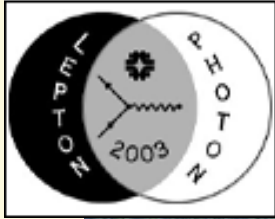


K. R. Schubert, TU Dresden
XXI Lepton-Photon Symposium
Fermilab, 12 Aug 2003



CKM Matrix Element Magnitudes

St. Model origin, invariants, and parametrisations of V_{CKM} .

$|V_{ud}|, |V_{us}|, |V_{cd}|, |V_{cs}|_1$: Unitary?

$|V_{cb}|, |V_{ub}|, |V_{td}|, |V_{ts}|, |V_{cs}|_2$: Unitary? CP-violating?

Parameter values without and with $\varepsilon(K^0)$ and $\sin 2\beta$

Many averaged results are my private guesses,
many references will only be given in the later write-up of this talk.

Yukawa Structure of the St. Model

$$L(\ell, q) = L_{kin} + L_{int} - \left[C_{\alpha\beta}^{(\ell)} \cdot \bar{\ell}_{R\alpha} \Phi^+ \begin{pmatrix} \nu_{L\beta} \\ \ell_{L\beta} \end{pmatrix} + C_{\alpha\beta}^{(d)} \cdot \bar{d}_{R\alpha} \Phi^+ \begin{pmatrix} u_{L\beta} \\ d_{L\beta} \end{pmatrix} + C_{\alpha\beta}^{(u)} \cdot \bar{u}_{R\alpha} \Phi^T \varepsilon \begin{pmatrix} u_{L\beta} \\ d_{L\beta} \end{pmatrix} + h.c. \right],$$

$$\Phi = \begin{pmatrix} \Phi_1 \\ \Phi_2 \end{pmatrix}; \quad \alpha, \beta = 1, 2, 3.$$

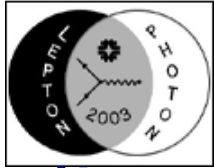
$C^{(u)}$ and $C^{(d)}$ cannot be diagonalised simultaneously since Glashow married $u_{L\alpha}$ and $d_{L\alpha}$ into doublets. The difference of the two „rotations“ in family space which diagonalize $C^{(u)}$ and $C^{(d)}$ is V_{CKM} .

$$\begin{pmatrix} u_L \\ d'_L \\ c_L \\ s'_L \\ t_L \\ b'_L \end{pmatrix} = V \begin{pmatrix} u'_L \\ d_L \\ c'_L \\ s_L \\ t'_L \\ b_L \end{pmatrix}$$

$$V V^+ = 1.$$

V was introduced 1973 by M. Kobayashi and T. Maskawa; is called V_{CKM} since 1987 in recognition of N. Cabibbo 1963.

St. Model allows arbitrary $C^{(u)}$ and $C^{(d)}$ \Rightarrow Standard weak interaction is not CP-invariant.



Invariants of the CKM matrix

In $\mathcal{L}_{\text{St.Model}}$, $\varphi(u_\alpha)$ and $\varphi(d_\beta)$ arbitrary $\Rightarrow V_{\alpha\beta}$ not observable,

$$u_\alpha \rightarrow u_\alpha \cdot e^{i\varphi_\alpha}, d_\beta \rightarrow d_\beta \cdot e^{i\varphi_\beta} \Rightarrow V_{\alpha\beta} \rightarrow V_{\alpha\beta} \cdot e^{i(\varphi_\alpha - \varphi_\beta)}$$

Observables are, i. e. invariants under phase transformations

$$1) \quad V_{\alpha\beta} V_{\alpha\beta}^* = |V_{\alpha\beta}|^2$$

$$2) \quad V_{\alpha\beta} V_{\alpha\delta}^* V_{\gamma\delta} V_{\gamma\beta}^*$$

$$3 \text{ et al.}) \quad V_{\alpha\beta} V_{\alpha\delta}^* V_{\gamma\lambda} V_{\gamma\beta}^* V_{\kappa\lambda} V_{\kappa\delta}^* \text{ et al.}$$

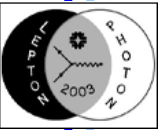
Parametrisations of the CKM matrix

$V_{\alpha\beta}$ has $2 \cdot 9 - 9 - 5 = 4$ observable parameters
and an infinite number of choices for these 4.

One choice: $|V_{us}|, |V_{cb}|, |V_{ub}|, \varphi(V_{ub}^* V_{ud} V_{cd}^* V_{cb})$.

L. Wolfenstein's $|V_{us}| = \lambda, |V_{cb}| = A \cdot \lambda^2,$

choice 1983: $|V_{ub}| \cdot \cos \varphi = A \cdot \lambda^3 \cdot \rho, |V_{ub}| \cdot \sin \varphi = A \cdot \lambda^3 \cdot \eta.$



$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix};$$

$$V V^+ = 1;$$

$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \left[\begin{pmatrix} 1 - \lambda^2/2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + o(\lambda^4) \right] \begin{pmatrix} d \\ s \\ b \end{pmatrix}.$$



V_{ud}	V_{us}	V_{ub}
V_{cd}	V_{cs}	V_{cb}
V_{td}	V_{ts}	V_{tb}

Three sources:

Super-allowed nuclear β^+ -decays

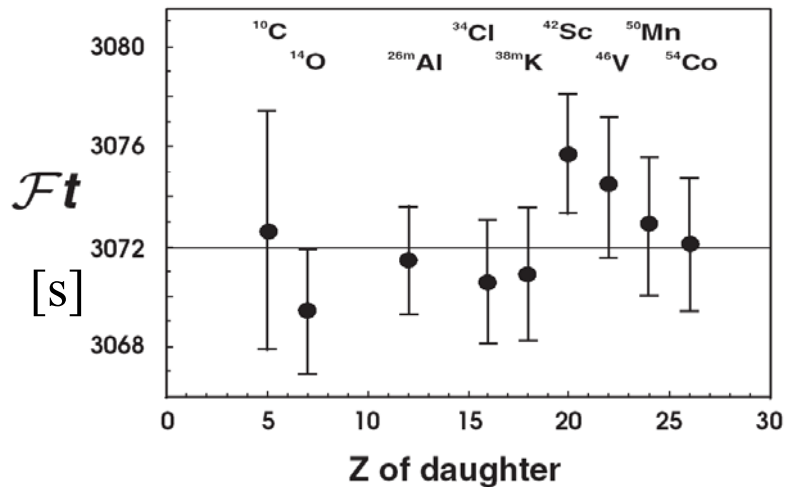
β^- decays of polarized neutrons

β^+ decay of the π^+

Super-allowed nuclear β^+ -decays:

$0^+ \rightarrow 0^+$ nuclear transitions within same isospin multiplet, pure V.

I. S. Towner and J. C. Hardy 2003:



$$Ft = (3072.2 \pm 0.9 \pm 1.1) \text{ s}$$

fit error and estimated error on δ_C

$$|V_{ud}|^2 = \frac{2 \pi^3 \ln 2}{m_e^5} \cdot \frac{1}{2 G_F^2 (1 + \Delta_{RV}) Ft}$$

G_F from μ decay, $\Delta_{RV} = (2.40 \pm 0.08)\%$

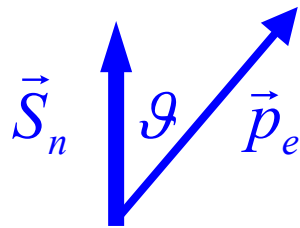
$$|V_{ud}| = 0.9740 \pm 0.0001_{\text{ft,exp}} \pm 0.0004_{\Delta} \pm 0.0003_{\text{Ft/ft}}$$

$$Ft = f \cdot t_{1/2} \cdot (1 + \delta'_R) \cdot (1 + \delta_{NS} - \delta_C)$$

$$|V_{ud}|_{\text{Nucl}} = 0.9740 \pm 0.0005$$

β^- decays of polarized neutrons:

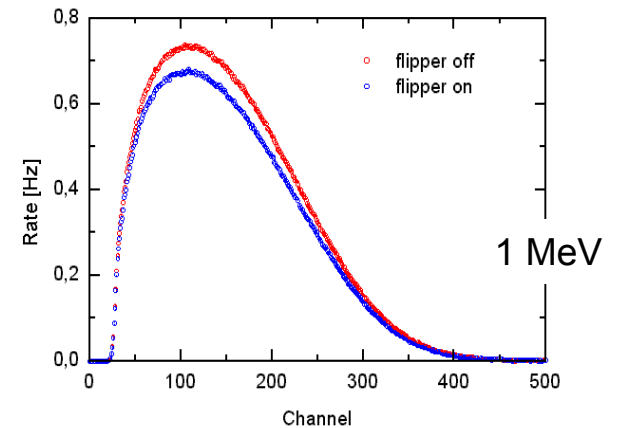
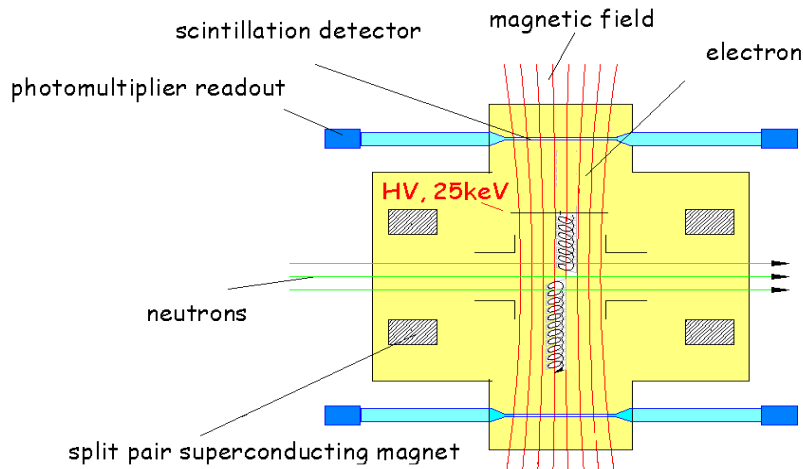
V and A transition because of $1/2^+ \rightarrow 1/2^+$. $G_V = G_F |V_{ud}|$, but j_A only partially conserved. Determine $G_A/G_V = \lambda$ experimentally!



$$W(\vartheta) = 1 + \frac{v}{c} \cdot P \cdot A \cdot \cos \vartheta, \quad A = \frac{-2\lambda(\lambda+1)}{1+3\lambda^2} + o(1\%)$$

$$\frac{1}{\tau_n} = \frac{m_e^5 \cdot G_F^2 \cdot |V_{ud}|^2}{2\pi^3} \cdot (1+3\lambda^2) \cdot f(1+\delta_R) \cdot (1+\Delta_{RV}).$$

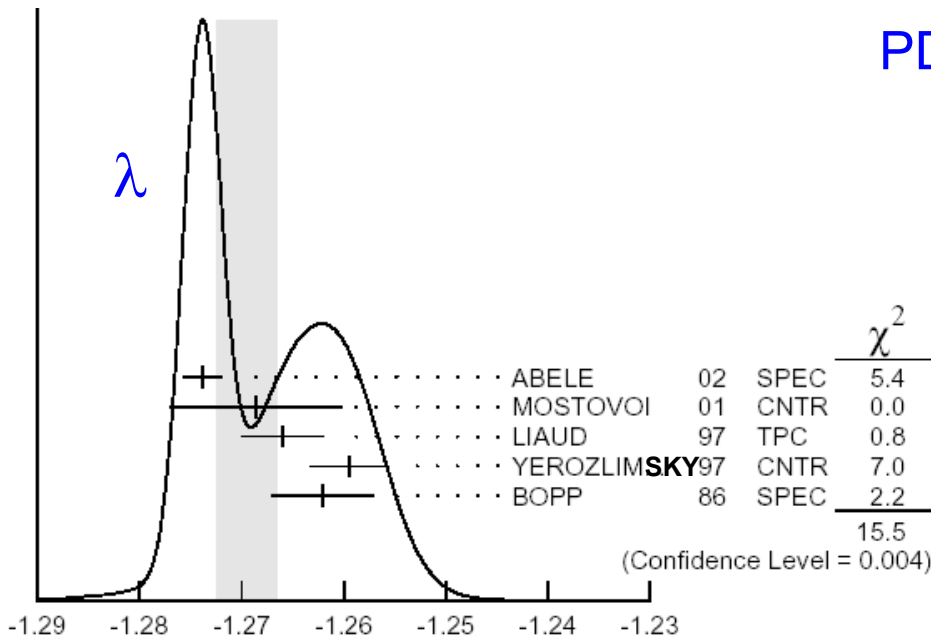
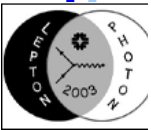
Most recent experiment is PERKEO-II at ILL Grenoble; neutrons of 25 K with $P = (98.9 \pm 0.3)\%$, periodical spin-flip. e-detector:



$$A = -0.1189 (7)$$

$$\lambda = G_A/G_V = -1.2739 (19)$$

PDG 2003: $\lambda = -1.2695 \pm 0.0029$
 (S = 2.0). $\tau_n = (885.7 \pm 0.8) \text{ s}$



P	A/A _{raw} - 1
0.989	0.02
0.97	-
0.98	0.15
0.70	0.30
0.98	0.13

$$|V_{ud}|_{\text{Nucl}} = 0.9740 \pm 0.0005$$

$$|V_{ud}|_n = 0.9741 \pm 0.0020$$

PERKEO-II (Abele 03, corrected) alone:

$$|V_{ud}|_n = 0.9717 \pm 0.0013$$

β decay of π^+ :

Recent experiment **PIBETA** at PSI; stopped π^+ ,
 $\pi^+ \rightarrow \pi^0 e^+ \nu_e$, detection of π^0 in CsI ball,
 normalisation with $e^+ \nu_e$. Preliminary result:

$$BF(\pi^+ \rightarrow \pi^0 e^+ \nu_e) = (1.044 \pm 0.007 \pm 0.009) 10^{-8}.$$

$$|V_{ud}|_\pi = 0.9765 \pm 0.0056$$

Summary of V_{ud} :

$$|V_{ud}|_{\text{Nucl}} = 0.9740 \pm 0.0005 \quad (1)$$

$$|V_{ud}|_n = 0.9741 \pm 0.0020 \quad S = 2.0 \quad (2)$$

$$\text{PERKEO-II alone: } |V_{ud}|_n = 0.9717 \pm 0.0013 \quad (3)$$

$$|V_{ud}|_\pi = 0.9765 \pm 0.0056 \quad (4)$$

Prospects: PIBETA will not reach competitive precision, ± 0.0030 ?

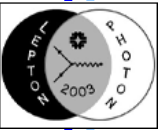
$\sigma(V_{ud, \text{Nucl}})$ dominated by radiative corr.

$\sigma(V_{ud, n})$ dominated by experiment. New experiments are underway,

PERKEO 03, „new PERKEO“ 05 , LANL, SNS, Gatchina/PSI

My average: (1) + (3) + (4) with $S = 1.3 \Rightarrow$

$$|V_{ud}| = 0.9737 \pm 0.0007$$



V_{ud}	V_{us}	V_{ub}
V_{cd}	V_{cs}	V_{cb}
V_{td}	V_{ts}	V_{tb}

Sources: Old K_{l3} decays, new K_{l3} decays, hyperon β -decays, τ decays

K_{l3} decays: $K^+ \rightarrow \pi^0 l^+ \nu_e$ and $K^0 \rightarrow \pi^- l^+ \nu_e$, $0^- \rightarrow 0^-$, pure V

$$\Gamma_i = \frac{m_K^5 \cdot G_F^2 \cdot |V_{us}|^2}{192 \pi^3} \cdot C_i^2 \cdot |f_+(0)|^2 \cdot I_i(\lambda_+, \lambda_0) \cdot (1 + \delta_R), \quad f_{+,0}(q^2) = f_+(0) \cdot \left(1 + \lambda_{+,0} \frac{q^2}{m_\pi^2} + \dots \right)$$

$$C_i = 1 / \sqrt{2} \text{ for } K^+ \text{ and } K_L^0$$

Mode	BR (%)	$10^3 \lambda_+$	$10^3 \lambda_0$
K_{e3}^+	4.87 ± 0.06	27.8 ± 1.9	
K_{e3}^0	38.79 ± 0.27	29.1 ± 1.8	
$K_{\mu 3}^+$	3.27 ± 0.06	33 ± 10	4 ± 9
$K_{\mu 3}^0$	27.18 ± 0.25	33 ± 5	27 ± 6

$$\tau_{K^\pm} = (1.2384 \pm 0.0024) \times 10^{-8} \text{ s}$$

$$\tau_{K_L} = (5.17 \pm 0.04) \times 10^{-8} \text{ s}$$

← Exp. input since ~1980.

Leutwyler and Roos 1984:

$$f_+^{K^0}(0) = 0.961, \quad f_+^{K^+}(0) = 0.982.$$

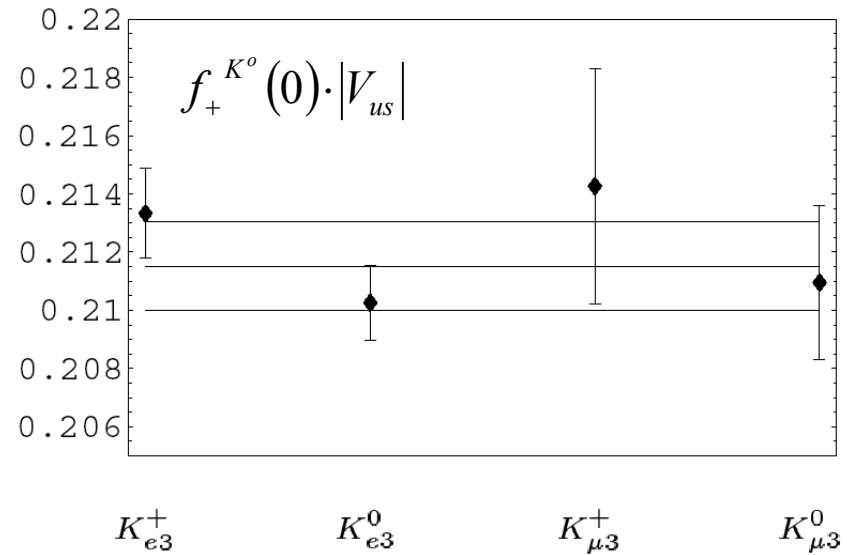
$$|V_{us}|_{Kl3,old} = 0.2196 \pm 0.0023$$

New theoretical inputs

increase V_{us} by $+ 0.2\% \pm 0.2\%$

V. Cirigliano 2003:

$$|V_{us}|_{\text{old K13}} = 0.2201 \pm 0.0024$$



New K_{l3} results: Final K_{e3}^+ result of BNL-E865, hep-ex/0305042
Preliminary KLOE results on three K_{l3}^0 rates

BNL-E865: Aim $K^+ \rightarrow \pi^+ \mu^+ e^-$. Dedicated run for $K^+ \rightarrow \pi^0 e^+ \nu_e$ during one week 1998, $\pi^0 \rightarrow e^+ e^- \gamma$. Normalised to $K^+ \rightarrow \pi^+ \pi^0$, $\pi^+ \pi^0 \pi^0$. Result:

$$\begin{aligned} \text{BF}(K^+ \rightarrow \pi^0 e^+ \nu_e) &= (5.13 \pm 0.02 \pm 0.09 \pm 0.04)\% \\ &= (1.053 \pm 0.024) \cdot \text{BF}(\text{old}), \mathbf{2.2\sigma} \end{aligned}$$

$$\lambda_+ = \lambda_+(\text{old})$$

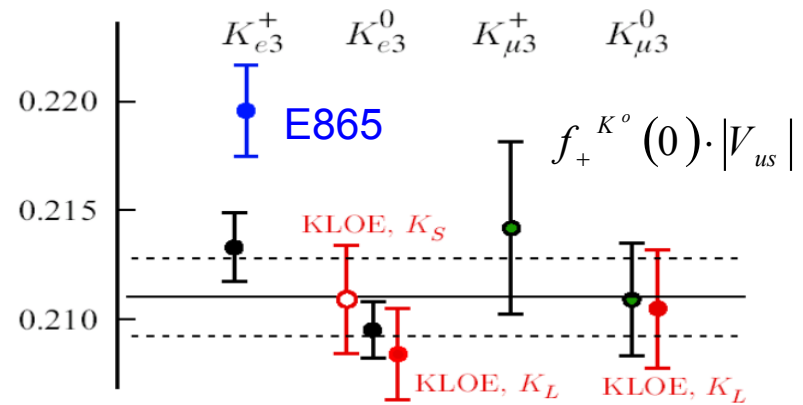


$$|V_{us}|_{K_{13,old}} = 0.2201 \pm 0.0016 \pm 0.0018$$

$$|V_{us}|_{E865} = 0.2285 \pm 0.0023 \pm 0.0019$$

using Cirigliano's $f(0)(1+\delta)$,

3.0 σ higher than old K^+K^0 average



$$|V_{us}|_{K_{13,old}+E865} = 0.2220 \pm 0.0019 \text{ (S=1.5)} \pm 0.0018$$

KLOE: $e^+e^- \rightarrow \phi(1020) \rightarrow K_S K_L$

hep-ex/0307016 gives preliminary K_{13}^0 results from 78 / pb.

Values only given in this plot (\uparrow), in agreement with $K_{13,old}$

Hyperon Decays: revisited by N. Cabibbo et al, hep-ph/0307298.

Exp. data from $n \rightarrow p e \nu$, $\Lambda \rightarrow p e \nu$, $\Sigma^- \rightarrow n e \nu$, $\Xi^- \rightarrow \Lambda e \nu$, and $\Xi^0 \rightarrow \Sigma^+ e \nu$.

New: SU(3) breaking values of „ g_A/g_V “ = $g_1(0)/f_1(0)$ taken from experiment, compatible with no SU(3) breaking. Using $f_1(0) = 1.000$:

$$|V_{us}|_{\text{Hyperons}} = 0.2250 \pm 0.0027. \text{ Unknown } f(0) \text{ error.}$$

Tau decays: $\Gamma(\tau \rightarrow K n\pi \nu) / \Gamma(\tau \rightarrow \text{had } \nu)$ is sensitive to $|V_{us}|$.

Using ALEPH data and $m_s(2 \text{ GeV}) = (105 \pm 20) \text{ MeV}$, Gamiz et al find

$$|V_{us}|_{\tau} = 0.2179 \pm 0.0044_{\text{exp}} \pm 0.0009_{\text{th}}$$

Dominant error is experimental. Better measurements of rates and mass moments would give both m_s and $|V_{us}|$.

Summary of V_{us}

Prospects for K_{l3} : Final results from KLOE, also on K^+ decays, will come soon. NA48 & KTeV have these decays recorded, but not analysed.

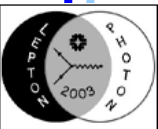
for Hyperons: More theoretical work needed.

for τ decays: BABAR and BELLE have 10^8 $\tau\tau$ events, should look into their potential to get $\Gamma(\tau \rightarrow K n\pi \nu)$ and mass moments.

My average

from old K_{l3} , E865, and τ decays:

$$|V_{us}| = 0.2210 \pm 0.0023$$



V_{ud}	V_{us}	V_{ub}
V_{cd}	V_{cs}	V_{cb}
V_{td}	V_{ts}	V_{tb}

Old source: Production of dimuon pairs by neutrinos on nuclei

$$\begin{aligned} \nu_\mu d &\rightarrow \mu^- c, & c &\rightarrow s \mu^+ \nu_\mu \\ \bar{\nu}_\mu \bar{d} &\rightarrow \mu^+ \bar{c}, & \bar{c} &\rightarrow \bar{s} \mu^- \bar{\nu}_\mu \end{aligned}$$

with $B = BF(c \rightarrow \mu^+ X)$:

$$\frac{\sigma(\nu \rightarrow \mu^+ \mu^-) - \sigma(\bar{\nu} \rightarrow \mu^+ \mu^-)}{\sigma(\nu \rightarrow \mu^-) - \sigma(\bar{\nu} \rightarrow \mu^+)} = \frac{3}{2} \cdot B \cdot |V_{cd}|^2$$

$$= (0.41 \pm 0.07) \% \quad \text{CDHS 1982}$$

$$= (0.534 \pm 0.021^{+0.025}_{-0.051}) \% \quad \text{CCFR 1995}$$

$$B = 0.099 \pm 0.012 \quad \Rightarrow$$

$$|V_{cd}| = 0.224 \pm 0.016$$

Prospects: CLEO-c



V_{ud}	V_{us}	V_{ub}
V_{cd}	V_{cs}	V_{cb}
V_{td}	V_{ts}	V_{tb}

Sources: (1) β decays of D mesons and
(2) decays of real W^\pm

$$D^+ \rightarrow \bar{K}^0 e^+ \nu \text{ and } D^0 \rightarrow K^- e^+ \nu: \quad \Gamma = \frac{B}{\tau} = \frac{G_F^2 \cdot |V_{cs}|^2}{192 \pi^3} \cdot \Phi \cdot |f(0)|^2 \cdot (1 + \delta_R)$$

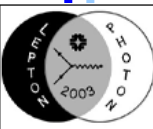
Constituent quark models and QCD sumrules:

$$f(0) = 0.7 \pm 0.1$$

$$\Rightarrow |V_{cs}| = 1.04 \pm 0.16$$

2nd method, much more precise, needs 3rd quark family,
will be discussed later.

Unitarity check of the udsc matrix:


$$\begin{array}{ccc} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{array}$$

$$\text{Inputs: } |V_{ud}| = 0.9737 \pm 0.0007$$

$$|V_{us}| = 0.2210 \pm 0.0023$$

$$|V_{cd}| = 0.224 \pm 0.016$$

$$|V_{cs}| = 1.04 \pm 0.16$$

$$|V_{ud}|^2 + |V_{us}|^2 = 0.9969 \pm 0.0017 \quad -1.8 \sigma$$

$$|V_{cd}|^2 + |V_{cs}|^2 = 1.13 \pm 0.33 \quad +0.4 \sigma$$

$$|V_{ud}|^2 + |V_{cd}|^2 = 0.9983 \pm 0.0073 \quad -0.2 \sigma$$

$$|V_{us}|^2 + |V_{cs}|^2 = 1.13 \pm 0.33 \quad +0.4 \sigma$$

$$|V_{ud}V_{cd}| - |V_{us}V_{cs}| = -0.012 \pm 0.039 \quad 0.3 \sigma$$

$$|V_{ud}V_{us}| - |V_{cd}V_{cs}| = -0.018 \pm 0.040 \quad 0.4 \sigma$$

From this unitarity check we cannot predict a 3rd family. Fit:

$$\lambda_{\text{Wolfenstein}} = 0.2235 \pm 0.0033$$

$$(S = 1.8)$$



$$\lambda = 0.2235 \pm 0.0033$$

($\pm 1.5\%$)



V_{ud}	V_{us}	V_{ub}
V_{cd}	V_{cs}	V_{cb}
V_{td}	V_{ts}	V_{tb}

Source: Inclusive and exclusive semileptonic B-meson decays

Inclusive decays:

$$\Gamma(B \rightarrow l \nu X) = \Gamma(b \rightarrow l \nu c) + \Gamma(b \rightarrow l \nu u) + o(\Lambda_{QCD}^2 / m_b^2)$$

Primary information:
± 0.8%

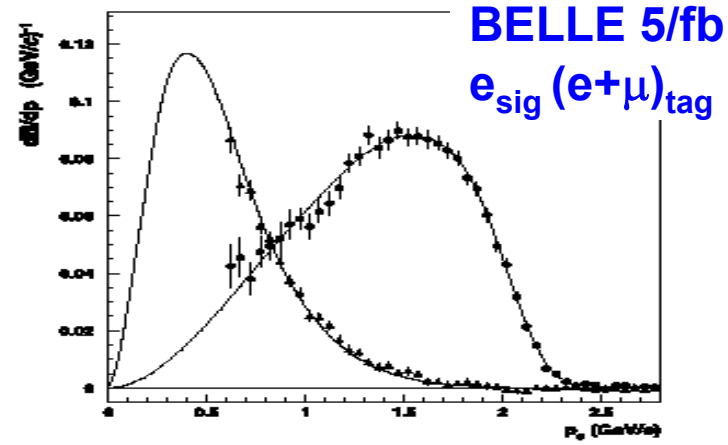
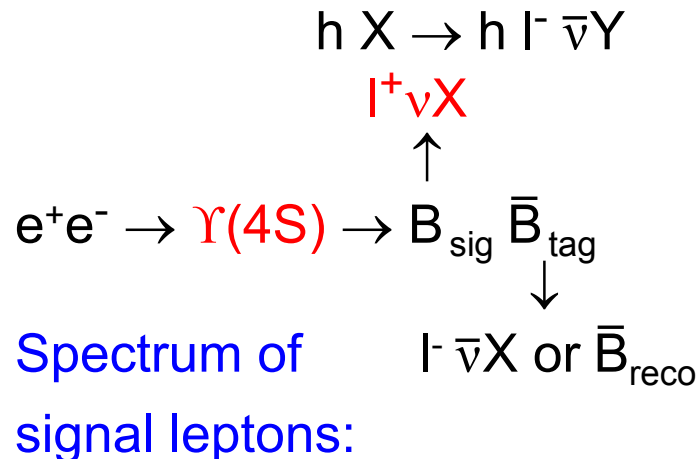
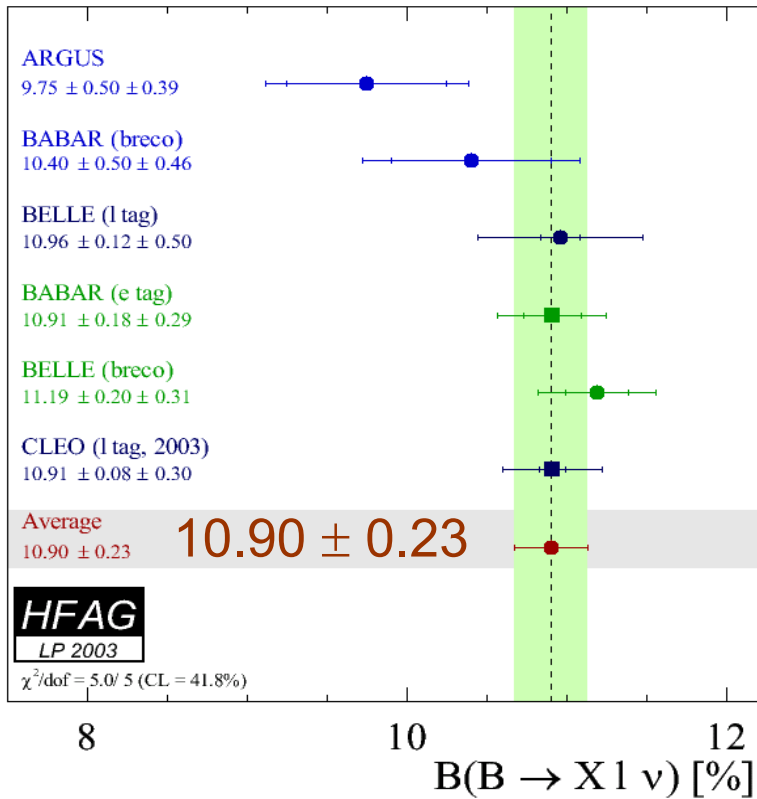
$\tau(B^0)$	1.534 ± 0.013 ps
$\tau(B^+)$	1.653 ± 0.014 ps

HFAG
07/03

data from ALEPH, BABAR, BELLE, CDF, DELPHI, L3, OPAL, SLD

$$\Gamma(b \rightarrow e \nu X) = \frac{BF(b \rightarrow e \nu X)}{\tau(b)} = \frac{G_F^2 \cdot m_b^5}{192 \pi^3} \cdot \left(\Phi\left(\frac{m_u}{m_b}\right) \cdot |V_{ub}|^2 + \Phi\left(\frac{m_c}{m_b}\right) \cdot |V_{cb}|^2 \right) + c(\alpha, \alpha_s)$$

Next information: $BF(B \rightarrow l \nu X)$



Integral over spectrum $\Rightarrow BF$,

98% $b \rightarrow c$, 2% $b \rightarrow u$, $\sigma_{BF}(V_{cb}) = 1.1\%$, $\sigma_\tau(V_{cb}) = 0.4\%$.

1982 spectrum given by ACCMM model, $d\Gamma/dp_l = f(m_b, m_c, p_F, \alpha_s)$.

V_{cb} with $\sigma(V_{cb}) \approx 10\%$. Today QCD, i.e. HQET and OPE:

$m_b \rightarrow \bar{\Lambda}$, $p_F \rightarrow \lambda_1$, $m_c \rightarrow$ substituted, and more parameters $\lambda_2, \rho_i, \tau_i \dots$

HQET gives:
$$\frac{d^3\Gamma(B \rightarrow l\nu X_c)}{dm_X^2 dE_l dq^2} = f(m_X^2, E_l, q^2 | m_B, |V_{cb}|, \alpha_s, \bar{\Lambda}, \lambda_1, \lambda_2, \dots)$$

No m_c since
$$m_B - m_b + \frac{\lambda_1 + 3\lambda_2}{m_b} = \bar{\Lambda} = m_D - m_c + \frac{\lambda_1 + 3\lambda_2}{m_c}$$

Of special interest are the moments

M_{ijk} of f . M_{000} :

$$\Gamma(B \rightarrow l\nu X_c) = \frac{G_F^2 |V_{cb}|^2}{192 \pi^3} \cdot 0.369 \cdot m_B^5 \cdot \left[1 - 1.54 \frac{\alpha_s}{\pi} - 1.65 \frac{\bar{\Lambda}}{m_B} \left(1 - 0.87 \frac{\alpha_s}{\pi} \right) - 0.95 \frac{\bar{\Lambda}^2}{m_B^2} - 3.18 \frac{\lambda_1}{m_B^2} + 0.02 \frac{\lambda_2}{m_B^2} + o\left(\frac{\Lambda_{QCD}}{m_B}\right)^3 \right]$$

Bases are duality, HQET, OPE. Local duality predicts results for more low moments like $\langle m_X^2 \rangle = M_{100}/M_{000}$, $\langle (m_X^2)^2 \rangle = M_{200}/M_{000}$, $\langle E_l \rangle = M_{010}/M_{000}$

Comparing measurements and calculations of „low“ M_{ijk} tests goodness of local duality and expansions, and determines λ_1 , $\bar{\Lambda}$, $|V_{cb}|$...

OPE and duality are not valid „too locally“, i.e. „high“ moments and the full $d^3\Gamma$ are not determining λ_1 , $\bar{\Lambda}$, $|V_{cb}|$...



Moment measurements:

CLEO, DELPHI, BABAR



DELPHI 2003 determines M_{i00} by reconstructing $B \rightarrow D^{**} l\nu$ events from 34 M Z at LEP. $\langle m_x^2 - \bar{m}_D^2 \rangle = (0.647 \pm 0.046 \pm 0.093) \text{ GeV}^2$,

$\bar{m}_D = (m_D + 3m_{D^*})/4$. Also results for M_{200} , M_{300}

2002 they obtained $\langle E_l \rangle = (1.383 \pm 0.012 \pm 0.009) \text{ GeV}$, also M_{020} , M_{030} .

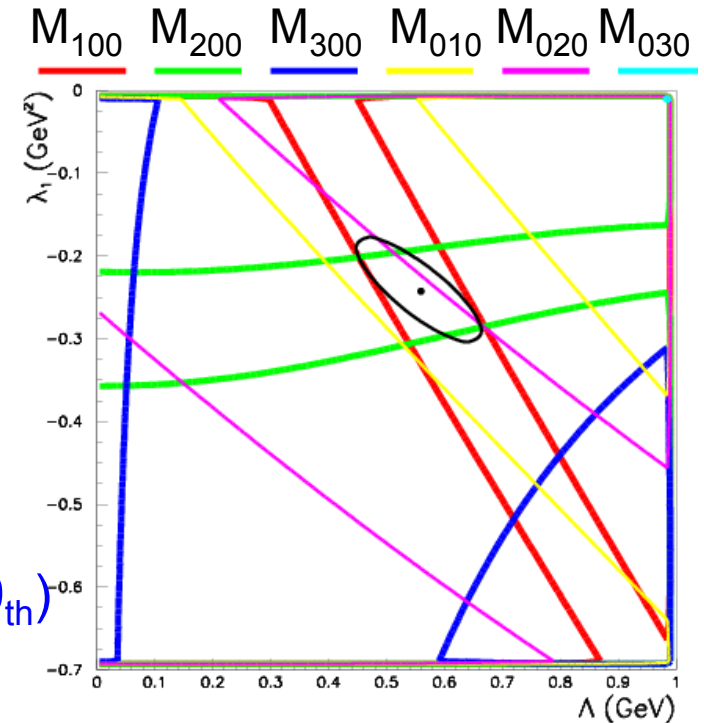
They fit in two mass schemes, with \overline{MS} scheme:

Fit Parameter	Fit Values	Fit Uncertainty	Syst. moments	Syst. theory
$\bar{\Lambda}$ (GeV)	0.542	± 0.065	± 0.087	± 0.04
λ_1 (GeV ²)	-0.238	± 0.055	± 0.028	± 0.06

With kinetic scheme:

$|V_{cb}| = 0.0429 (1 \pm 0.012_{\Gamma_{sl}} \pm 0.019_{fit} \pm 0.010_{th})$

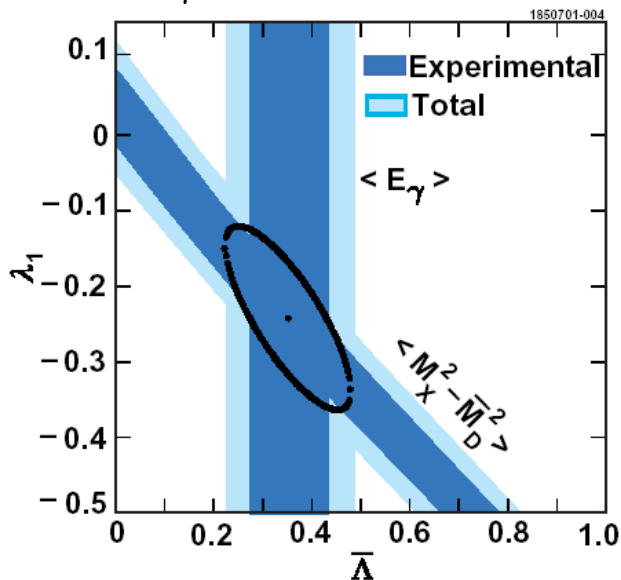
$BF(B \rightarrow l\nu X)$ readjusted to 10.9%



Because of the high B-meson boost, DELPHI moments in full m_x, E_l, q^2 space, $E_l^* \geq 0$. Different for CLEO and BABAR.

CLEO 2001 results:

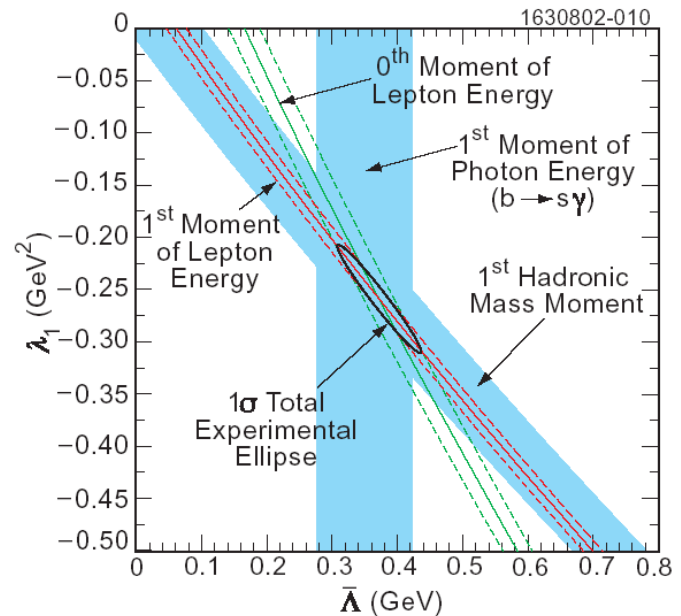
$\langle m_x^2 - \bar{m}_D^2 \rangle (E_l > 1.5 \text{ GeV})$
 $= (0.251 \pm 0.023 \pm 0.062) \text{ GeV}^2$
 and $\langle E_\gamma \rangle$ from $b \rightarrow s\gamma$:



$$|V_{cb}|^{(*)} = 0.0414 (1 \pm 0.012_{\Gamma_{sl}} \pm 0.022_{fit} \pm 0.020_{th})$$

(*) $BF(B \rightarrow l\nu X)$ re-adjusted to 10.9%

from E_l spectrum,
 $M_{010} (E_l > 1.5 \text{ GeV})$ and
 $M_{000} (> 1.7 \text{ GeV}) / M_{000} (> 1.5 \text{ GeV})$

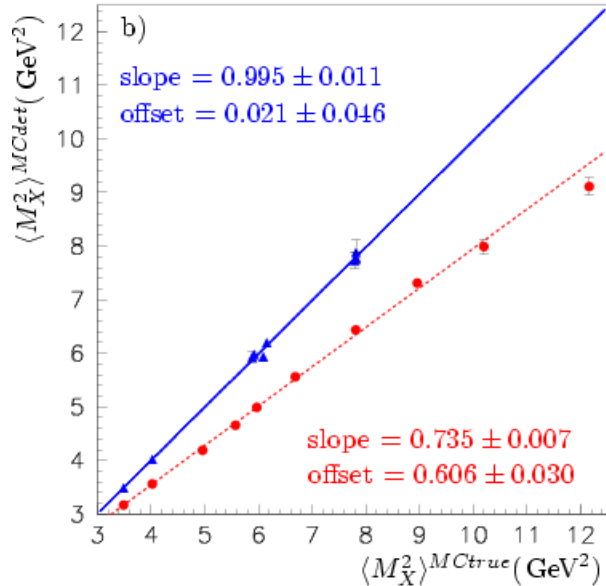
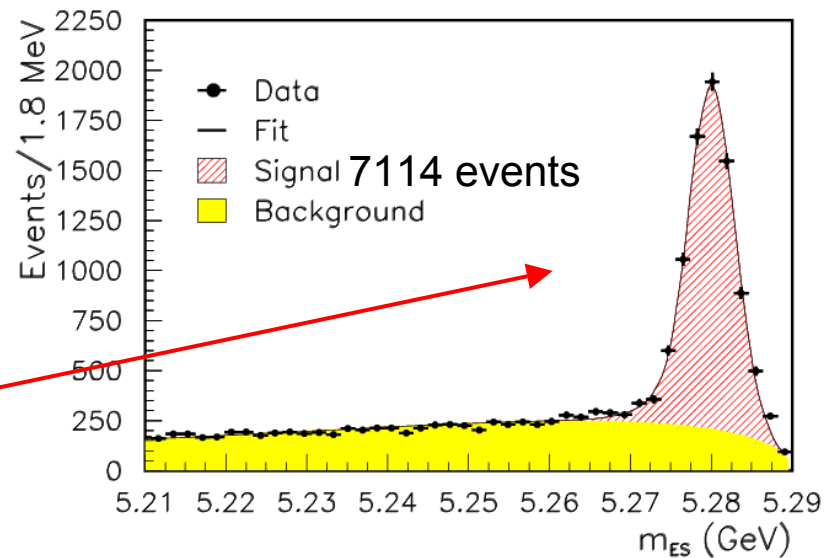


$$|V_{cb}|^{(*)} = 0.0418 (1 \pm 0.012_{\Gamma_{sl}} \pm 0.012_{fit} \pm 0.022_{th})$$

No combined fit performed.

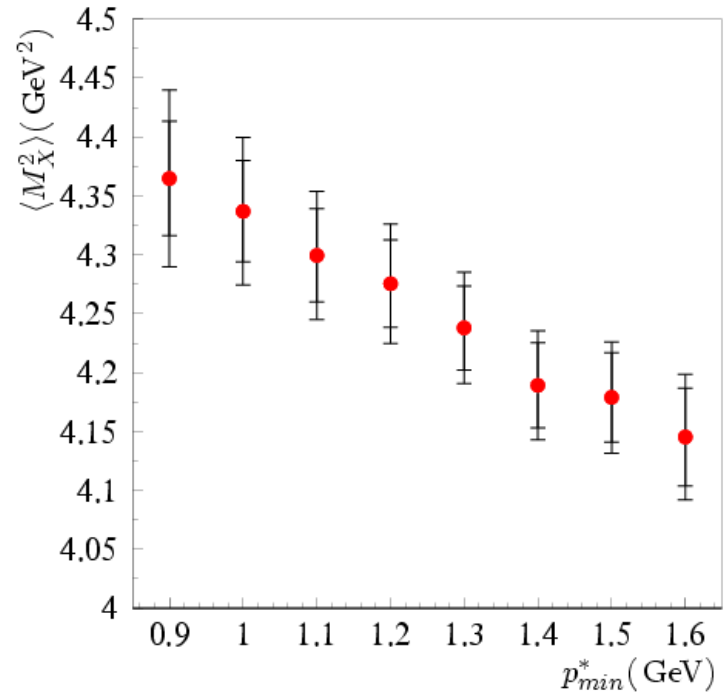
BABAR 2003 results:

Moments M_{100} with $E_l > 0.9 \dots 1.6$ GeV, obtained from 89 M $B\bar{B}$ with B_{tag} fully reconstructed, e and μ in B_{signal} , $E_l > 0.9$ GeV. $\tilde{m}_{X,\text{signal}}$ from fit to p_{miss} and m_{obs} $\langle \tilde{m}_X^2 \rangle \rightarrow \langle m_X^2 \rangle$ using MC:



Very small model dependence!

Obtained moments M_{100} :





BABAR fits HQET parameters
in 3 schemes, here pole mass \Rightarrow

quotes $|V_{cb}|$ from 1S scheme:

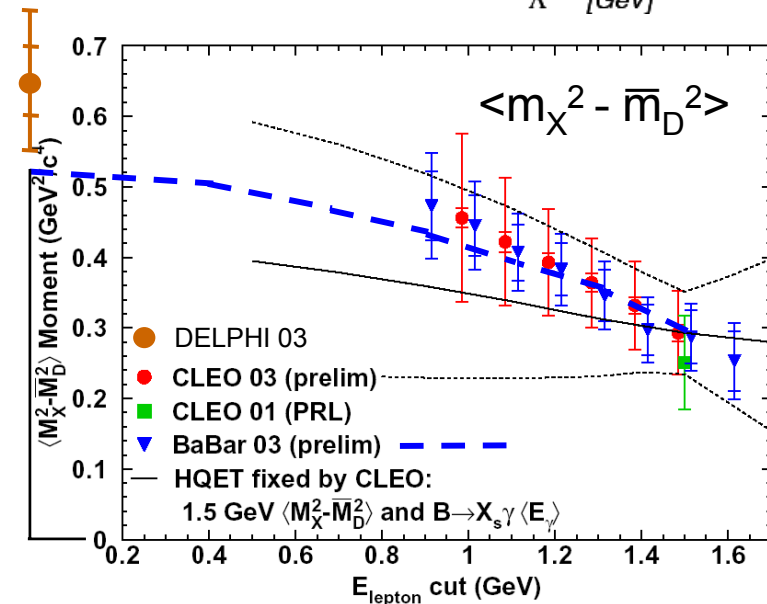
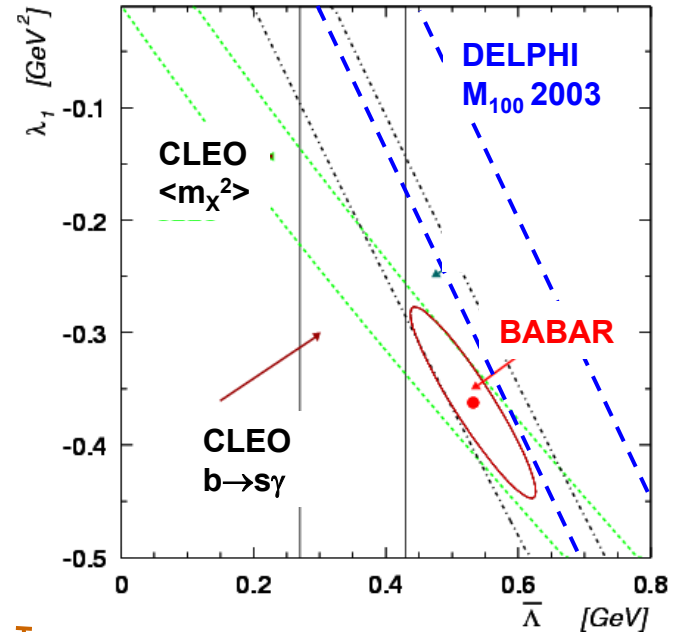
$$0.0421(1 \pm 0.025_{\text{exp}} \pm 0.017_{\text{th}})$$

CLEO 2003:

~ 10 M $B\bar{B}$, $p_{\text{miss}} = p_{e^+e^-} - p_{\text{obs}} = p_\nu$
 $|M_{\text{miss}}^2/2E_\nu| < 0.35$ GeV, only 1 e or μ ,
 m_X^2 , q^2 , E_1 for each event,
 $\langle m_X^2 \rangle$ from fit in 3 dimensions
to MC sum of 1ν (D, D*, D**, nonres, u)

Result:

No new fit of $\bar{\Lambda}$, λ_1 , $|V_{cb}|$.



Summary V_{cb} inclusive:

Moment measurements

of
$$\frac{d^3\Gamma(B \rightarrow l\nu X_c)}{dm_X^2 dE_l dq^2}$$

and HQET/OPE offer the potential to determine $|V_{cb}|$ with $\sigma < 2\%$.

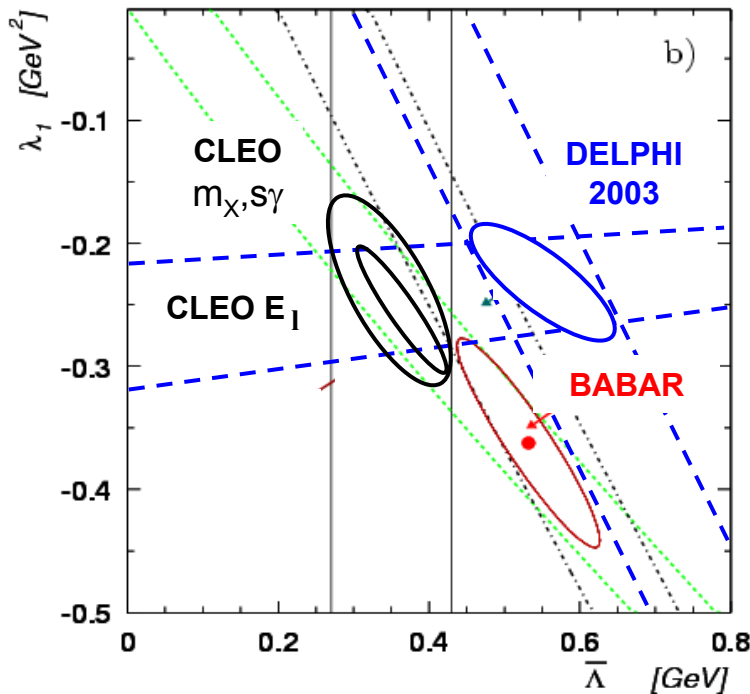
Duties for experiment:

Identify inconsistency areas.

for theory: Identify best scheme

(1S?), get terms with α_s/m_b^2

and more $1/m_b^3$ and α_s^2 terms ...



- $|V_{cb}|_{incl} = 0.0429 (1 \pm 0.012_{\Gamma_{Sl}} \pm 0.019_{fit} \pm 0.010_{th})$ DELPHI, kin
- $0.0414 (1 \pm 0.012_{\Gamma_{Sl}} \pm 0.022_{fit} \pm 0.020_{th})$ CLEO m, pole mass
- $0.0418 (1 \pm 0.012_{\Gamma_{Sl}} \pm 0.012_{fit} \pm 0.022_{th})$ CLEO E, pole mass
- $0.0421 (1 \pm 0.025_{exp} \pm 0.017_{th})$ BABAR, 1S

My average:

$$|V_{cb}|_{incl} = 0.0421 \pm 0.0013 \text{ (3.0\%)}$$

Exclusive V_{cb} determination: from $\frac{d\Gamma(B^0 \rightarrow D^{*-} \ell \nu)}{dw}$; $w = \frac{m_{D^*}^2 + m_D^2 - q^2}{2m_{D^*}m_D}$

new results submitted to LP03 by **DELPHI** and **BABAR**

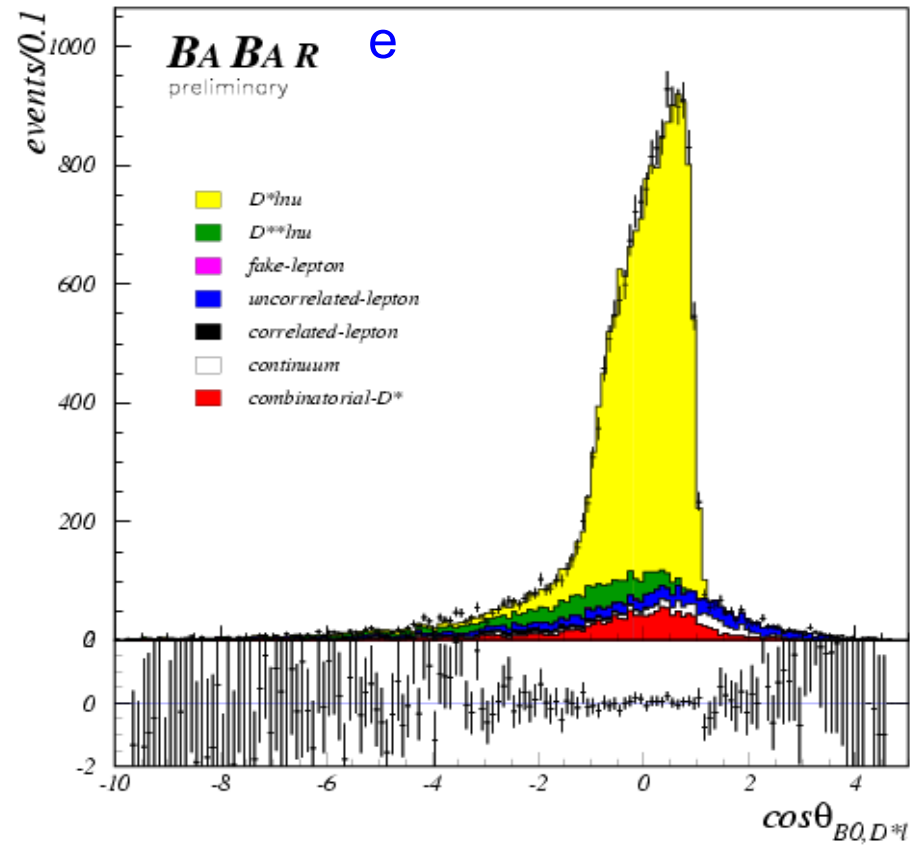
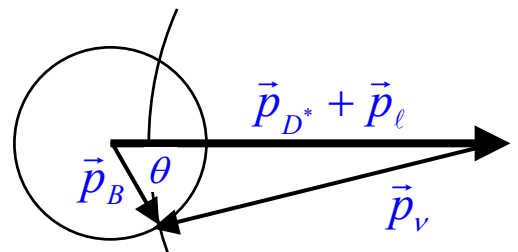
both with full reconstruction $D^{*+} \rightarrow D^0 \pi^+$, $D^0 \rightarrow K^- \pi^+$, $K^- \pi^+ \pi^+ \pi^-$, $K^- \pi^+ \pi^0$

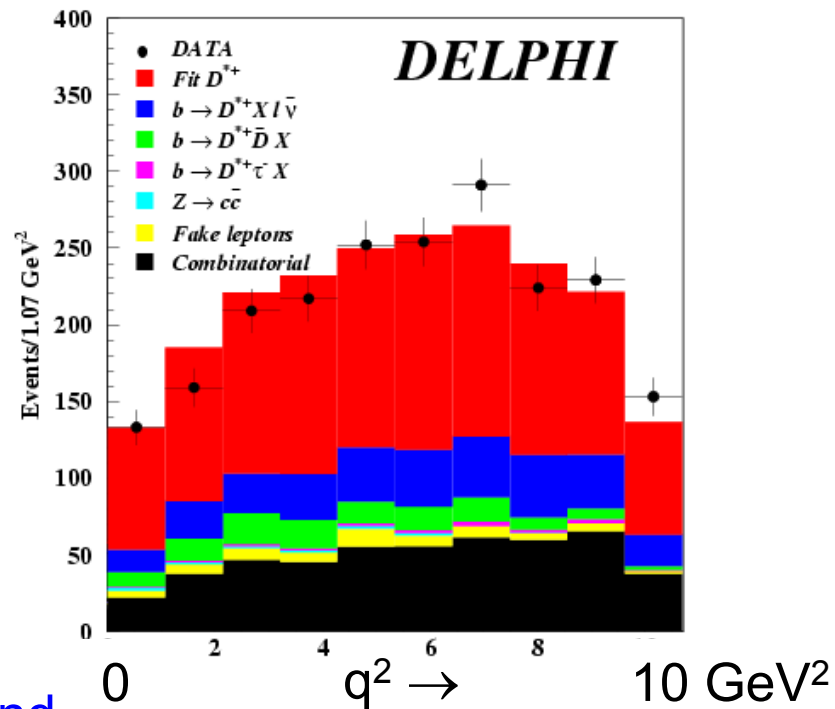
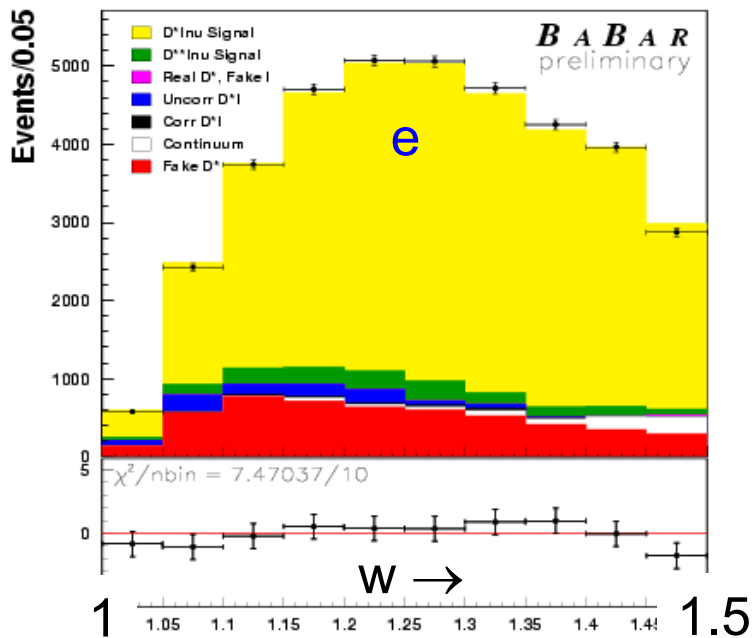
DELPHI 3.4 M Z, 1688 ev. (e+μ), BABAR 86 M $\Upsilon(4S)$, 55700 (e+μ)

Delicate background from D^{**} .

DELPHI uses hemisphere and vertex separation to identify extra tracks from B_{sig}

BABAR uses $\cos \theta_{B,D^*l}$



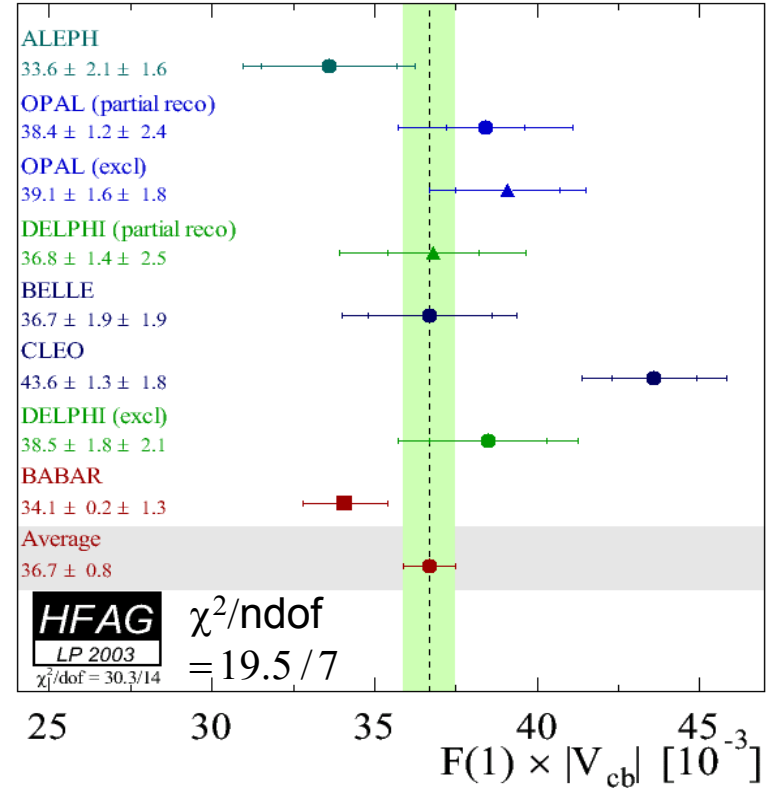
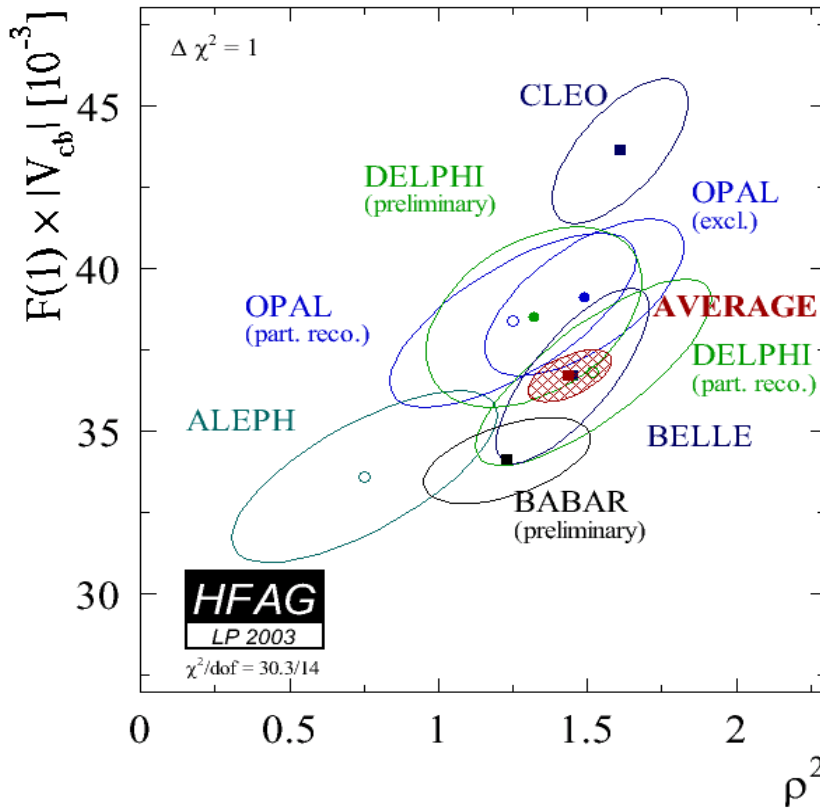


Advantage of BABAR: less background,
of DELPHI: large acceptance also at q^2_{max} , i.e. $w = 1$. Results:

	DELPHI	BABAR
$10^3 V_{cb} \cdot F(1)$	$39.2 \pm 1.8 \pm 2.2$	$34.0 \pm 0.2 \pm 1.3$
ρ_{A1}^2	$1.32 \pm 0.15 \pm 0.33$	$1.23 \pm 0.02 \pm 0.28$
$BF(B^0 \rightarrow D^* l \nu) \%$	$5.90 \pm 0.22 \pm 0.48$	$4.68 \pm 0.03 \pm 0.29$

~2 σ discrepancy

Summary for V_{cb} :



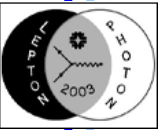
$$|V_{cb}| \cdot F(1) = 0.0367 \pm 0.0013 \quad (S = 1.7)$$

$$F(1) = 0.913^{+0.030}_{-0.035} \quad \text{HQET}$$

$$|V_{cb}|_{\text{excl}} = 0.0402 \pm 0.0020$$

$$|V_{cb}|_{\text{incl}} = 0.0421 \pm 0.0013$$

$$|V_{cb}| = 0.0415 \pm 0.0011$$



$$A \lambda^2 = 0.0415 \pm 0.0011$$

($\pm 2.7\%$)



V_{ud}	V_{us}	V_{ub}
V_{cd}	V_{cs}	V_{cb}
V_{td}	V_{ts}	V_{tb}

Source: Inclusive and exclusive semileptonic B-meson decays into charmless final states

Exclusive decays:

BELLE: BF for $B^0 \rightarrow \pi^- l \nu$, $B^+ \rightarrow \rho^0 l \nu$, $B^+ \rightarrow \omega l \nu$, no $|V_{ub}|$

BABAR: $|V_{ub}|$ from $B^0 \rightarrow \rho^- e^+ \nu$, $B^+ \rightarrow \rho^0 e^+ \nu$

with 55 M $\Upsilon(4S)$ and 5 form-factor calculations, „model dependent“

CLEO: $|V_{ub}|$ from $\pi^- l^+ \nu$, $\pi^0 l^+ \nu$, $\eta l^+ \nu$, $\rho^- l^+ \nu$, $\rho^0 l^+ \nu$, $\omega l^+ \nu$

with 10 M $\Upsilon(4S)$ and QCD form-factors only, „model independent“

Because of small statistics, both use isospin / quark-model constraints:

$$\Gamma(\rho^0 l \nu) = \Gamma(\omega l \nu) = \Gamma(\rho^- l \nu) / 2, \Gamma(\pi^0 l \nu) = \Gamma(\pi^- l \nu) / 2$$

BABAR 2003:

$$B^0 \rightarrow \rho^- e^+ \nu$$

$$B^+ \rightarrow \rho^0 e^+ \nu$$

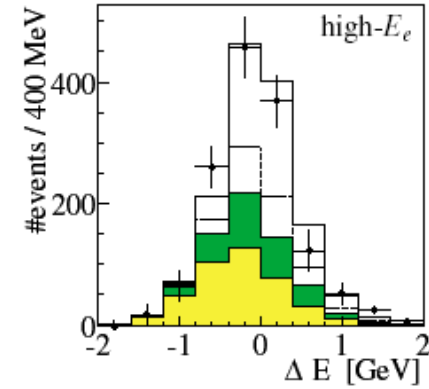
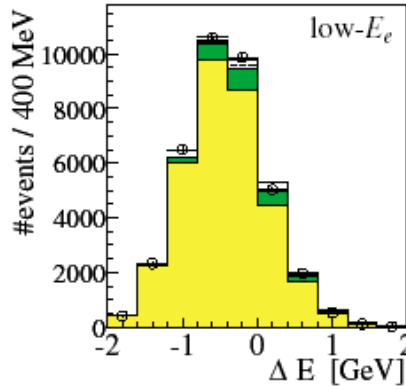
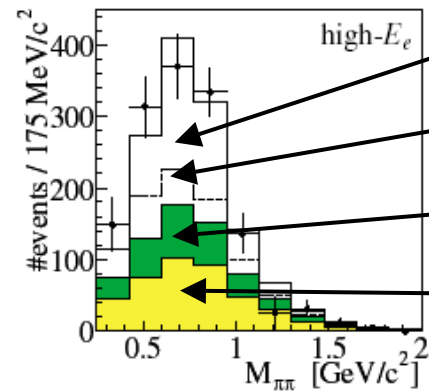
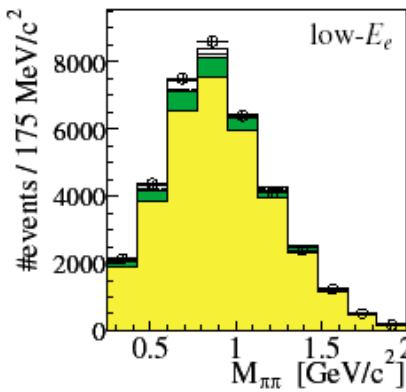
high- E_e : 2.3-2.7 GeV

low- E_e : 2.0-2.3 GeV

signals for $\rho^- \Rightarrow$

results from ρ^- & $\rho^0 \Downarrow$

$$10^4 BF(B^0 \rightarrow \rho^- e^+ \nu)$$



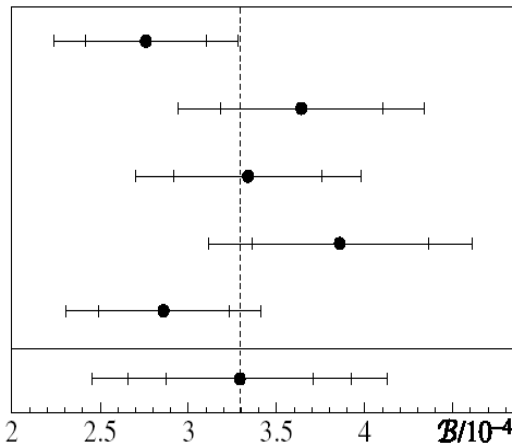
Signal

Crossfeed

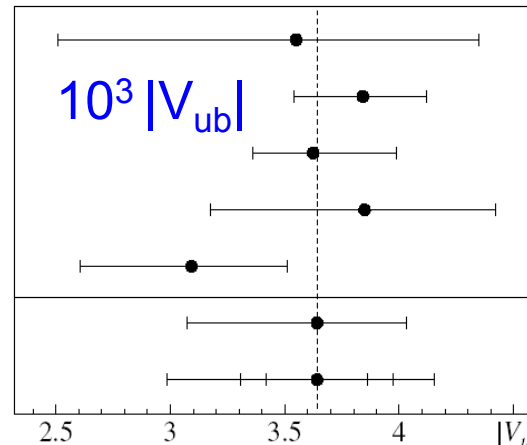
Downfeed

$b \rightarrow clv$

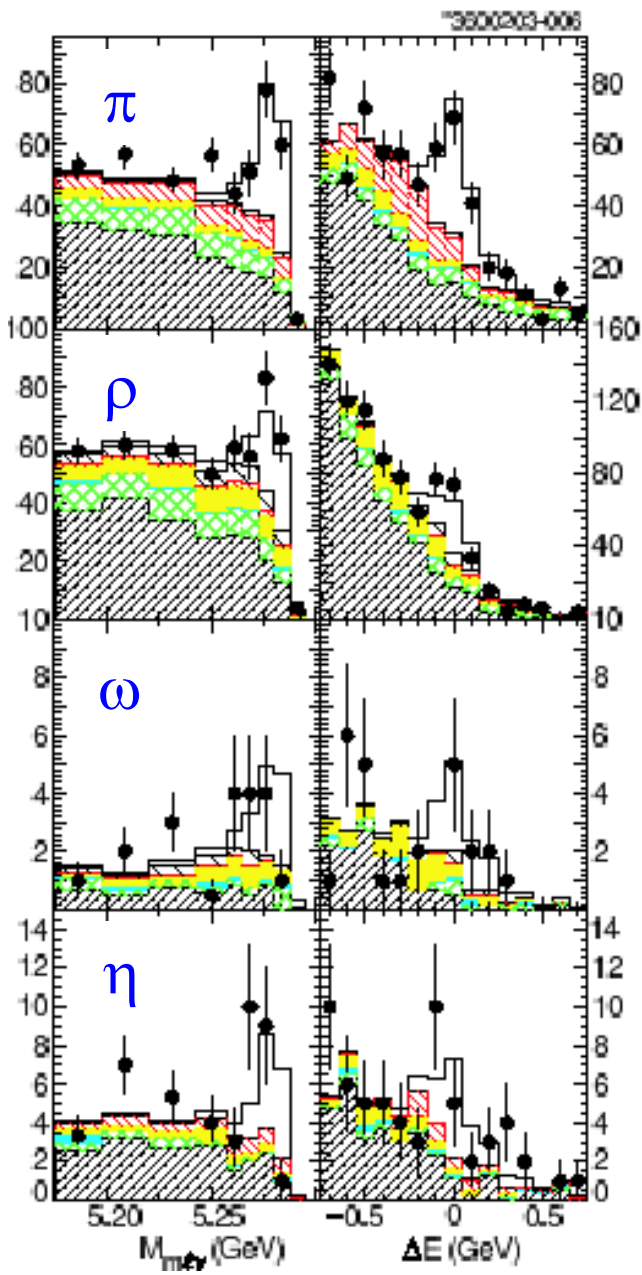
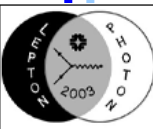
continuum
is already
subtracted



ISGW2:
 $2.76 \pm 0.34 \pm 0.40$
 Beyer/Melikhov:
 $3.64 \pm 0.46 \pm 0.52$
 UKQCD:
 $3.34 \pm 0.42 \pm 0.48$
 LCSR:
 $3.86 \pm 0.50 \pm 0.56$
 Ligeti/Wise:
 $2.86 \pm 0.37 \pm 0.41$
 Combined:
 $3.29 \pm 0.42 \pm 0.47 \pm 0.55$



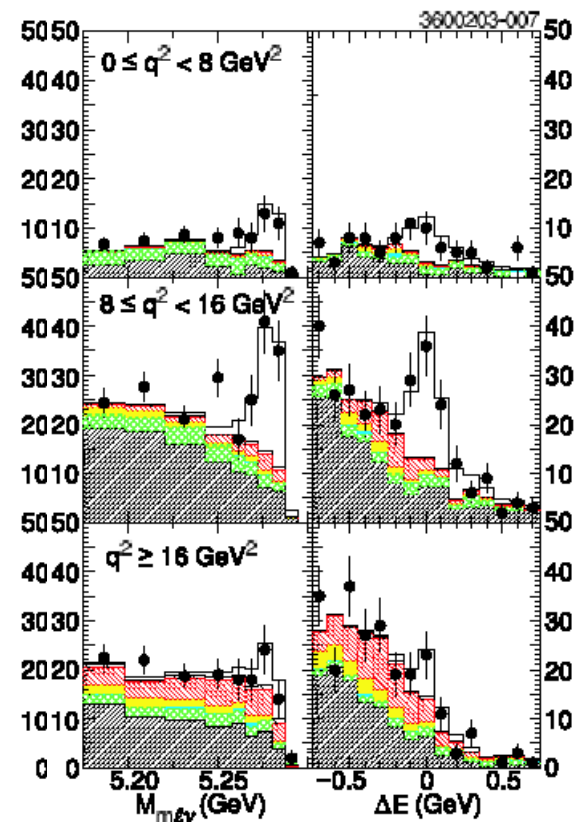
ISGW2:
 $3.55 \pm 0.21 \pm 0.25$ $+0.80$
 -1.04
 Beyer/Melikhov:
 $3.84 \pm 0.24 \pm 0.27$ $+0.28$
 -0.30
 UKQCD:
 $3.62 \pm 0.22 \pm 0.25$ $+0.36$
 -0.26
 LCSR:
 $3.85 \pm 0.24 \pm 0.27$ $+0.57$
 -0.67
 Ligeti/Wise:
 $3.09 \pm 0.19 \pm 0.22$ $+0.42$
 -0.49
 Combined:
 $3.64 \pm 0.22 \pm 0.25$ $+0.39$
 -0.56



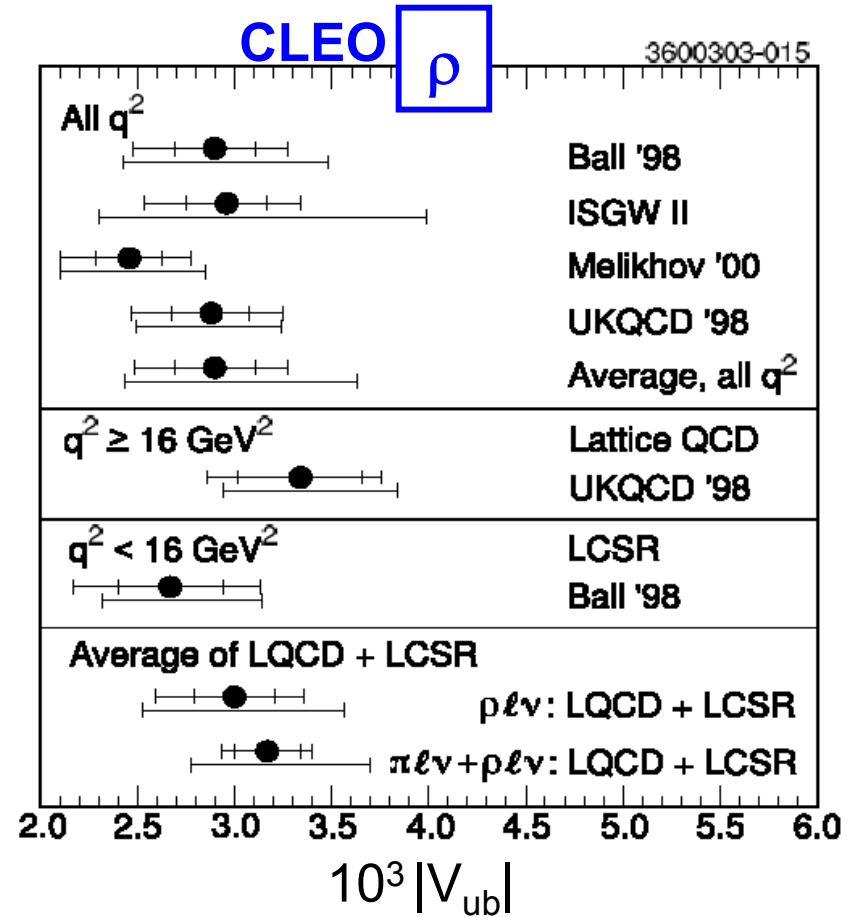
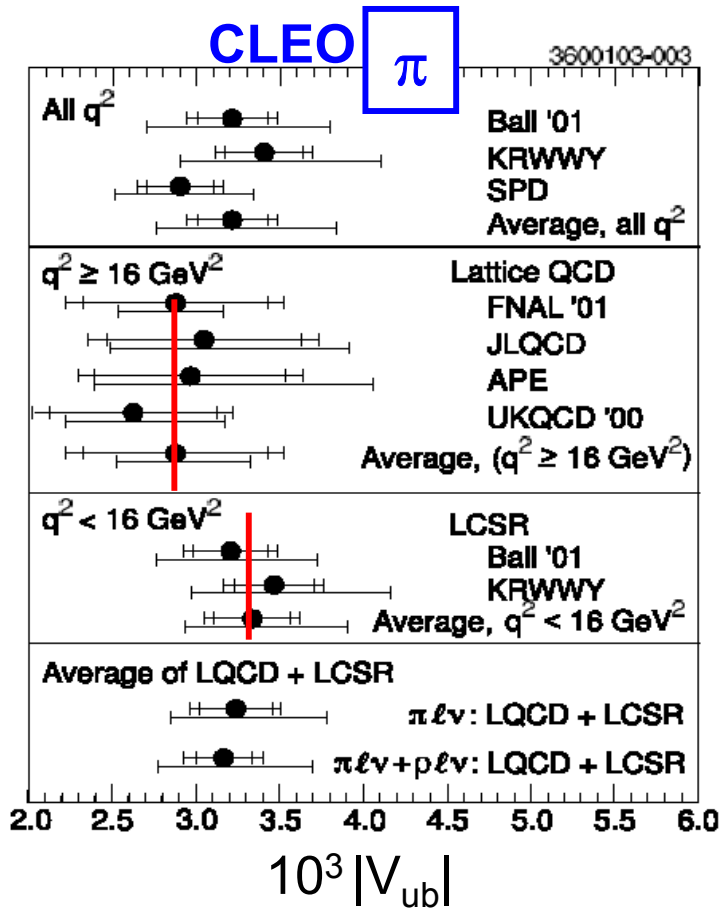
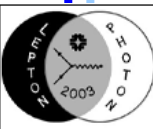
CLEO 2003:

Detector hermeticity \Rightarrow „ ν reconstruction“
 $\Rightarrow q^2$ and $E_l > 1.0$ GeV (π), > 1.5 GeV (ρ)

\leftarrow Signals
 in q^2 bins \Downarrow



white = signal
 red = crossfeed
 yellow = downfeed
 green = continuum
 black = b \rightarrow clv



$$|V_{ub}|_{\text{CLEO}, \pi+\rho} = (3.17 \pm 0.17 \begin{matrix} +0.16 & +0.53 \\ -0.17 & -0.39 \end{matrix}) 10^{-3}$$

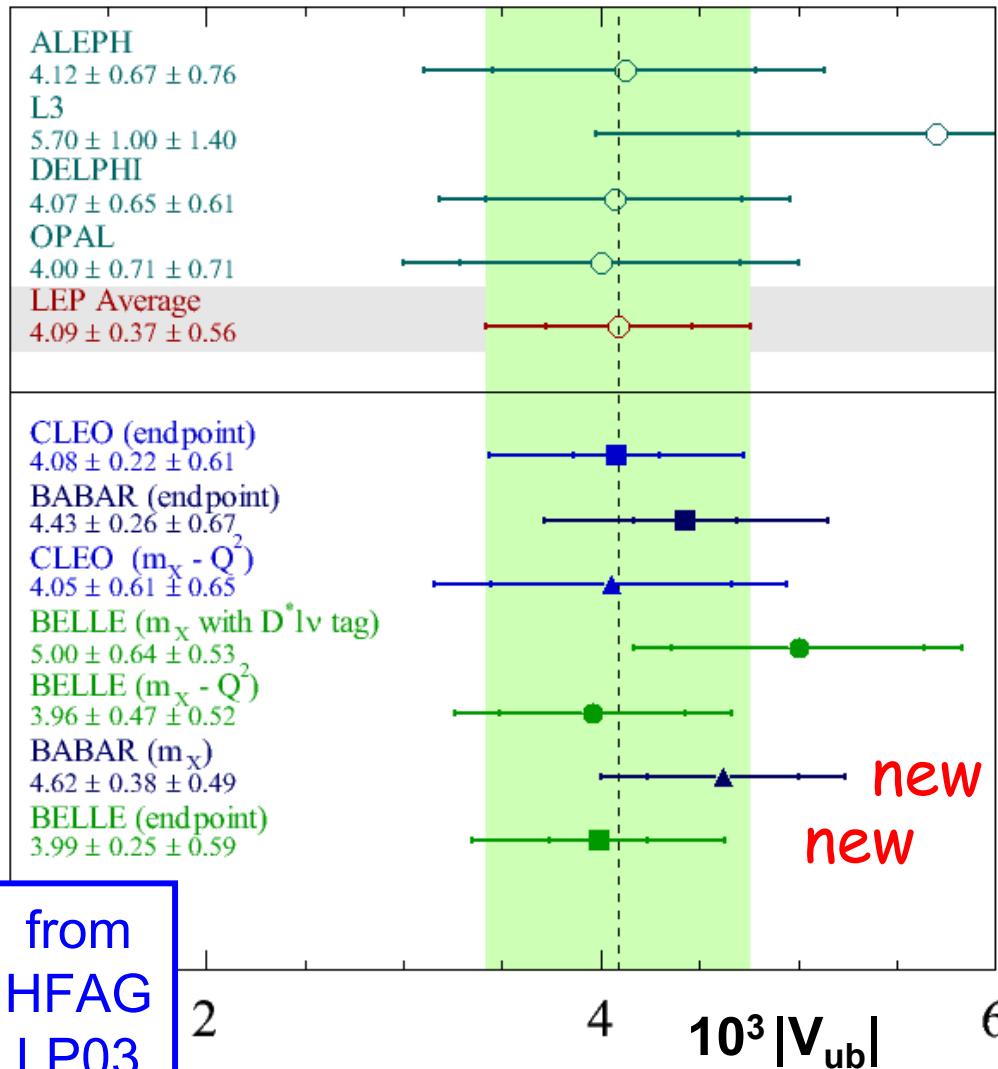
$$|V_{ub}|_{\text{BABAR}, \rho} = (3.64 \pm 0.22 \pm 0.25 \begin{matrix} +0.39 \\ -0.56 \end{matrix}) 10^{-3}$$

$$|V_{ub}|_{\text{excl}} = (3.40 \begin{matrix} +0.24 \\ -0.33 \end{matrix} \pm 0.40) 10^{-3}$$

Inclusive decays $b \rightarrow ul\nu$:

Three methods

- 1) $E_l > 2.3$ GeV, „endpoint“
- 2) $E_l > 1.0$ GeV
and $m_X < 1.5$ GeV,
requires tagged B,
less QCD-dependent.
- 3) $E_l > 1.0$ GeV
and $m_X < 1.5$ GeV
and $q^2 > 12$ GeV²,
requires tagged B
and high statistics.
needs even less QCD.



from
HFAG
LP03

BELLE:

29 MY(4S),

(a) $B \rightarrow e\nu X$

(b) continuum

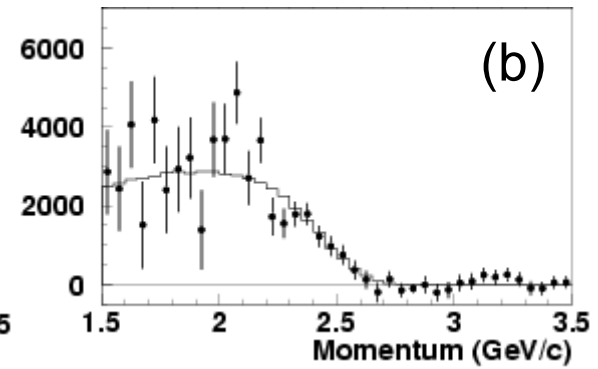
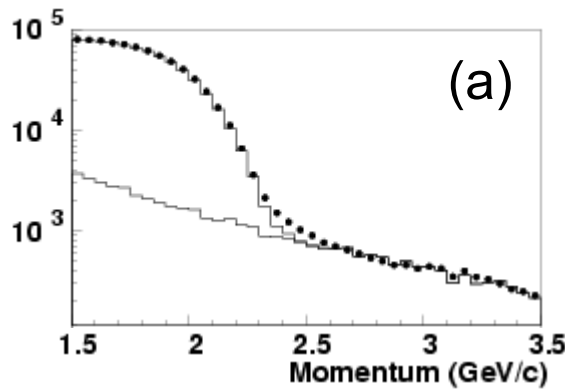
and $b \rightarrow c$ subtracted

$$BF(B \rightarrow e\nu X_u) = \Delta BF(2.3 < E_l < 2.6 \text{ GeV}) / f_u(\text{CLEO})$$

$$|V_{ub}| = (3.99 \pm 0.17_{\text{stat}} \pm 0.16_{\text{sys}} \pm 0.59_{\text{th}}) 10^{-3}$$

What is f_u ? Already used in endpoint analyses of CLEO and BABAR.

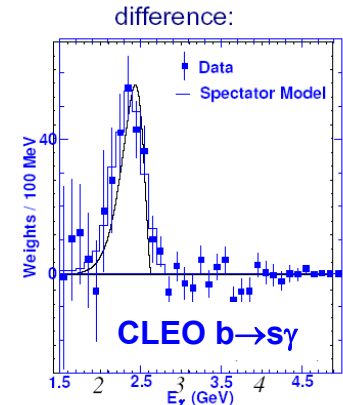
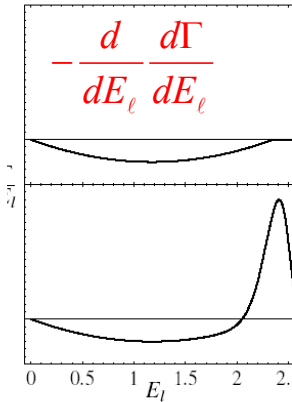
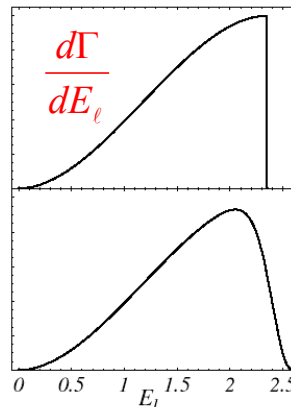
Determined by shape function, also concept of HQET, but beyond OPE, needs nonlocal operators („twists“).



From Z. Ligeti
FPCP-03 Paris:

b-quark
decay

B-meson
decay

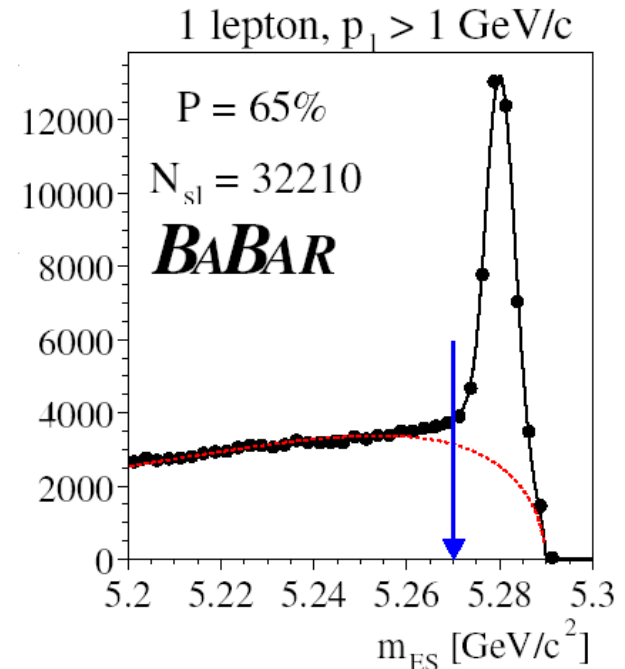
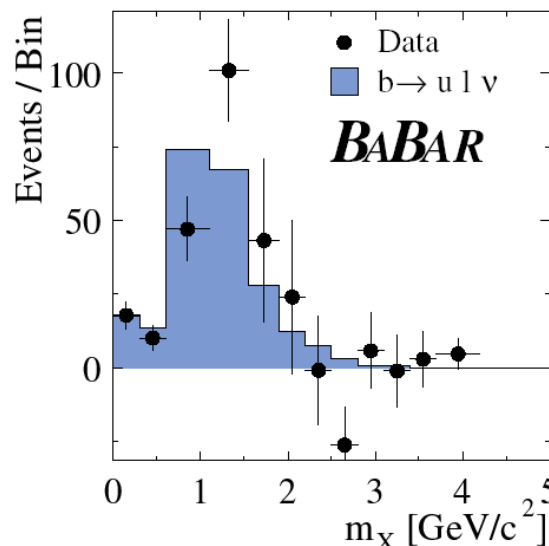
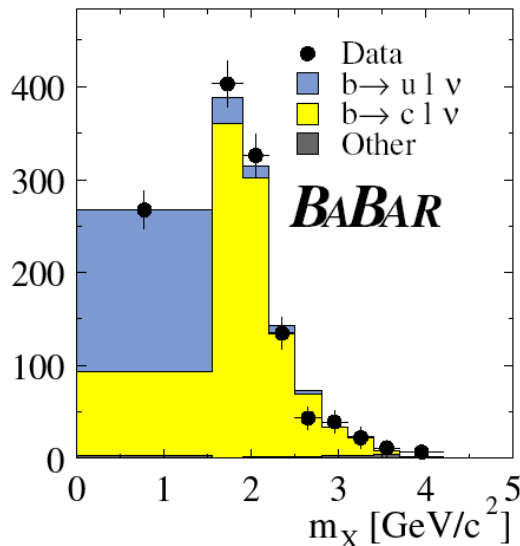


m_X Result of BABAR:

89 M Υ (4S), 32 k events with

$\Upsilon(4S) \rightarrow B_{\text{reco}} B_{\text{sig}}, E_l > 1 \text{ GeV}, B_{\text{reco}} \Rightarrow$

reconstruct m_X in $B_{\text{sig}} \rightarrow l\nu X \Downarrow$

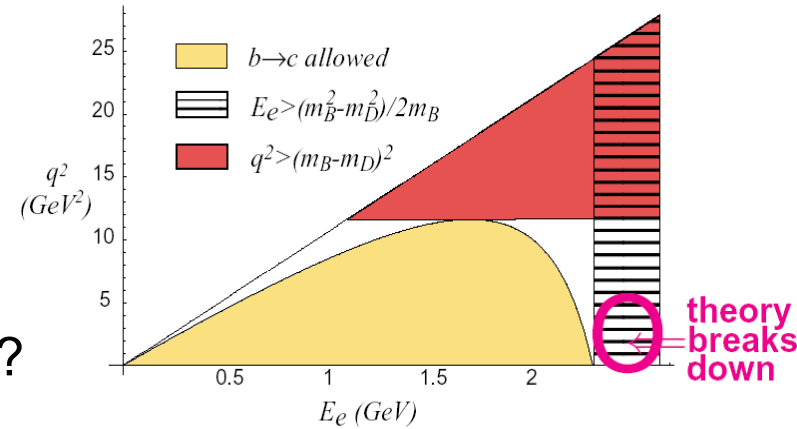


Using the shape function \Rightarrow

$$|V_{ub}| = (4.62 \pm 0.28_{\text{stat}} \pm 0.27_{\text{sys}} \pm 0.40_{\text{shf}} \pm 0.26_{\Gamma \rightarrow V_{ub}}) 10^{-3}$$

Summary for $V_{ub, incl}$:

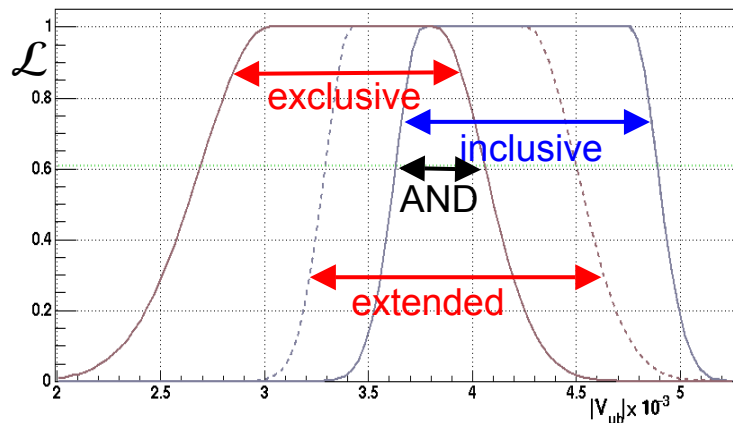
No discussion of m_X - q^2 method here.
 Best prospects in the future because
 of smallest dependence on HQET
 parameters. Take them from V_{cb} data?



HFAG does not yet present an average for $|V_{ub}|_{incl}$.

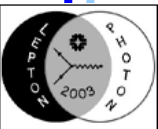
My weighted inclusive mean:

$$|V_{ub}|_{incl} = (4.26 \pm 0.13 \pm 0.50) 10^{-3}$$



$$|V_{ub}|_{excl} = (3.40^{+0.24}_{-0.33} \pm 0.40) 10^{-3}$$

$$|V_{ub}| = (3.80^{+0.24}_{-0.13} \pm 0.45) 10^{-3}$$



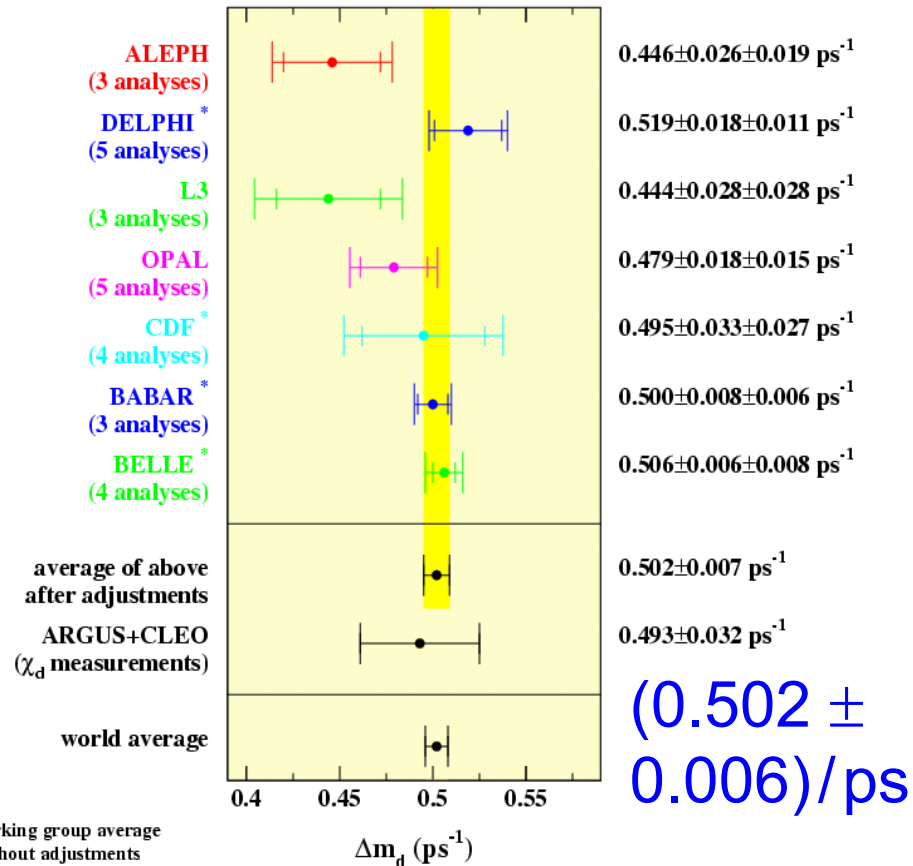
V_{ud}	V_{us}	V_{ub}
V_{cd}	V_{cs}	V_{cb}
V_{td}	V_{ts}	V_{tb}

Source: Δm_d of $B^0\bar{B}^0$ Oscillations

from HFAG LP03 \Rightarrow

$$\Delta m_d = \frac{G_F^2 m_{B_d} f_{B_d}^2 B_{B_d} \eta_B}{6\pi^2} \cdot |V_{td}|^2 \cdot |V_{tb}|^2 \cdot f(m_t^2, m_W^2)$$

$$f_B^2 B_B = (223 \pm 33 \pm 12)^2 \text{ MeV}^2 \text{ from lattice QCD}$$



$$|V_{td}| \cdot |V_{tb}| = (9.2 \pm 1.4 \pm 0.5) 10^{-3}$$



V_{ud}	V_{us}	V_{ub}
V_{cd}	V_{cs}	V_{cb}
V_{td}	V_{ts}	V_{tb}

from $B_s \bar{B}_s$ oscillations
and $b \rightarrow s \gamma$ penguins

$\Delta m_s > 0$ since $\chi_s = (\chi - f_d \chi_d) / f_s > 0$.

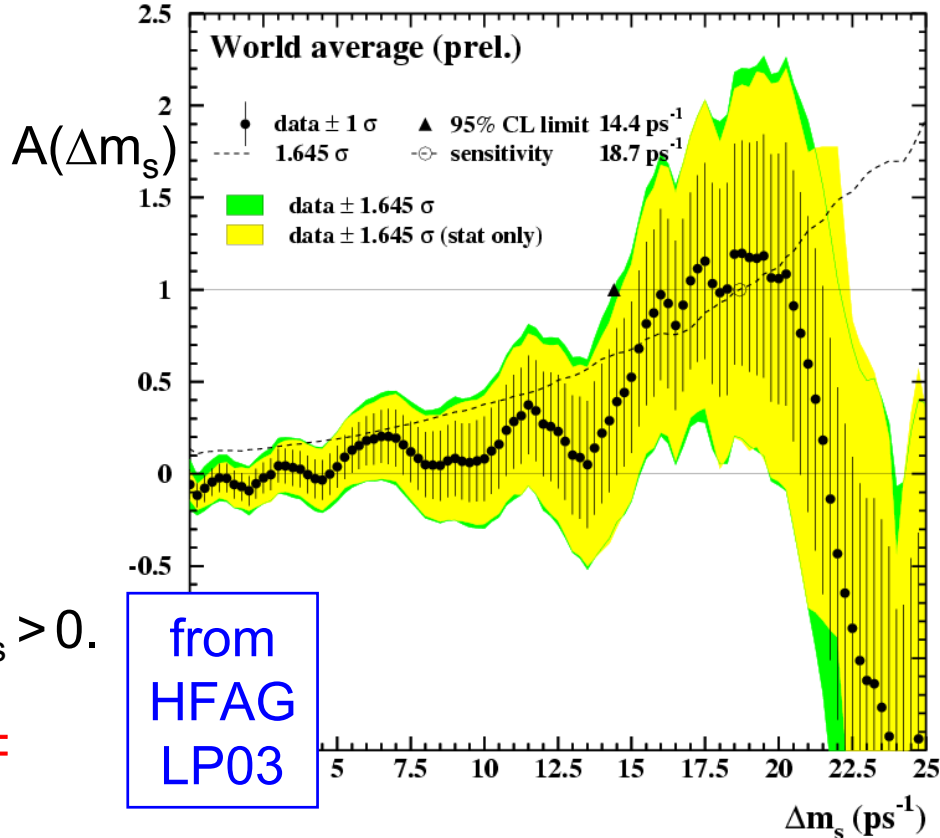
$\Delta m_s > 14.4 / \text{ps}$ (95% CL) \leftarrow

$$\Delta m_s = \frac{G_F^2 m_{B_s} f_{B_s}^2 B_{B_s} \eta_{B_s}}{6\pi^2} \cdot |V_{ts}|^2 \cdot |V_{tb}|^2 \cdot f(m_t^2, m_W^2)$$

$$\xi = \frac{f_{B_s} \sqrt{B_{B_s}}}{f_{B_d} \sqrt{B_{B_d}}} = 1.24 \pm 0.04 \pm 0.06$$

from
HFAG
LP03

$$|V_{ts}| \cdot |V_{tb}| > 0.033$$



Penguins: BF ($B \rightarrow X_s \gamma$) from CLEO, ALEPH, BABAR, BELLE

Ali and Misiak:

$$|V_{ts}| \cdot |V_{tb}| = 0.047 \pm 0.008$$



V_{ud}	V_{us}	V_{ub}
V_{cd}	V_{cs} again	
V_{td}	V_{ts}	V_{tb}

was 1.04 ± 0.16
using $\Gamma(D \rightarrow \bar{K}e\nu)$

Decays of real W-bosons at LEP-2 increase precision:

$$\frac{\Gamma(W \rightarrow \text{hadrons})}{\Gamma(W \rightarrow e\nu)} \propto \frac{|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 + |V_{cd}|^2 + |V_{cs}|^2 + |V_{cb}|^2}{1} = 2.039 \pm 0.026$$

only using that there are five quarks with $m(q) < m(W) \Rightarrow$

$$|V_{cs}| = 0.995 \pm 0.014$$

Prospects: Check by CLEO-c

Unitarity check of the full CKM matrix:

$$V_{ud} \quad V_{us} \quad V_{ub}$$

$$V_{cd} \quad V_{cs} \quad V_{cb}$$

$$|V_{ud}| = 0.9737 \pm 0.0007$$

$$|V_{us}| = 0.2210 \pm 0.0023$$

$$|V_{cd}| = 0.224 \pm 0.016$$

$$|V_{ub}| = 0.0038 \pm 0.0005$$

$$|V_{cb}| = 0.0415 \pm 0.0011$$

$$|V_{cs}| = 0.995 \pm 0.014$$

$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 0.9969 \pm 0.0017 \quad -1.8 \sigma$$

$$|V_{cd}|^2 + |V_{cs}|^2 + |V_{cb}|^2 = 1.042 \pm 0.029 \quad +1.5 \sigma$$

$$|V_{ud}V_{cd}| - |V_{us}V_{cs}| \pm |V_{ub}V_{cb}| = -0.002 \pm 0.016 \quad 0.1 \sigma$$

The observed CKM matrix magnitudes fulfill unitarity reasonably well.

\Leftrightarrow All processes which we call „weak“ can be described by the Standard weak interaction in which the CKM matrix is necessarily unitary.

Assuming Unitarity:

$$|V_{tb}|^2 = 1 - |V_{cb}|^2 - |V_{ub}|^2 \Rightarrow |V_{tb}| = 0.99913 \pm 0.00009$$

$$|V_{td}| = (9.2 \pm 1.4 \pm 0.5) 10^{-3}$$

$$|V_{ts}|^2 = |V_{cb}|^2 + |V_{ub}|^2 - |V_{td}|^2 \Rightarrow |V_{ts}| = 0.0406 \pm 0.0023$$

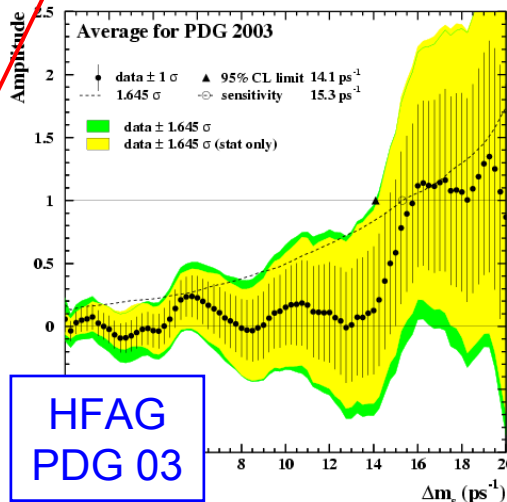
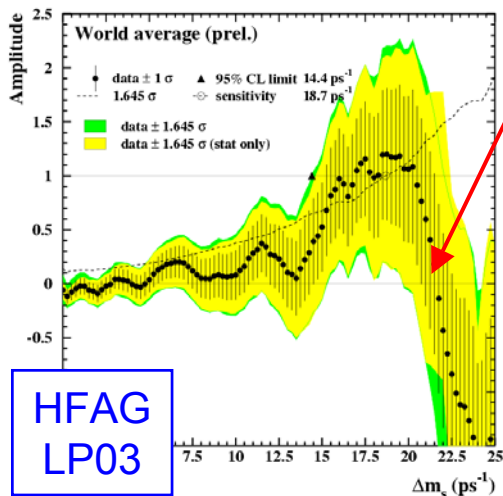


V_{ud}	V_{us}	V_{ub}
V_{cd}	V_{cs}	V_{cb}
V_{td}	again	

This region has often been over-interpreted. Better: Measure Δm_s !

$$\frac{\Delta m_d}{\Delta m_s} = \frac{m_{B_d}}{m_{B_s}} \cdot \frac{|V_{td}|^2}{|V_{ts}|^2} \cdot \xi^2$$

$$\xi = \frac{f_{B_s} \sqrt{B_{B_s}}}{f_{B_d} \sqrt{B_{B_d}}} = 1.24 \pm 0.04 \pm 0.06$$

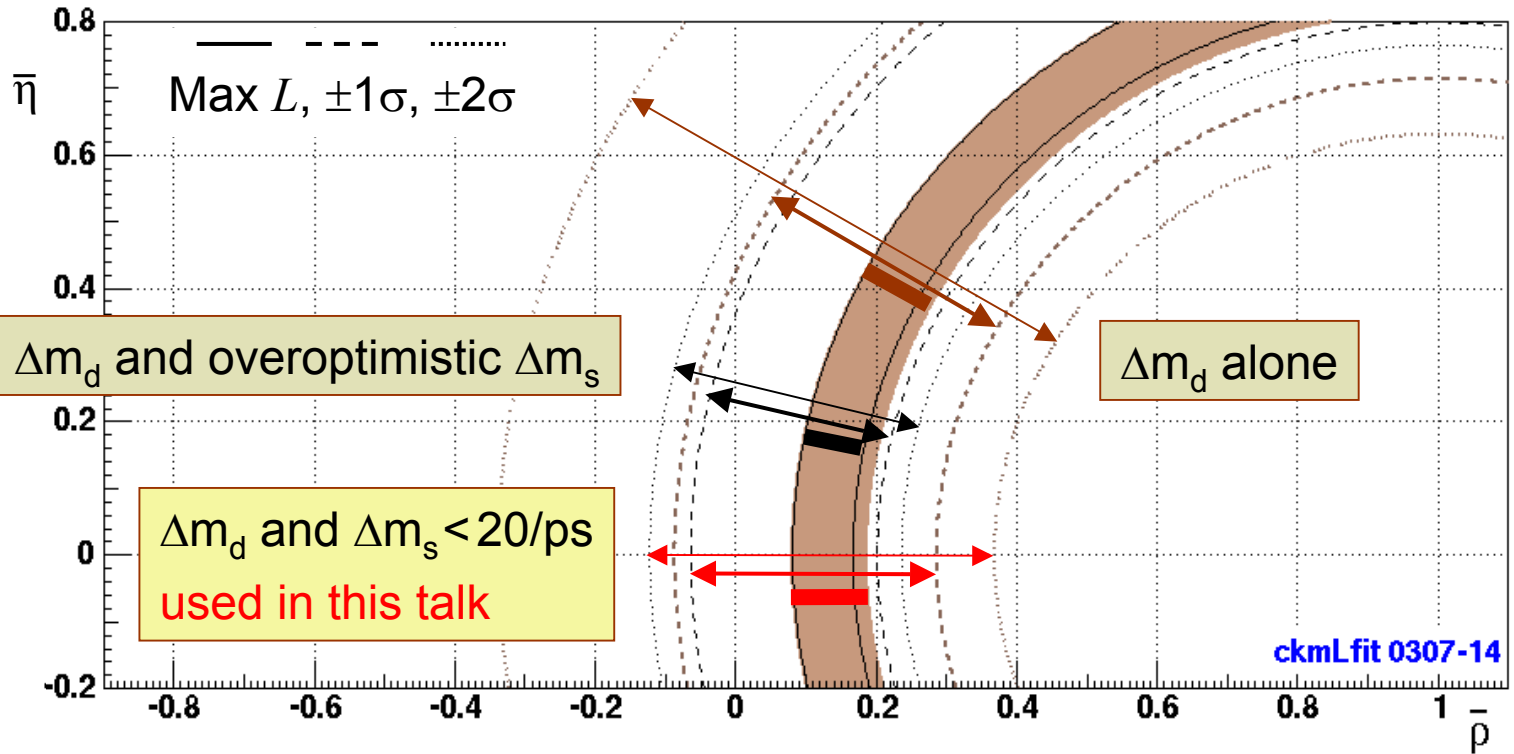


$$L(\Delta m_s) = \begin{cases} e^{-(A-1)^2/2\sigma_A^2} & |\Delta m_s| < 20 / \text{ps} \\ 1 & |\Delta m_s| > 20 / \text{ps} \end{cases}$$

Contours for $|V_{td}|$ in the $\bar{\rho} - \bar{\eta}$ plane:

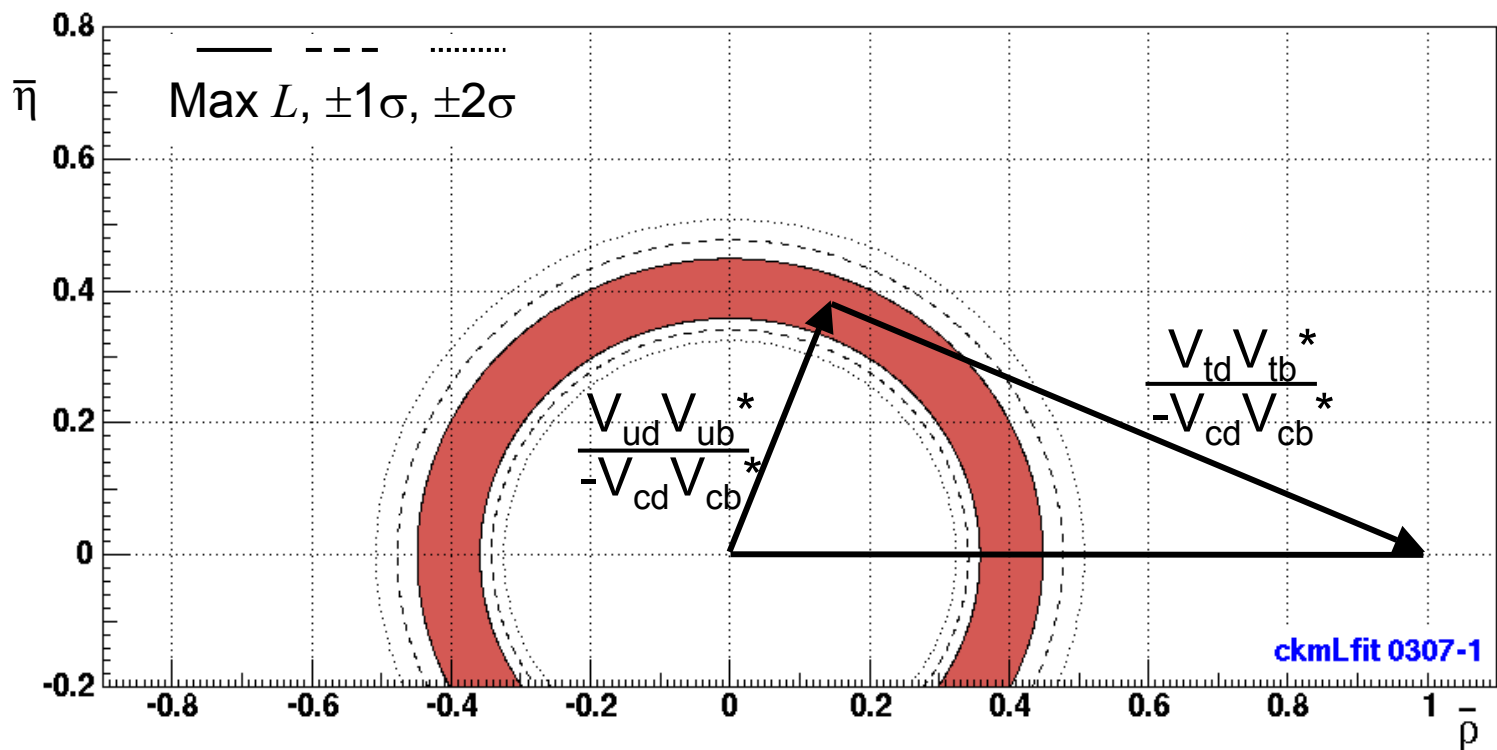
$$|V_{td}| :$$

ckm
Lfit

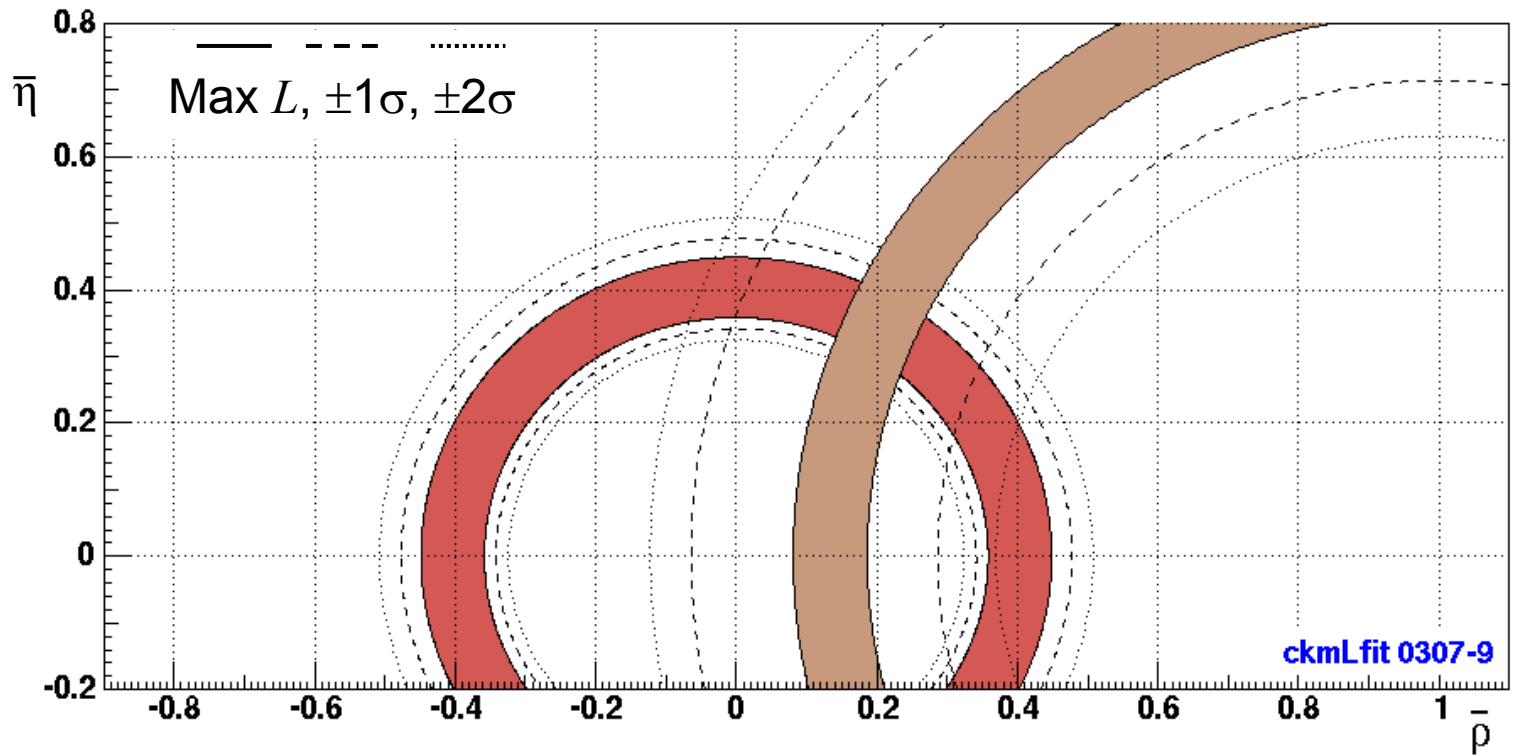


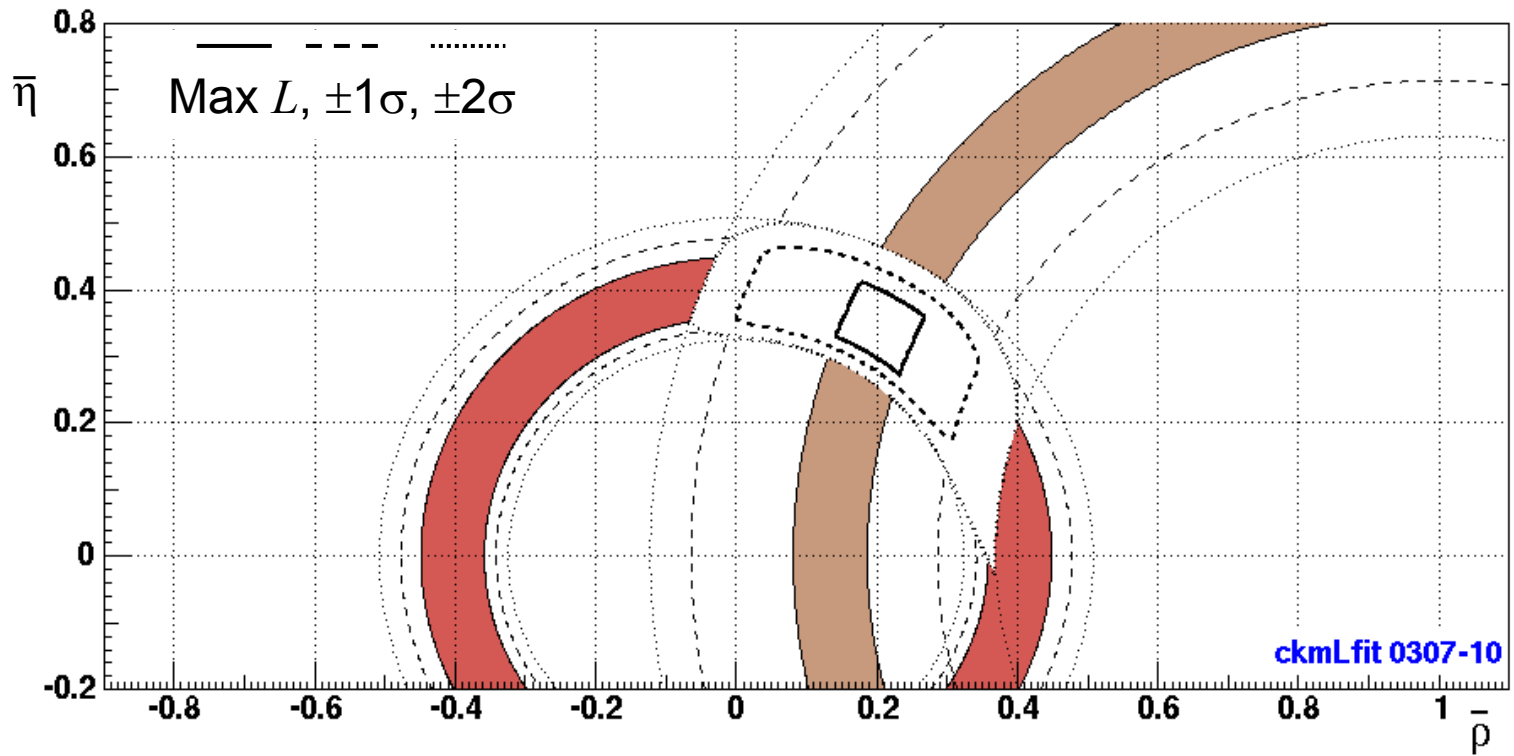
$$V_{ud} V_{ub}^* + V_{cd} V_{cb}^* + V_{td} V_{tb}^* = 0$$

ckm
Lfit



$$\bar{\rho} = \text{Re} \frac{V_{ud} V_{ub}^*}{-V_{cd} V_{cb}^*}, \quad \bar{\eta} = \text{Im} \frac{V_{ud} V_{ub}^*}{-V_{cd} V_{cb}^*}$$

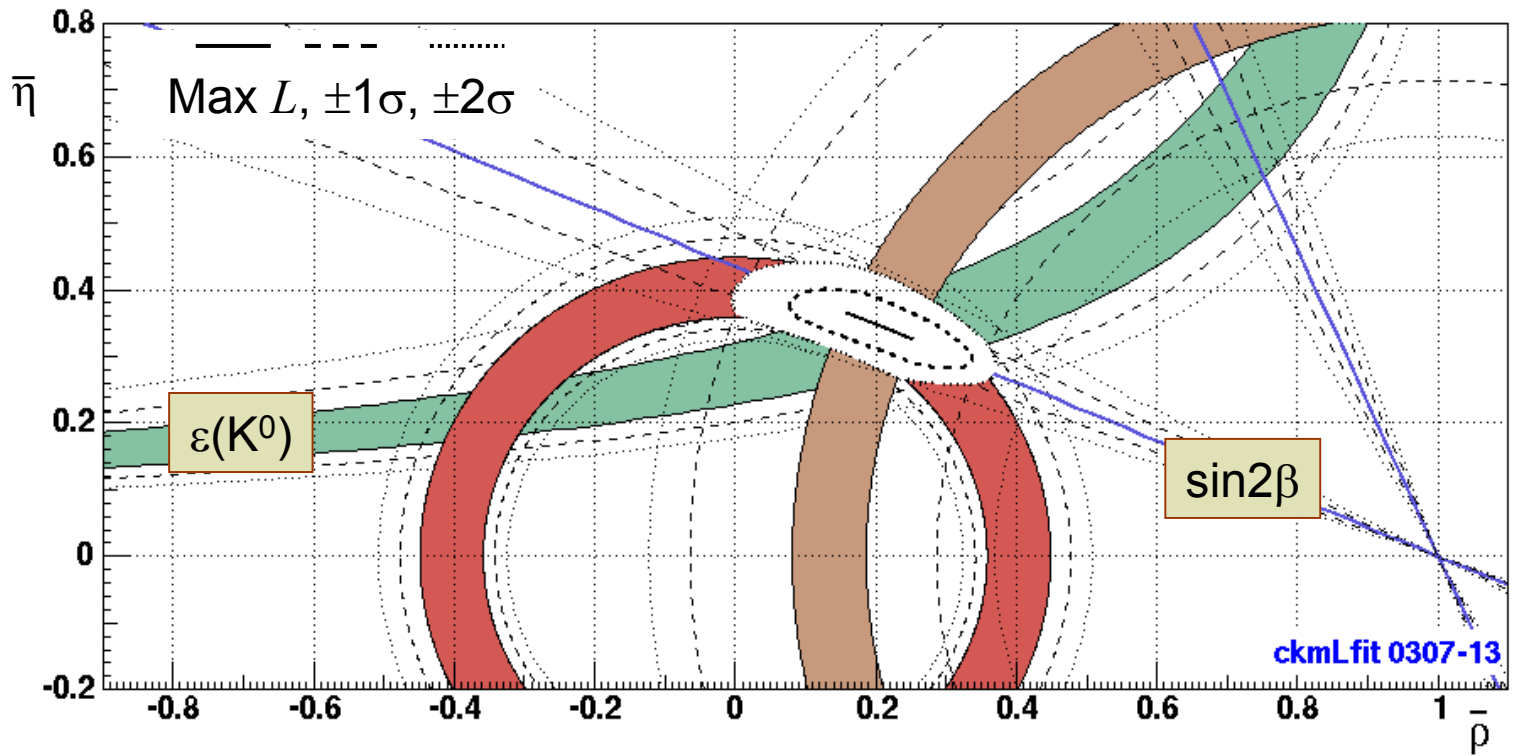




From magnitudes alone: There is CP violation in the St. Model;
but the point $(\bar{\rho}, \bar{\eta}) = (0.37, 0)$ is only excluded with 2σ .

Including CP violation measurements into the unitarity fit:

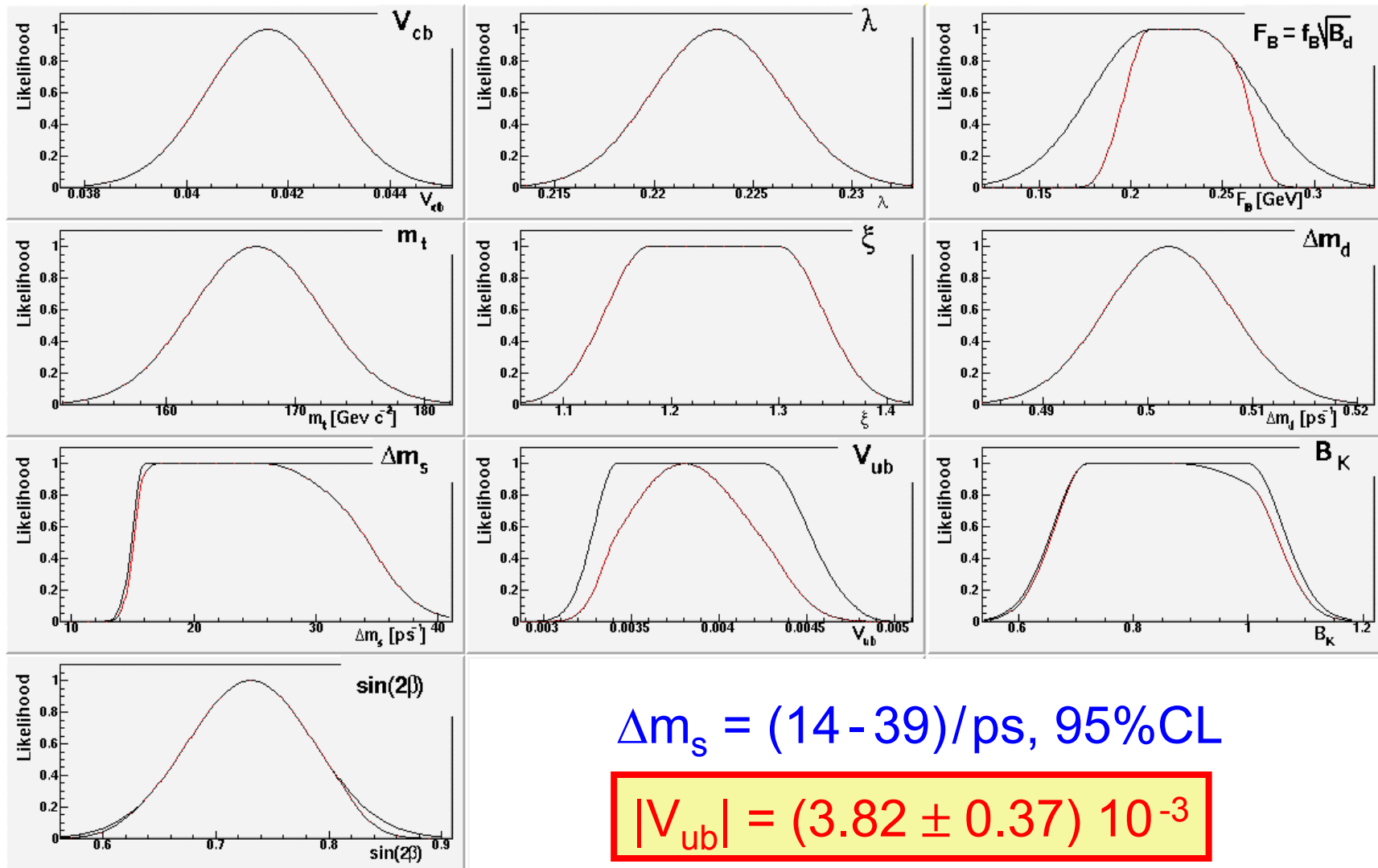
ckm
Lfit



$$\bar{\rho} = 0.21 \pm 0.08 \pm 0.05, \quad \bar{\eta} = 0.34 \pm 0.04 \pm 0.02$$

Parameter values before and after the unitarity fit:

ckm
Lfit



$$\Delta m_s = (14 - 39) / \text{ps}, 95\% \text{CL}$$

$$|V_{ub}| = (3.82 \pm 0.37) 10^{-3}$$

Summary: Rich experimental and theoretical progress in the determination of CKM matrix magnitudes.

Experimental problems: $G_A/G_V(n)$, $\Gamma(K_{l3})$, $F(1) \cdot |V_{cb}| \dots$

Important inputs missing: Δm_s , $\tau(t) \dots$

More statistics will help $|V_{cb}|_{incl}$ and $|V_{ub}|$

„Matrix is unitary“ within $\pm 1.8 \sigma$, using my present error estimates.

Assuming „unitarity“, i. e. no New Physics, and including $\varepsilon(K^0)$, $\sin 2\beta$:

$$\lambda = 0.2235 \pm 0.0033 \quad (\pm 1.5 \%)$$

$$A \lambda^2 = 0.0415 \pm 0.0011 \quad (\pm 2.7 \%)$$

$$A \lambda^3 \sqrt{\rho^2 + \eta^2} = 0.0038 \pm 0.0004 \quad (\pm 10 \%)$$

$$\text{atan}(\eta/\rho) = (58 \pm 19)^\circ \quad (\pm 5 \% \text{ of } 360^\circ)$$

Hierarchy of magnitudes $1, \lambda, \lambda^2, \lambda^3$ was also a hierarchy of precision.

No longer now, $A\lambda^2$ is already better known than A .

V_{ud}	V_{us}	V_{ub}
V_{cd}	V_{cs}	V_{cb}
V_{td}	V_{ts}	V_{tb}