

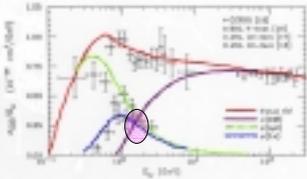


# Unified approach for modeling $\nu$ -N and e-N scattering cross sections from high energy to very low energy, Un-ki Yang (Chicago), Arie Bodek (Rochester)



## 1. Neutrino cross sections at low energy?

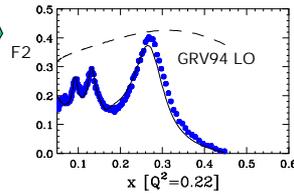
- Many neutrino oscillation experiments (K2K, MI NOS, CNGS, MiniBooNE, and neutrino programs at the JHF) are in few GeV region.
- But neutrino cross sections in this low energy region is poorly understood (especially, resonance and low  $Q^2$  DIS contributions).
- Thus, neutrino cross section model at low energy is crucial for the precise next generation neutrino oscillation experiments.



- Quasi-Elastic / Elastic ( $W=Mn$ ):  $\nu_\mu + n \rightarrow \mu^- + p$ 
  - well measured and described by form factors
- Resonance (low  $Q^2$ ,  $W < 2$ ):  $\nu_\mu + p \rightarrow \mu^- + p + \pi$ 
  - poorly measured and only 1<sup>st</sup> resonance described by Rein and Seghal (double counting issue with DIS)
- Deep Inelastic:  $\nu_\mu + p \rightarrow \mu^- + X$ 
  - well measured by high energy experiments and described by quark-parton model.

## 2. Building up a model for all $Q^2$ region

- Describe DIS, resonance, even photo-production ( $Q^2=0$ ) in terms of quark-parton model. With PDFs, it is straightforward to convert charged-lepton scattering cross sections into neutrino cross section.
- Challenge:
  - ↳ Understanding of high x PDFs at very low  $Q^2$ ? - non-perturbative QCD effects
  - ↳ Understanding of resonance scattering in terms of quark-parton model?

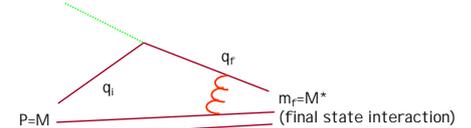
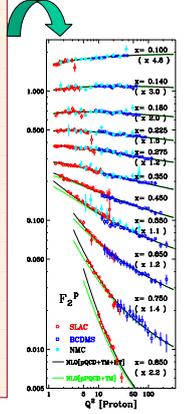


The PDFs do not describe the data at low  $Q^2$

## 3. Lessons from previous QCD studies

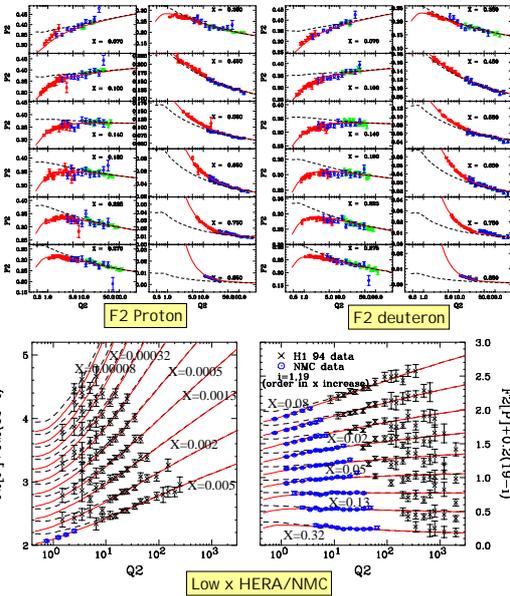
- The DIS data are well described by NLO pQCD with following non-perturbative corrections.
  - Kinematic higher twist (target mass: TM) in the form of Georgi & Politzer  $\xi$  scaling.
  - Dynamic higher twist (multi-quark correlation etc: HT) using power corrections.
- Most of dynamic higher twist corrections (in NLO analysis) are similar to missing NNLO higher order terms (NNLO-TM-NLO-TM-HT).
- Resonance region also works (duality works).

[Ref. Yang & Bodek: PRL 82, 2467 (1999). Eur. Phys. J. C13, 241 (2000)]



Resonance: scattered with very high x parton, then final state int.

## 5. LO model fit results



## 4. Effective LO model

- NNLO QCD+TM approach: good to explain the non-perturbative QCD effects at low  $Q^2$
- Effective LO approach (for MC cross section): Use effective LO PDFs with a new scaling variable  $\xi_w$  to absorb target mass, higher twist, missing higher orders

$$Q^2 + m_p^2 \rightarrow O(m_p^2 - m_f^2) \rightarrow Xbj = Q^2 / 2 Mv$$

$$\xi = Mv (1 + (1 + Q^2/v^2))^{1/2}$$

$\xi$  = parton momentum fraction with finite initial and final quark masses

Use  $\xi_w = [Q^2 + B] / [Mv (1 + (1 + Q^2/v^2))^{1/2} + A]$

1. Start with GRV98 LO ( $Q^2_{min} = 0.80 \text{ GeV}^2$ ) - describe  $F_2$  data at high  $Q^2$
  2. Replace the X with a new scaling,  $\xi_w$
  3. Multiply all PDFs by K factors for photo prod. limit and higher twist [ $\sigma(\gamma) = 4\pi\alpha/Q^2 \cdot F_2(x, Q^2)$ ]  
 $K_{sea} = Q^2 / [Q^2 + C_{sea}]$   
 $K_{val} = [1 - G_p^2(Q^2)] \cdot [Q^2 + C1V] / [Q^2 + C1V]$   
 where  $G_p^2(Q^2) = 1 / [1 + Q^2 / 0.71]^4$
  4. Freeze the evolution at  $Q^2 = Q^2_{min}$   
 $F_2(x, Q^2 < 0.8) = K(Q^2) F_2(x_w, Q^2 = 0.8)$
- Fit to all DIS  $F_2$  P/D (with low x HERA data)  
 $A = 0.418, B = 0.222$   
 $C_{sea} = 0.381, C1V = 0.604, C2V = 0.485$   
 $\chi^2/DOF = 1268 / 1200$

## 6. Comparison with resonance, photo-production, neutrino data

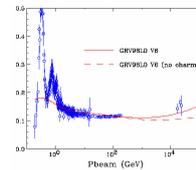
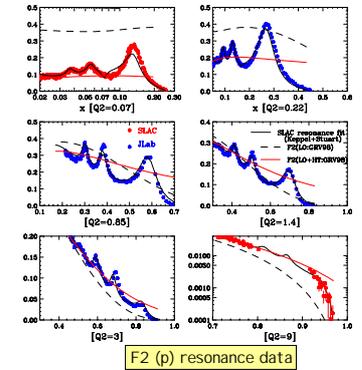
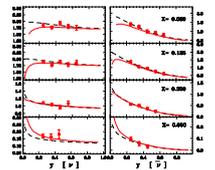


Photo-production ( $\gamma$ -P)



CCFR diff. xsection at 55 GeV

## Summary and Plan

- Our modified GRV98LO PDFs with a scaling variable,  $\xi_w$  describe all SLAC/BCDMS/NMC/HERA DIS data.
- Our predictions in good agreement with resonance data (down to  $Q^2 = 0$ ), photo-production data, and with high-energy neutrino data.
- This model should describe a low energy neutrino cross sections reasonably well. (implemented in NUANCE, NEUGEN)

Can be added from electron scattering  
 • Resonance effect from Jlab data.  
 • Nuclear effects on various targets

Cannot be added from electron scattering  
 • Axial vector effects at very low  $Q^2$   
 • Different nuclear effects in neutrino scatt.

Collaborative approach with nuclear physics community

1. High x and low  $Q^2$  PDFs for e/neutrino
2. Electron scattering exp. at JLAB.
3. Off-axis neutrino exp. at Fermilab/JHF