

QCD Loop Corrections
to Top Production and Decay
(Theoretical Framework)

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1 Introduction

At LC : precision measurements of top parameters :

mass, width, couplings

Also look for

- anomalous couplings
- CP violation

Magnitude of these effects : several % of the total cross section

⇒ we need precise theoretical predictions for the process

QCD radiative corrections

- production : - virtual and soft gluon Jersak, Laerman & Zerwas ('82)

↳ $e^+e^- \rightarrow t\bar{t}(g)$
- hard gluon Korner *et al.*, Parke *et al.*,
Brandenburg *et al.*, ...

- decay : virtual + hard gluons Jezabeck & Kuhn, ...

↳ $t \rightarrow bW(g)$
Lee, Oakes & Yuan, ...

→ Top on shell C. Schmidt

↳ $e^+e^- \rightarrow t\bar{t}(g) \rightarrow bW^+bW^-(g)$

Effects due to top being off-shell : naively, of order Γ_t/m_t , but :
possibly larger in differential cross-sections.

- soft gluon radiation Khoze, Orr & Stirling ('94)

→ Top off shell : - hard gluon Macesanu & Orr ('99)

- virtual corrections

2 Feynman diagrams – resonant behavior

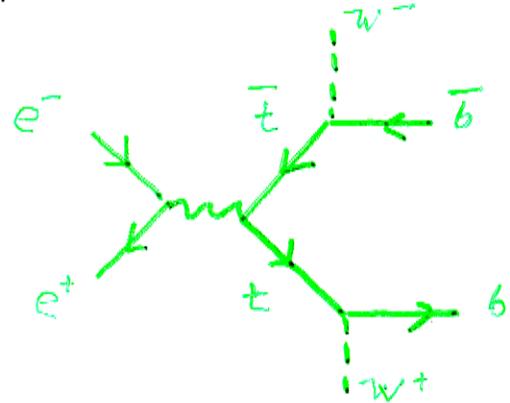
- Physical process : $e^+e^- \rightarrow b W^+ \bar{b} W^-$

TREE LEVEL

- a) doubly resonant diagram :

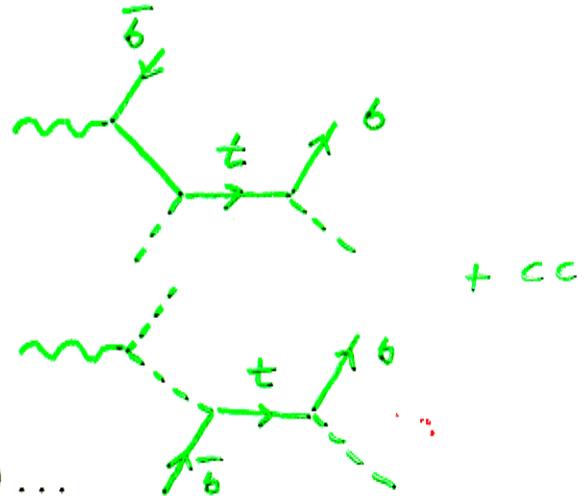
$$M_0 \sim \frac{1}{p_t^2 - \bar{m}_t^2} \frac{1}{p_{\bar{t}}^2 - \bar{m}_t^2}$$

$$\bar{m}_t^2 = m_t^2 - im_t\Gamma_t$$



- b) singly resonant diagrams :

$$M_0 \sim \frac{1}{p_t^2 - \bar{m}_t^2}$$



- c) nonresonant diagrams : about 50 ...

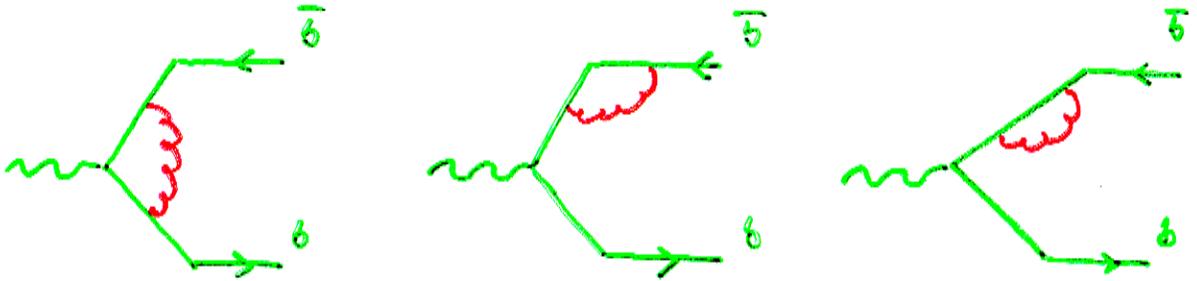
- computation done in *double pole approximation* (DPA):
 - keep only the amplitudes which have a doubly resonant behavior
- Similar approach has been used in evaluating the cross section for W pair production at LEP. ¹

¹RacoonWW talk by D. Wackerroth

VIRTUAL CORRECTIONS

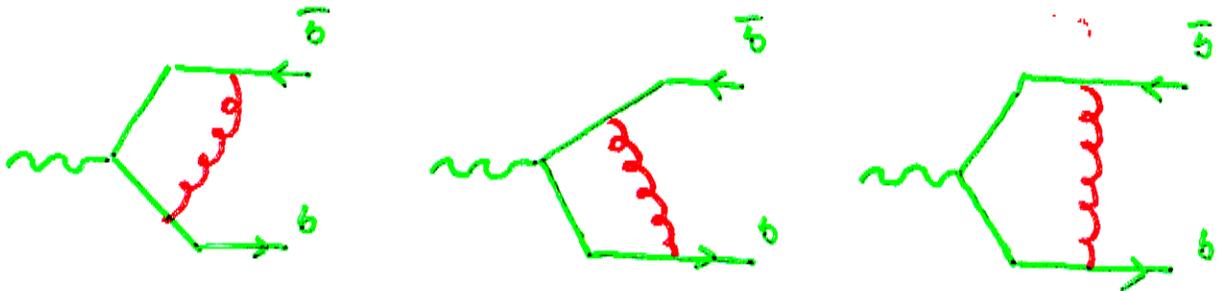
(to the doubly resonant diagram)

a) to subprocesses (factorizable-type corrections)



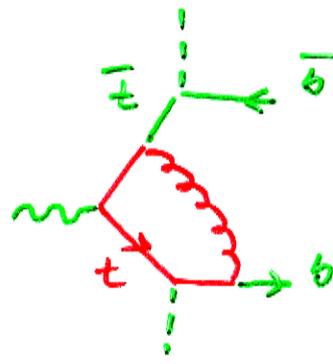
$$M \sim \frac{1}{p_t^2 - \bar{m}_t^2} \frac{1}{p_t^2 - \bar{m}_t^2} + \frac{1}{p_t^2 - \bar{m}_t^2} \log(p_t^2 - \bar{m}_t^2) + \log(p_t^2 - \bar{m}_t^2) \frac{1}{p_t^2 - \bar{m}_t^2}$$

b) interference



$$M \sim \frac{1}{p_t^2 - \bar{m}_t^2} \log(p_t^2 - \bar{m}_t^2)$$

3 Amplitudes in DPA



3.1 Production Decay Interference

$$M_{b\bar{t}} = \bar{u}(b) \left[(-ig_s^2) \int \frac{d^4 k}{2\pi^4} \frac{1}{k^2} \gamma^\mu \frac{\hat{p}_b - \hat{k} + m_b}{(p_b - k)^2 - m_b^2} \hat{\epsilon}_{W^+} + \frac{\hat{p}_t - \hat{k} + m_t}{(p_t - k)^2 - m_t^2} \hat{a} \right. \\ \left. \frac{-\hat{p}_{\bar{t}} - \hat{k} + m_t}{(p_{\bar{t}} + k)^2 - m_t^2} \gamma_\mu \right] \frac{-\hat{p}_{\bar{t}} + m_t}{p_{\bar{t}}^2 - m_t^2} \hat{\epsilon}_{W^-} v(\bar{b})$$

- hard gluon : $M_{b\bar{t}} \sim \frac{1}{p_{\bar{t}}^2 - m_t^2}$
 \Rightarrow doubly resonant terms are entirely due to soft gluons
- employ (*extended*) soft gluon approximation (ESGA) :

Denner, Dittmaier & Roth

$$M_{b\bar{t}}(DPA + ESGA) = \frac{\alpha_s}{4\pi} \underline{M_0} * (-4p_b p_{\bar{t}})(p_t^2 - m_t^2) * \\ \int \frac{d^4 k}{i\pi^2} \frac{1}{k^2} \frac{1}{k^2 - 2k p_b} \frac{1}{(p_t - k)^2 - m_t^2} \frac{1}{(p_{\bar{t}} + k)^2 - m_t^2} \rightarrow D_{b\bar{t}}^0$$

- contribution proportional to M_0

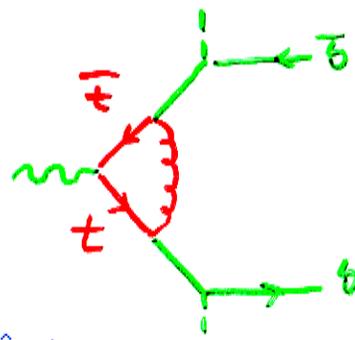
Resonant behavior :

$$D_{b\bar{t}}^0 \sim a_1 \log(p_t^2 - m_t^2) + a_2 \log(p_{\bar{t}}^2 - m_t^2) \\ \Rightarrow M_{b\bar{t}}(DPA) \sim \log(p_t^2 - m_t^2) \frac{1}{p_{\bar{t}}^2 - m_t^2} *$$

- similar results for the Decay-Decay Interference diagram

Also, results are identical to the ones obtained for the interference diagrams in W pair production.

3.2 Vertex Correction



$$M_{t\bar{t}} = \bar{u}(b) \hat{\epsilon}_{W^+} \frac{\hat{p}_t + m_t}{p_t^2 - \bar{m}_t^2} \delta\Gamma^\mu \frac{-\hat{p}_{\bar{t}} + m_t}{p_{\bar{t}}^2 - \bar{m}_t^2} \hat{\epsilon}_{W^-} v(\bar{b})$$

The vertex correction can be written :

$$\delta\Gamma^\mu = \frac{\alpha_s}{4\pi} *$$

$$\left[\begin{array}{l} p_t^\mu F_1 + \gamma^\mu F_2 \\ + (\hat{p}_t - m_t) p_t^\mu F_3 + (\hat{p}_t - m_t) \gamma^\mu F_4 \\ + p_t^\mu (\hat{p}_{\bar{t}} + m_t) F_5 + \gamma^\mu (\hat{p}_{\bar{t}} + m_t) F_6 \\ + (\hat{p}_t - m_t) p_t^\mu (\hat{p}_{\bar{t}} + m_t) F_7 + (\hat{p}_t - m_t) \gamma^\mu (\hat{p}_{\bar{t}} + m_t) F_8 \end{array} \right]$$

• 8 form factors in the general case; on-shell, only F_1 and F_2 contribute

• $F_i \sim f_i C_{t\bar{t}}^0 + \dots \quad i = 1, \dots, 8,$

$$C_{t\bar{t}}^0 \sim \log(a(p_t^2, p_{\bar{t}}^2))$$

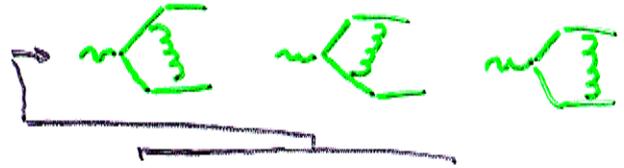
where $a(p_t^2, p_{\bar{t}}^2) \rightarrow 0$ when $p_t^2, p_{\bar{t}}^2 \rightarrow 0$

\Rightarrow in DPA, keep F_1, \dots, F_6

• beside terms similar to on-shell computation (F_1, F_2), we acquire extra terms (F_3, \dots, F_6). This is due to the fact that our off-shell particle is a fermion.

3.3 Total Amplitude

Virtual corrections in DPA :



$$M_1 = M_{t\bar{t}} + M_{tb} + M_{t\bar{b}} + M_0(f_{b\bar{t}} + f_{\bar{t}b} + f_{b\bar{b}})$$

- Evaluation :
 - loop integrals : routines for evaluating 4-point functions for complex masses
 - matrix elements : use spinor techniques (Kleiss & Stirling)

Gauge Invariance

- for W pair production computation, gauge invariance in DPA is guaranteed by the fact that the off shell corrections are proportional to the on-shell result.
- for t pair production, this is no longer true; but we have checked – analytically – that our results are gauge invariant in the approximation used (that is, up to singly resonant terms).

Infrared gluon radiation

- we take into account only radiation from the on-shell particles (final state b 's).
- radiation from the off-shell particles ($t\bar{t}$) is an infrared safe quantity - compute it using real gluons
- maximum energy of infrared gluons (analytically integrated) is much smaller than the top width (~ 0.1 GeV).

4 Status

- We have constructed a Monte Carlo program which implements the DPA computation for virtual corrections presented here.

This, together with a real gluon radiation MC , gives us the necessary tools for a full analysis of the top production and decay at an e^+e^- collider.

- Checks on the results going on right now.

- comparison with the on-shell computation

- in this approximation, we have been able to recreate the results first obtained by C. Schmidt

- In the near future : anticipate results for total cross section for $t\bar{t}$ production, top mass reconstruction analysis.