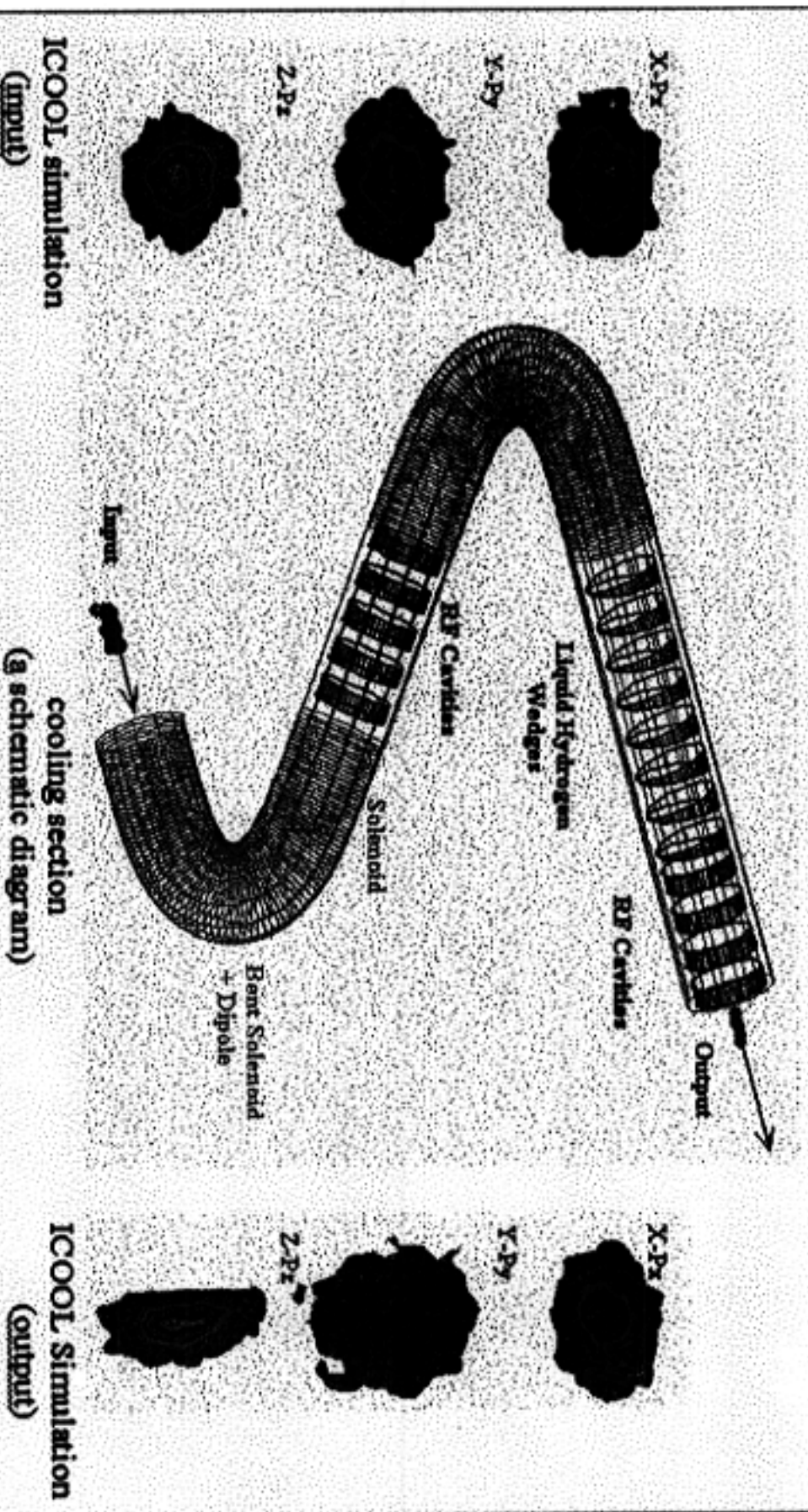
Fernow, Palmer, Kim, Penn



# Emittance exchange is crucial

## ICCOOL Simulation

Momentum Exchange Using Bent Solenoids and Wedges



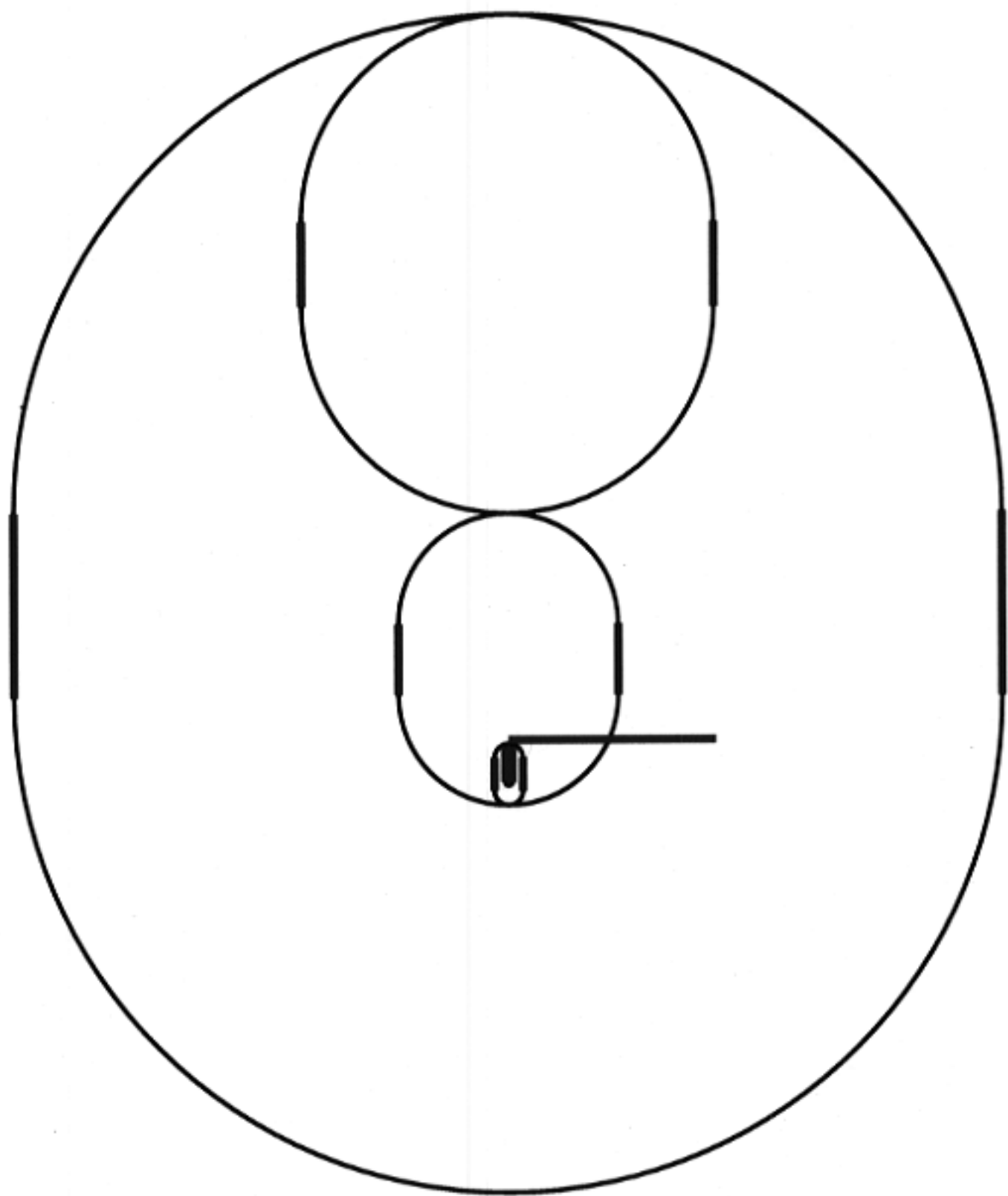
- Scenarios

1. Sequence of linacs (VERY EXPENSIVE)
2. Recirculating linacs with multiple arcs (similar to CEBAF) (RELATIVELY EXPENSIVE)
3. Synchrotrons with fast pulsed magnets with long SC linacs (MORE ECONOMICAL)
4. (250 GeV) 4 T pulsed magnets ( $t=1$  msec)
5. (2 TeV) Interlace of fixed 8 T SC dipole magnets with  $\pm 2$  T pulsed magnets
6. FFAG

†

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⊙  $\mu^+ \mu^-$  COLLIDER



# Recirculating Linacs

E. Keil

Frequency:	352.209 MHz	
Energy (GeV):	2-8	8-30
Number of Passes:	4	4
Accelerating Linac Voltage (MV)	1.5	5.5
Length of Half Cell (m):	3.4	14.9
$\beta_{\text{Max}}$ (m)	11.3	49.6
$\mu/2\pi$	0.21	0.21
Acceptance (mm) (normalized)	16.5	15.0

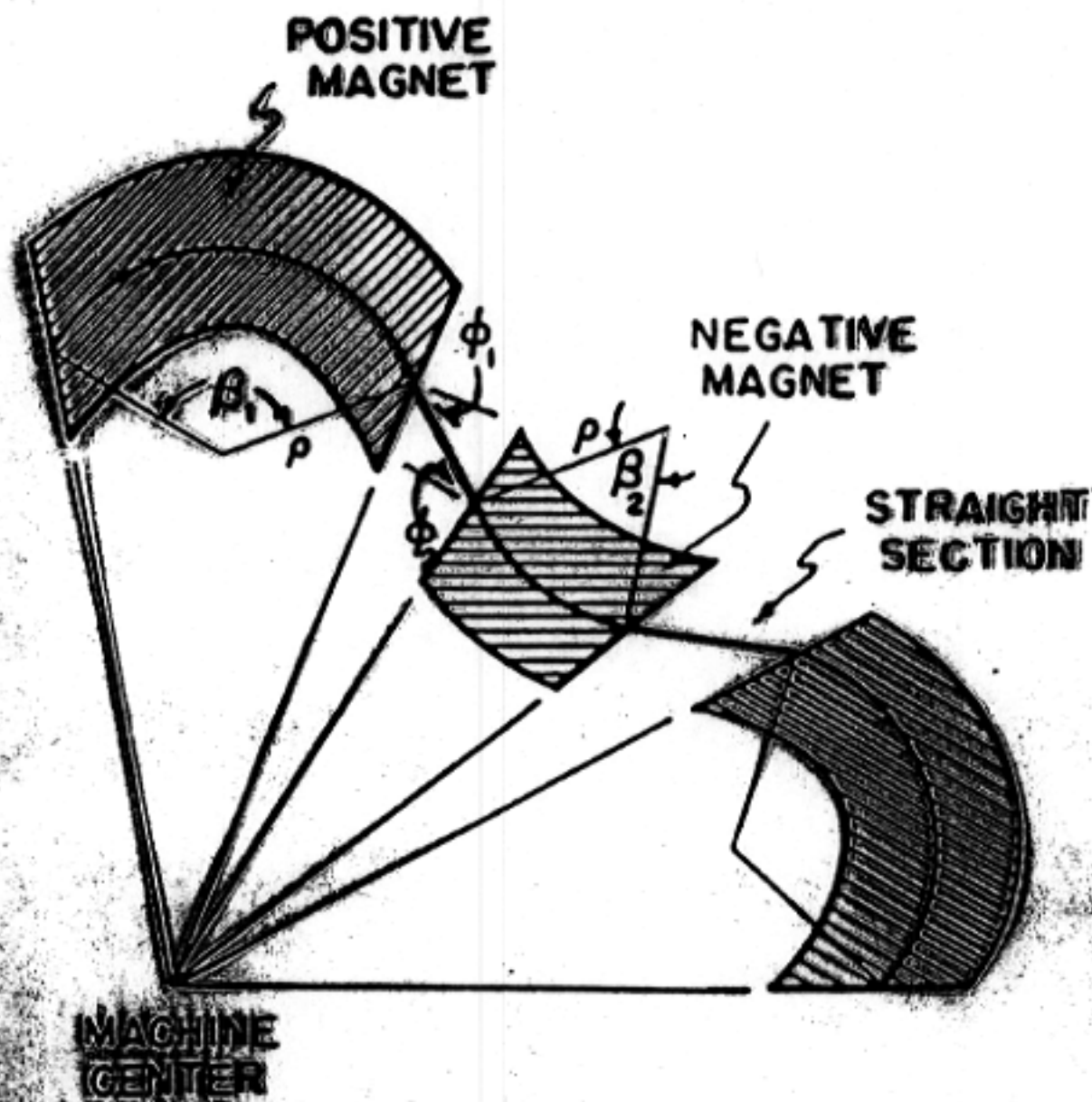


FIG. 7. Equilibrium orbit notation for radial sectors with straight sections.

# COLLIDER RING :\*

3 TeV x 3 TeV

- Highest possible bending magnet to maximize No. of turns in the ring before decay

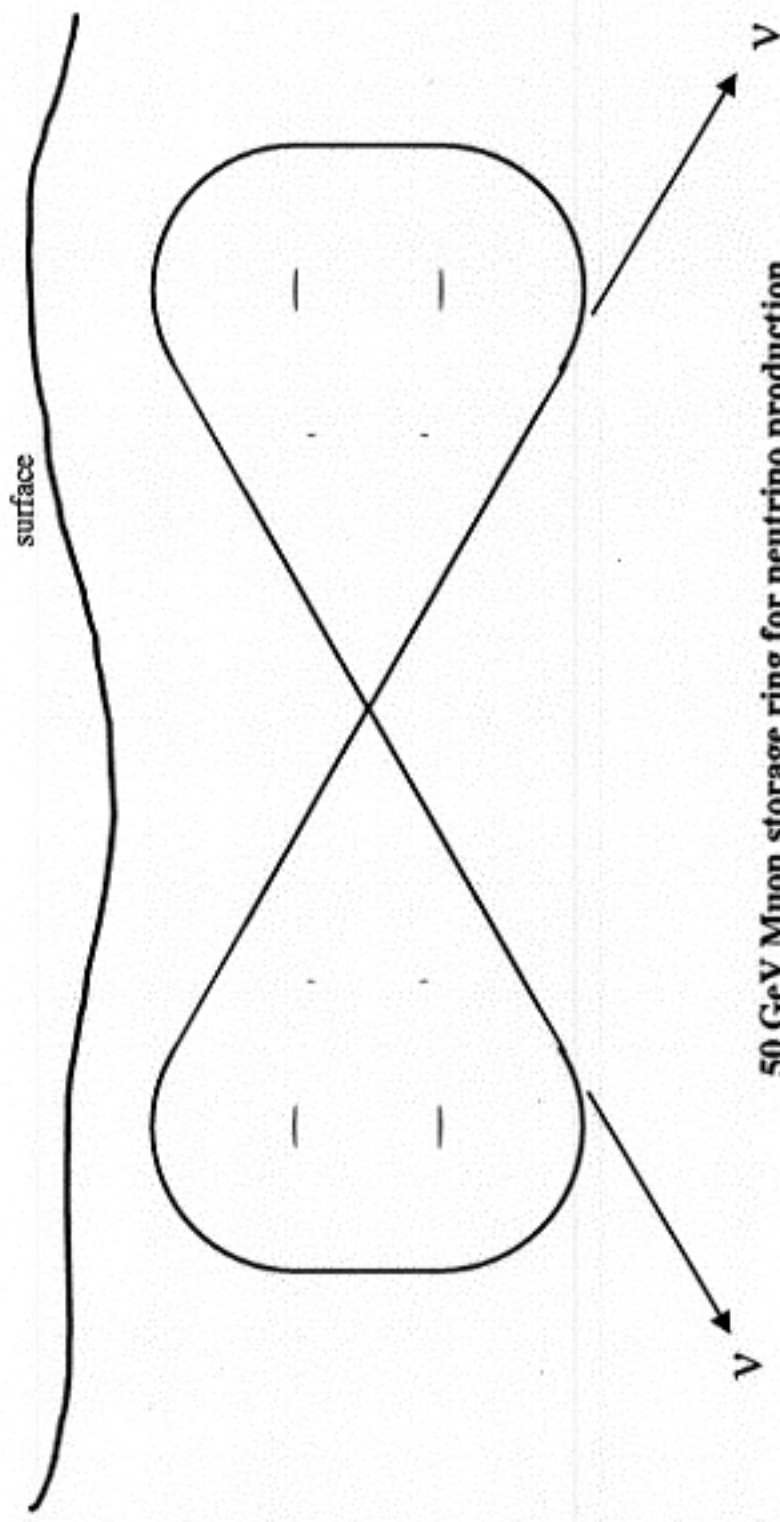
$\beta^*$	3 mm
$\sigma_z$	3 mm
$\epsilon_n$	$50 \pi \text{ mm} - \text{mrad}$
$\delta = \frac{\Delta p}{p}$	0.12%
No. of turns	11000
No. muons	$2 \times 10^{12}$
No. bunches	2
beam - beam tune shift	0.05

- Isochronous lattice

- IP-Local Chromatic Correction is essential

 COLLIDER





**50 GeV Muon storage ring for neutrino production**

Circumference 1150 m; 400 m total length of straight sections that produce low-divergence neutrino beams.

Ring lies in a tilted plane so that the neutrinos travel through the earth to two distant detectors.

Arcs contain superconducting dipoles at 5.3 T and quadrupoles.

# Muon Budget for a Neutrino Factory

All numbers are  $\mu/p$

Initially	0.66
After Phase Rotation #1	0.3
After Phase Rotation #2	0.21
After RF Capture	0.15
After Cooling	0.13
After Acceleration	0.1

From a 1.5 MW proton source, this would be  $4 \times 10^{20}$  muons per year decaying. (A year is taken as  $2.5 \times 10^7$  seconds.) About 25 % are pointing in a direction to hit a detector, so the number of decays will be  $10^{20}$  per year in any one detector. (Probably two detectors are illuminated.)

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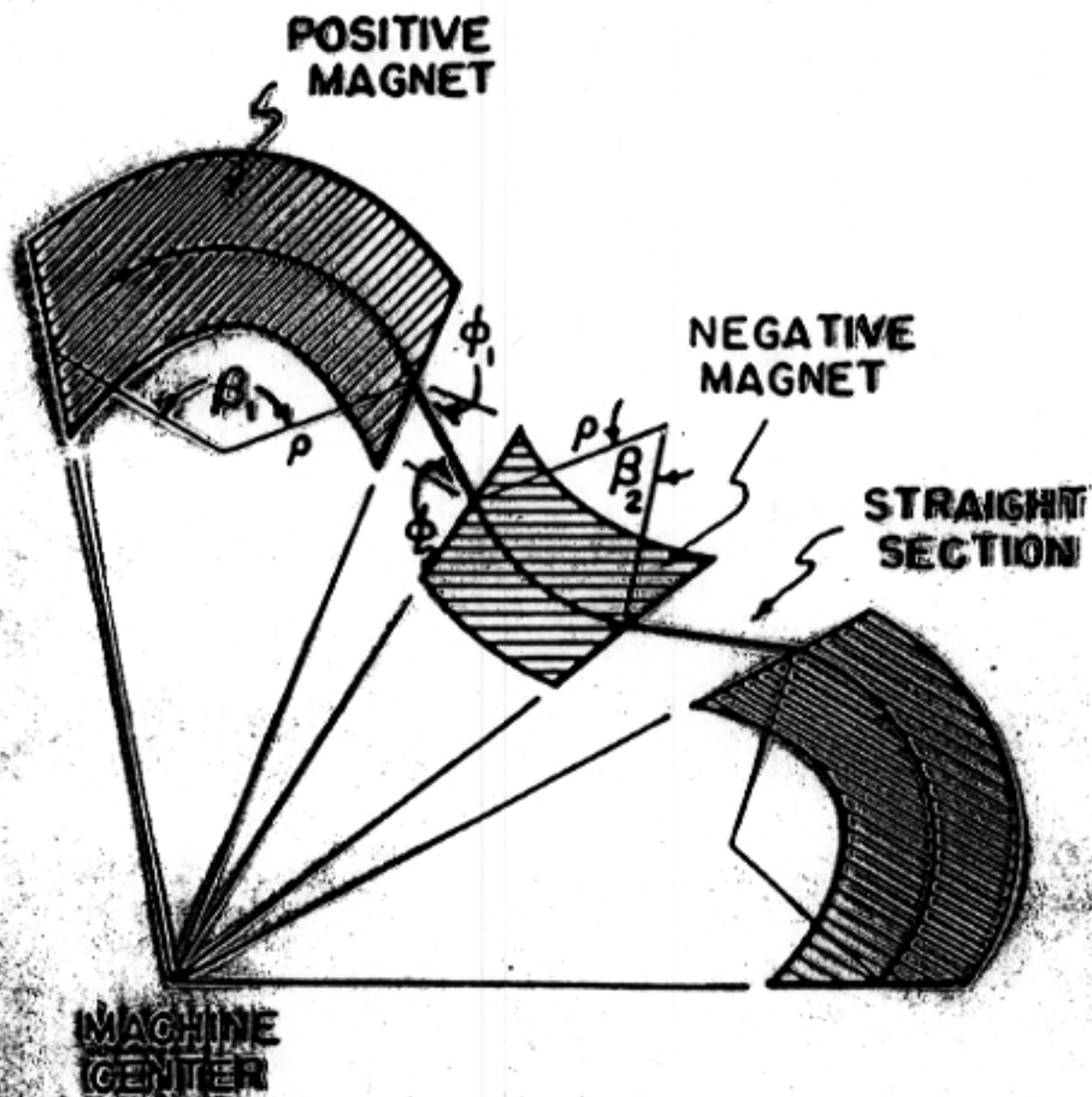


FIG. 17. Equilibrium orbit notation for radial sectors with straight sections.

# COLLIDER RING :\*

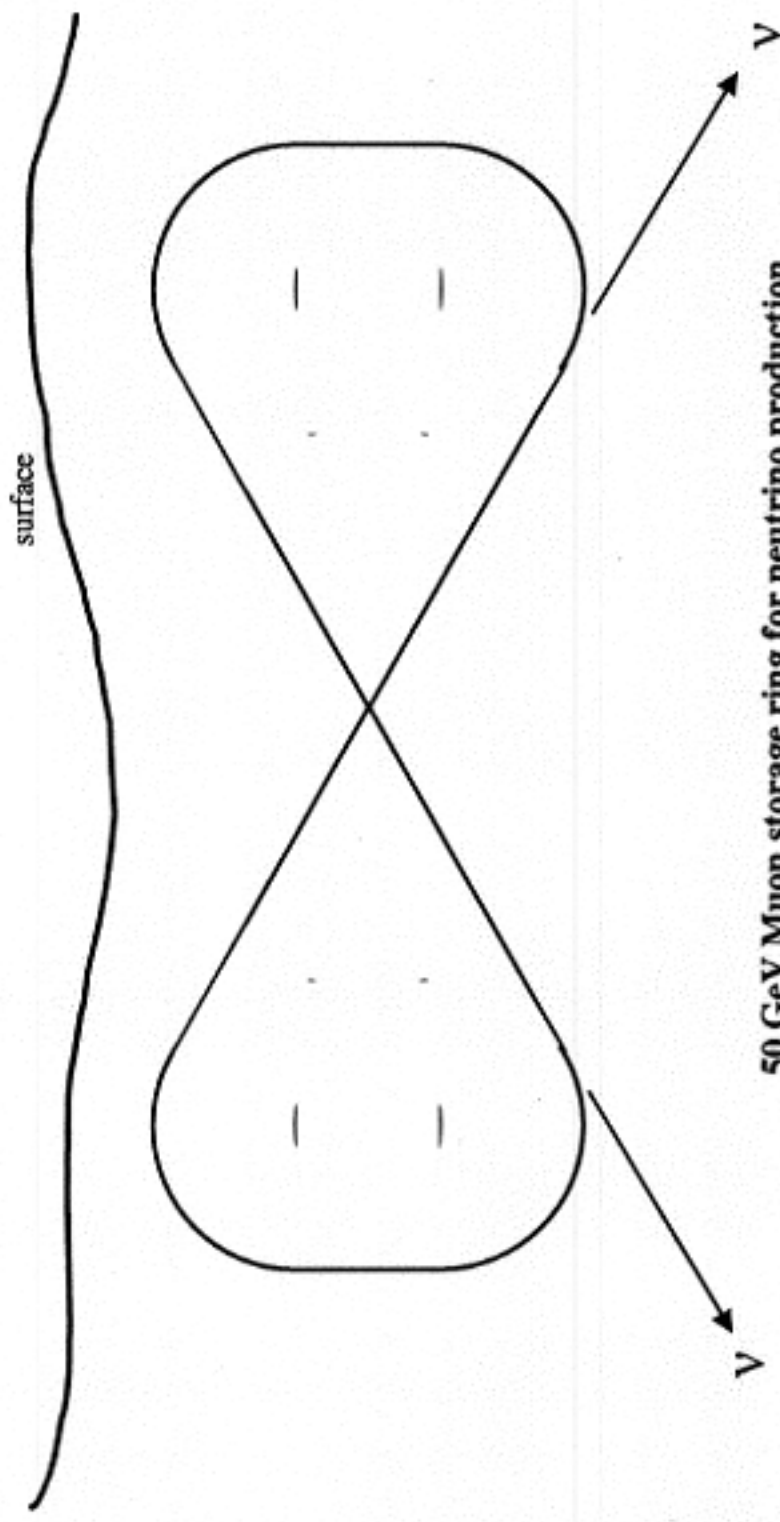
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### Linacs

$p_{\min}$ GeV/c	$p_{\max}$ GeV/c	$f$ MHz	$V$ MV/m	$\phi$ °	$L_{\text{lin}}$ m	loss %	$\sigma_E$ MeV	$\sigma_\tau$ ps
.186	.67	50	7.5	71-33	145	6.4	19-44	1231-541
.67	2.1	200	15	65-33	213	2.9	85-176	283-136
2.1	4	800	30	65-45	166	0.9	336-511	71-47

### Recirculators

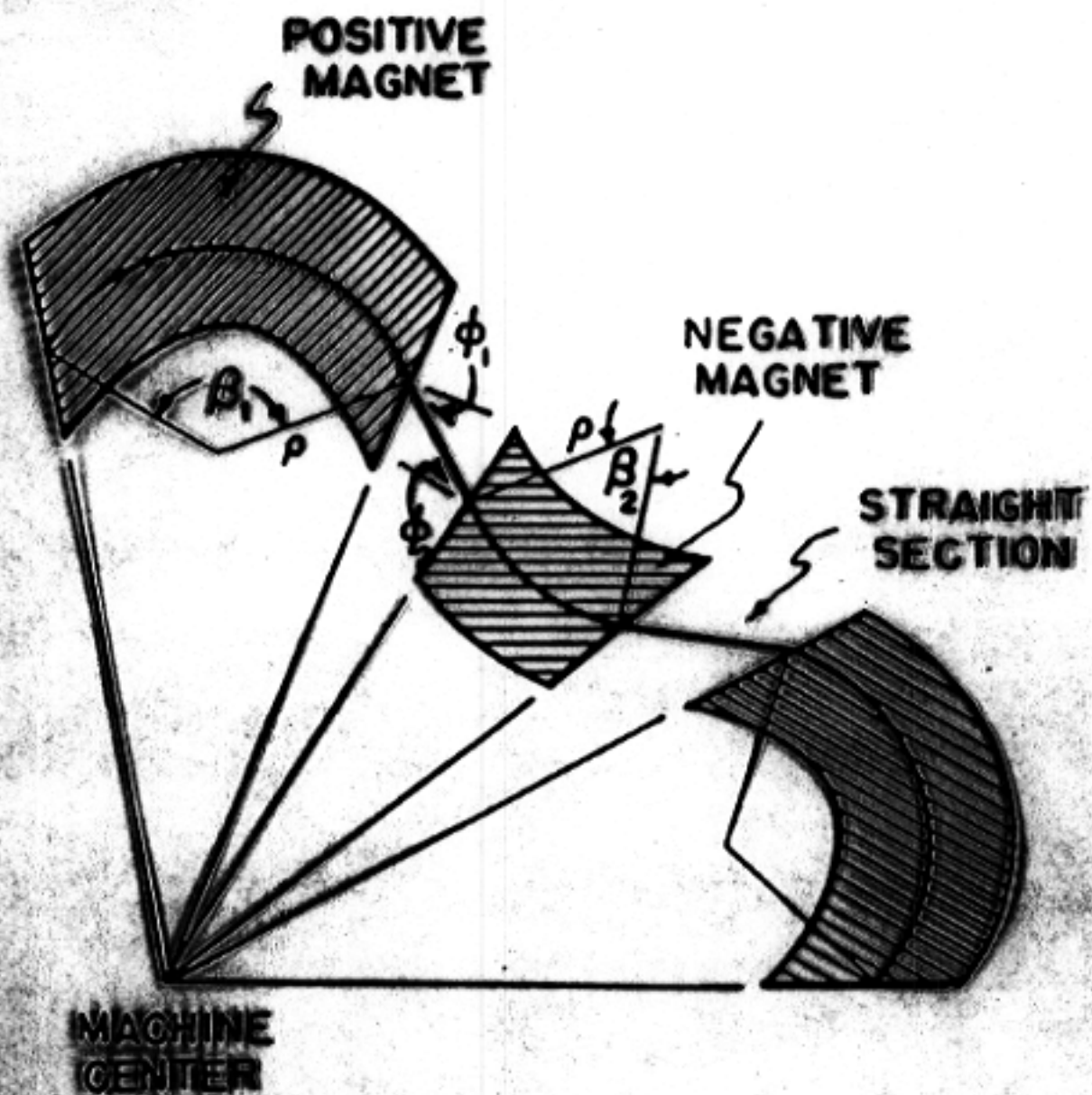
$p_{\min}$ GeV/c	$p_{\max}$ GeV/c	$f$ MHz	$V$ MV/m	$\phi$ °	$L_{\text{arc}}$ m	$L_{\text{lin}}$ m	$n_{\text{turn}}$	$P_{\text{peak}}$ MW	loss %	$\sigma_E$ MeV	$\sigma_\tau$ ps
4	16	800	30	29	28	88	4	1246	1.7	350	77
16	64	800	30	29	112	83	17	696	3.0	343	79
64	250	1600	42	25	873	178	21	405	5.0	792	34
250	625	1600	42	24	1637	213	35	278	4.9	842	32
625	1500	1600	42	18	3930	464	36	266	4.9	1097	25



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**FIG. 7. Equilibrium orbit notation for radial sectors with straight sections.**

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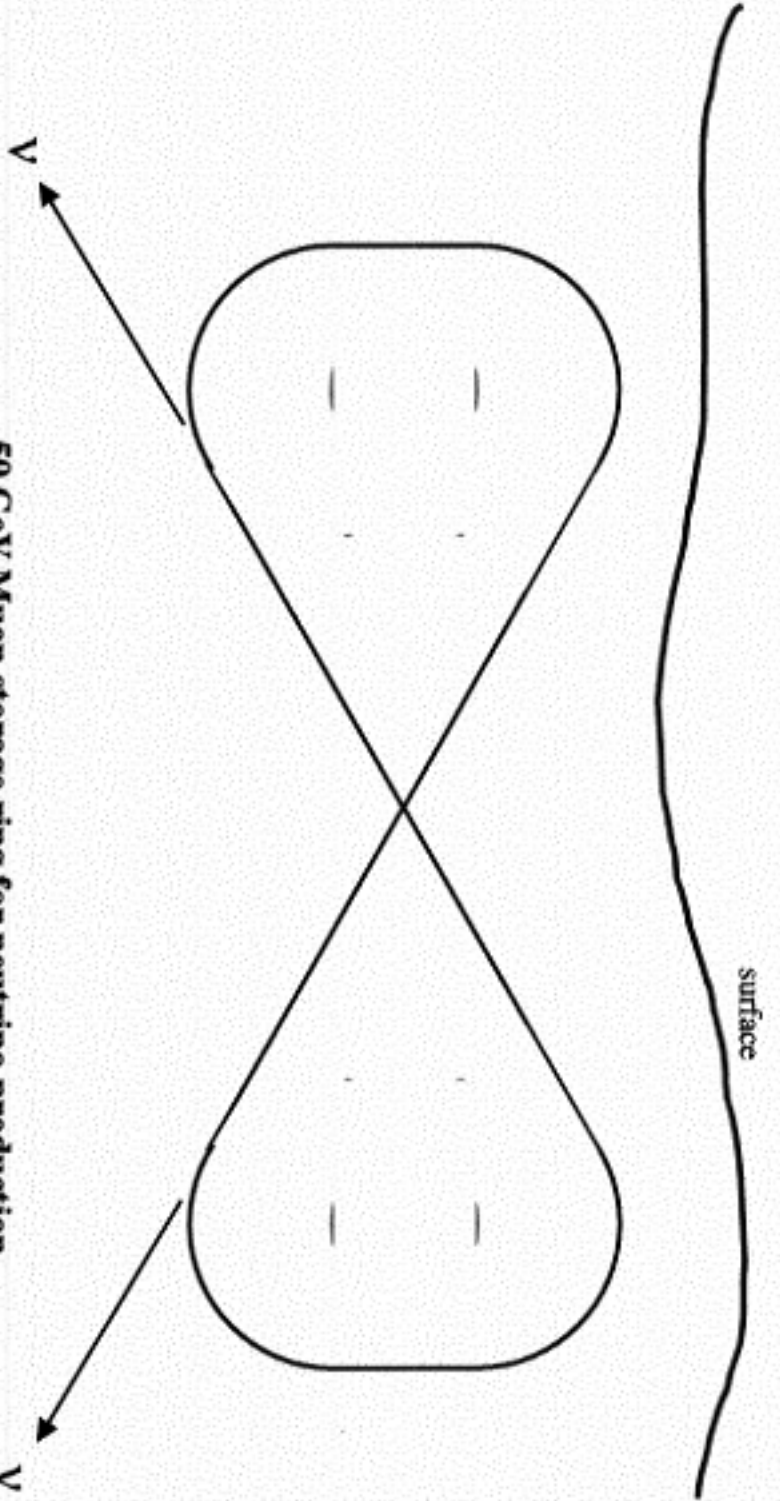
3 TeV × 3 TeV

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$\delta = \frac{\Delta p}{p}$	0.12%
No. of turns	1000
No. muons	$2 \times 10^{12}$
No. bunches	2
beam - beam tune shift	0.05

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 COLLIDER



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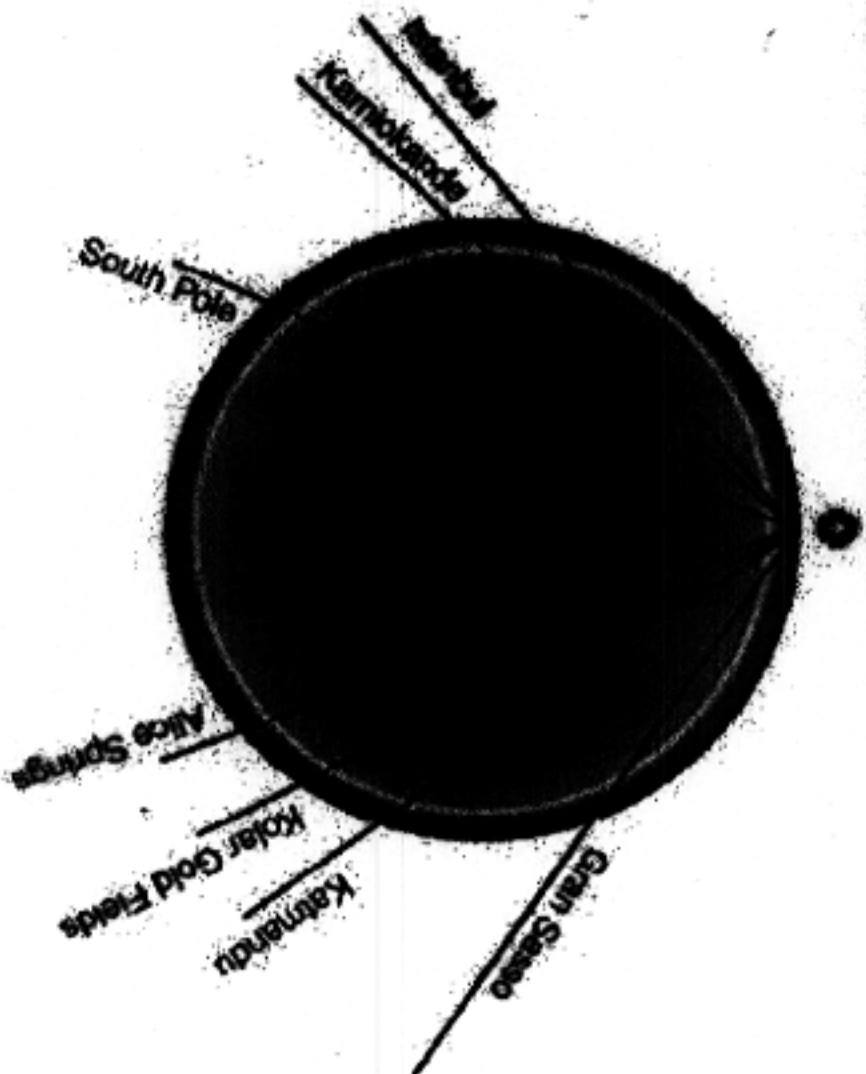
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## The Ultimate International Collaboration?



## Expected Event Rate

Rate is calculated for  $E_\mu = 50$  GeV and  $10^{20}$  muon decays per year pointing to the detector (1.5 MW driver), and oscillations are calculated assuming (the Super-K result) of  $\Delta m^2 = 3.5 \times 10^{-3} \text{ eV}^2/c^4$  and  $\sin^2 2\theta = 1$ . The detector is 1kT-year (and would surely be larger and run longer). [One kT of water is  $(33 \text{ ft})^3$ ]

Consider (just one example) Fermilab to Gran Sasso: 7332 km

$$\nu_\mu \rightarrow \nu_\tau \quad 410$$

$$\nu_\mu \rightarrow \nu_\mu \quad 490 \text{ (If no oscillations)}$$

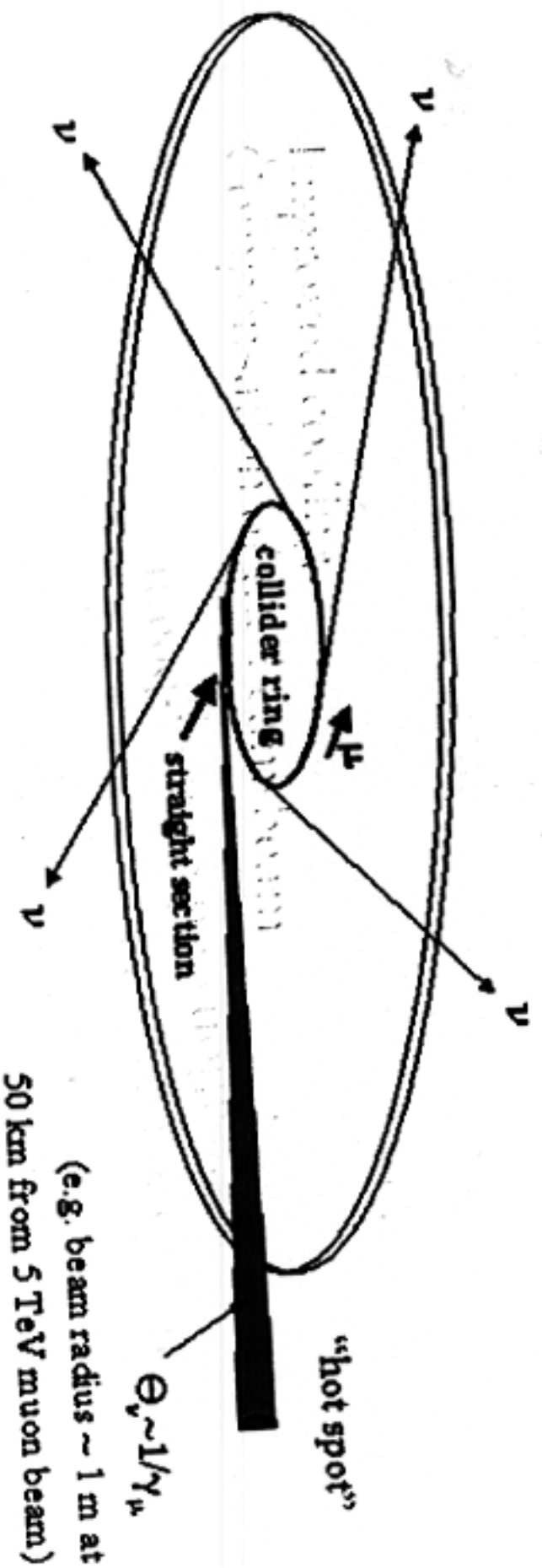
$$L + 2L$$

$$E + \frac{1}{2} E$$

$\rightarrow$  distance CP  
matter effects

Compare to Fermilab to Soudan (750 km), Minos, where the oscillations,  $\nu_\mu \rightarrow \nu_\tau$  are expected to be about 30 events per year. For this source the rate is  $1.4 \times 10^5$ .

# Neutrino Production at Muon Colliders



$\nu$  beam stronger at str. sections: e.g. even 0.1 m str. section is twice disk average





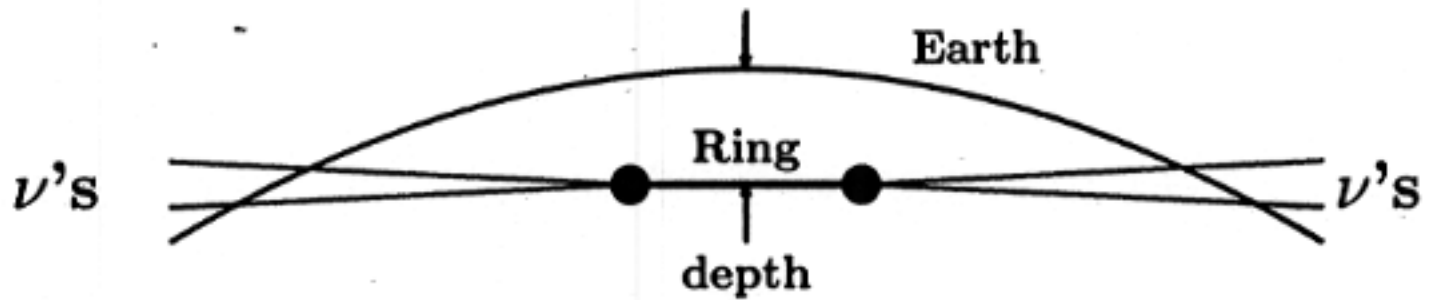
## Neutrino Background: Critical problem as energy increases

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- Radiation  $\sim (\text{Energy})^3 / \text{length}^2 \sim (\text{Energy})^3 / \text{depth}$
- Need to either wiggle beam to dilute effect, or build collider in isolated area, or
- Improved cooling— optical stochastic cooling?  
Compensation of the beam-beam interaction in the collider ring (lithium, plasma). Lowers average power and neutrino radiation.
- This and numerous other problems: Workshop on 10-100TeV muon colliders (27/9-1/10 1999, details at: <http://pubweb.bnl.gov/people/bking/heshop/>)
- *If technology works, 100TeV muons could share VLHC tunnel with 100TeV protons.*

27/9-1/10 1999

# NEUTRINO RADIATION



- Radiation  $\propto E^3/\text{length}^2 \propto E^3/\text{depth}$
- Use: 1/10 Federal limit = 10 mR/year

$\approx 3\%$   
of  
Natural  
Rad

THEN

- Negligible problem at 1.5 TeV
  - $\approx 1$  mR/year
- $E = 3$  TeV ok at 300 m depth
  - $\approx 10$  mR/year
- $E > 3$  TeV Requires:
  - Beam wobbles, and/or
  - Special Locations, and/or
  - Better Cooling (Optical Stochastic?)

M. Zolotover

## THE MOST CRITICAL ISSUES

### ● Target

- Heating → liquid metal?
- Splash?
- Motion in Magnet

### ● Capture RF

- Low Frequency (30-90 MHz)
- High Gradient (3-6 MV/m)
- High Radiation

### ● Cooling RF

- Higher Frequency (800 MHz)
- Very High Gradient (36 MV/m)

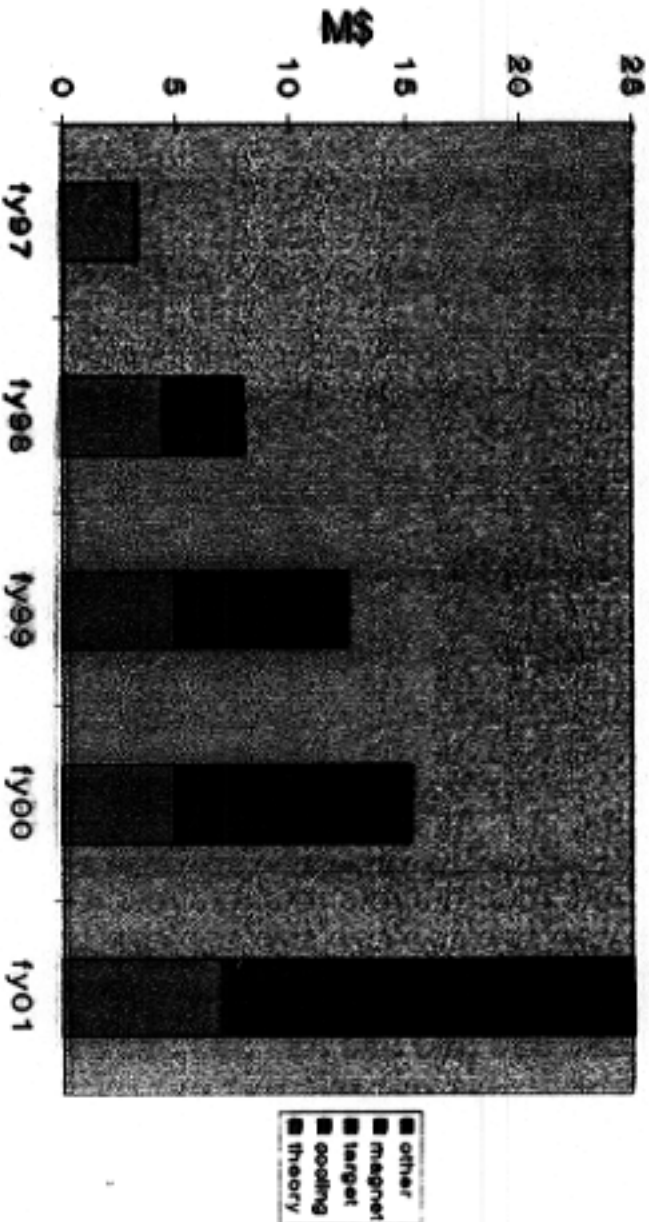
### ● Cooling Demonstrations

- Targets

# Short term funding needs

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- » These numbers are a first estimate. They do not include contingencies or EDIA.
- » Fiscal year 01 is very approximate, but indicates that increased funding will be needed.



# The Grand Scheme of Things

(As seen by muon beam enthusiasts)

1. **Lots of R and D**  
(Started: 1996)  
(Needed: 2000 + 5 to 10 years)
2. **Build a Neutrino Factory**  
(200X)
3. **Build a Higgs Factory Collider**  
(200X + 5 years = 20YY)
4. **Build a Few TeV Collider**  
(20YY + 10 years = 20ZZ)
5. **Build a 10-100 TeV Collider**  
(????)

(This should keep even our grandchildren's grandchildren busy)

# Conclusions

## For a Neutrino Factory:

1. **Most interesting physics**  
(We know almost nothing about the neutrino sector)
2. **Seems likely to "work"**
3. **Cost should not be "excessive"**  
(by US Congress criteria)
4. **Within (say) 5 years the R and D should be sufficiently advanced that a serious proposal can be made.**

## For a Muon Collider:

1. **Interesting physics even for a low energy machine (S coupling to a Higgs and a low  $dE/E$  can be achieved ( $3 \times 10^{-5}$ ))**
2. **Easier tolerances than linear colliders**
3. **A high energy (multi-TeV range) can be achieved without QED confusion**
4. **Perhaps the cost (\$/TeV) is not excessive**
5. **A fair amount of R and D is needed**