

PROSPECTS FOR FINDING
HEAVY MAJORANA NEUTRINO SIGNALS
AT THE L.C. IN THE ABSENCE OF $\beta\beta_{\text{nov}}$.

- 1) Motivation for possible existence of heavy Majorana neutrinos, N_H .
- 2) Using the Linear Collider for an N_H search:
parameter range,
cross-sections,
experimental signals,
backgrounds.
- 3) Compatibility with existing evidence:
rare decays of leptons
neutrinoless double beta decay
- 4) Conclusions: We will see them if ...

SEARCH FOR HEAVY MAJORANA NEUTRINOS WITH THE LINEAR COLLIDER

The neutrino mass problem remains one of the most challenging items on our plate when we consider the Standard Model and its limits:

- SM: neutrinos are massless;
they are left-handed only.
- We do not know whether they are properly represented by DIRAC or MAJORANA field operators

THE SM DOES NOT CARE

Mass terms in the Lagrangian:

connect right-handed / left-handed fields

$$- \mathcal{L}_{\text{Dirac}} = m_D \bar{\nu}_L N_R + \text{h.c.}$$

$$- \mathcal{L}_{\text{Majorana}} = \frac{1}{2} m_M \bar{\nu}_L \nu_R^c + \text{h.c.}$$

• NEUTRINO MASSES

3 known generations

$\left. \begin{array}{l} \nu_e \\ \nu_\mu \\ \nu_\tau \end{array} \right\}$ masses are small,
may vanish.

IF $m(\nu_i) = 0$, NO HELICITY FLIP
POSSIBLE

→ LEPTON NUMBER MAY BE A
MEANINGLESS CONCEPT

DIRAC EQUATION "ALLOWS" FOR THE PARTICLE/
ANTIPARTICLE CONCEPT VIA EL. CHARGE

→ IN THE ABSENCE OF CHARGE, HELICITY
CONSERVATION MAY BE THE ONLY REASON
WHY ν AND $\bar{\nu}$ LOOK DIFFERENT:

$$CPT |\dots, \lambda\rangle \rightarrow |\dots, -\lambda\rangle$$

FOR $m(\nu) = 0$, THERE IS NO MEANING TO
A DIFFERENCE BETWEEN

DIRAC
MAJORANA } MASSES

BUT...

THIS SCENARIO IS STARTING TO
CRUMBLE

SOLAR NEUTRINO ANOMALY?

ATMOSPHERIC NEUTRINO
ANOMALY?

OSCILLATIONS? LSND ... ?
KARMEN ...
KAMIOKANDE ...

Irrespective of the outcome of these searches

$m_\nu = \text{very small}$ (if not \emptyset)
for ν_e, ν_μ, ν_τ

HIGHER SYMMETRY SCHEMES WOULD
BE REPLACED BY A

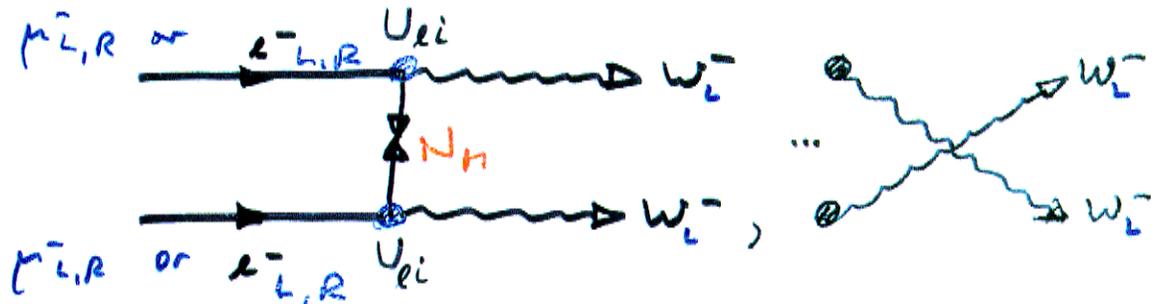
SEE-SAW MECHANISM

$$m_\nu m_N \approx m_e^2 \leftarrow \text{charged lepton mass}$$

\uparrow
 $0(1\text{TeV})$

A UNIQUE OPPORTUNITY AT LIKE-SIGN MUON e^-e^- COLLIDERS:

A SIMPLE CONFIGURATION IS ACCESSIBLE



IF CROSS-SECTIONS ARE PROMISING,
 THERE ARE SOME UNIQUE ADVANTAGES:

- PLENTIFUL SOURCES AVAILABLE
- EASY BACK-TO-BACK FINAL-STATE KINEMATICS
- POLARIZABILITY OF e^- BEAMS MAKES CHIRAL COUPLINGS
- MUON POLARIZATION? ADJUSTABLE

earlier work: ushio (1982)

Rizzo (1982)

London et al (1987)

Maalampi et al (1993)

work done with

PETER MINKOWSK

Nuc. Phys. B 416, 3 (1994)

Phys Lett. B 374, 116 (1996)

WE WORK IN THE KINEMATIC REGIME

$$2m_W \ll \sqrt{s} \ll M_1$$

WITH COUPLING/MIXING PARAMETERS (FOR THE ELECTRONS)

$$V_{eA}$$

$$A = 1, 2, (\dots)$$

THE OVERALL NEUTRINO MASS MATRIX IS THEN

$$M = \begin{pmatrix} & \begin{matrix} \alpha \\ 1 & 2 & 3 \end{matrix} & \begin{matrix} A \\ 1 & 2 & \dots \end{matrix} \\ \alpha \begin{matrix} 1 \\ 2 \\ 3 \end{matrix} & 0 & \mu^T \\ A \begin{matrix} 1 \\ 2 \\ \vdots \end{matrix} & \mu & M \end{pmatrix}$$

AND

$$M = U m_D U^T$$

↳ diagonal matrix

$$m_1, m_2, m_3, M_1, M_2$$

INCLUDING ALL KINEMATIC INTEGRATIONS, WE ARRIVE AT CROSS-SECTIONS

$$\sigma(e^-_i e^-_i \rightarrow W^- W^-_{\text{long}}) \approx \frac{1}{\pi^2 (\pi W)^2} \left(\frac{s}{\pi^2}\right)^2 \left(\frac{g_{ei}}{4\pi}\right)^2$$

mixing parameter

$$\pi = \sqrt{\pi_1 \pi_2} \gtrsim 1-10 \text{ TeV}$$

The resulting cross-section estimates are conservative:

they assume ~ equal mixings for μ, e with N_H

↳ which are to be identified with right-handed singlets that occur naturally in the decomposition of $E(6) \rightarrow SO(10) \rightarrow \dots \rightarrow S.M.$

They lead to small \rightarrow respectable event rates for realistic L.C. luminosities

for standard 10^7 sec year:

\sqrt{s}	L	event rate/y	
		2×10^{-4}	5×10^{-3}
0.5 TeV	$10^{34} \text{ cm}^{-2} \text{ sec}^{-1}$	0.1	60
1. TeV	10^{34} "	2	1,000
	10^{35} "	20	10,000

- SPECTACULAR FINAL-STATE SIGNALS:

$W^+ \rightarrow$
 $W^- \rightarrow$ } back-to-back decays into

- reconstructed hadronic jets

• $\left. \begin{array}{l} \mu^- \mu^- \\ \mu^- e^- \\ \mu^- \tau^- \\ \tau^- e^- \end{array} \right\}$ with missing p_{\perp}

- All presently discussed L.C. detectors will have a good efficiency for identifying these final states

with good efficiency

IF BACKGROUNDS

ARE MANAGEABLE

- Is the principal "generator" of similar signals →

$$e^-e^- \rightarrow W^-W^- \nu_e \nu_e$$

A SERIOUS BACKGROUND TO THE LEPTON #
VIOLATING PROCESS WITH N_H EXCHANGE?

NO!

- $\nu_e \nu_e$ GENERALLY ESCAPE WITH
- HALF THE C.T. ENERGY

→ E_{CAL} CUTS WILL DO THE TRICK.

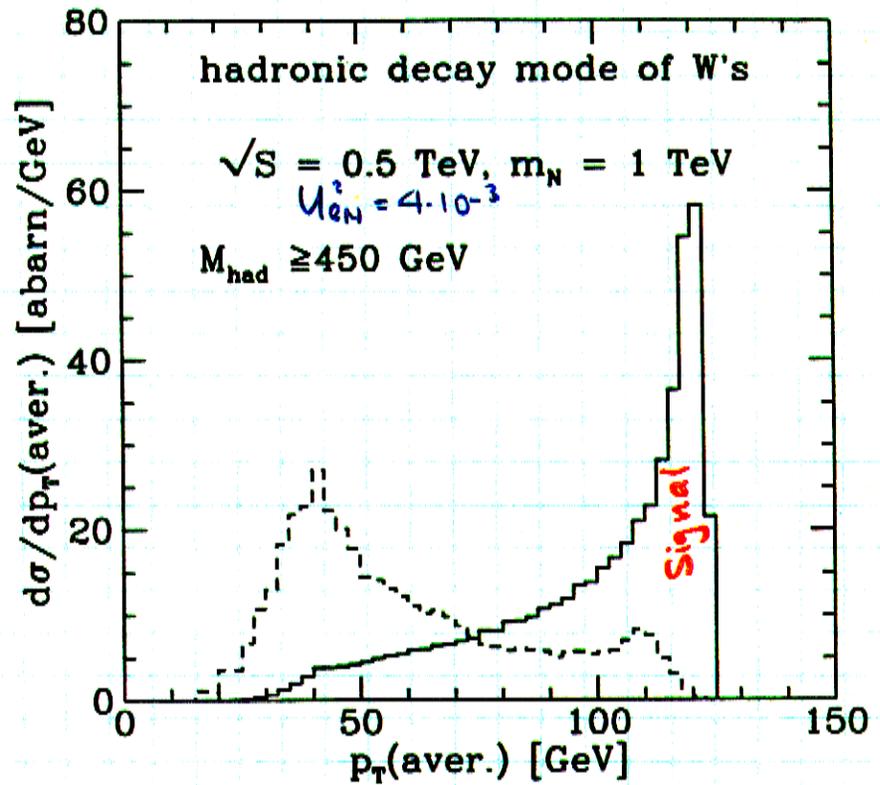
- ALL BACKGROUND GRAPHS COUPLE
A GAUGE BOSON TO e_L

→ CHANGING THE BEATTI POL'N
WILL ELIMINATE ALL 9 TOPOLOGIES
(in the absence of W_R)

tech: $e^-e^- \rightarrow e^-e^- W^+W^-$

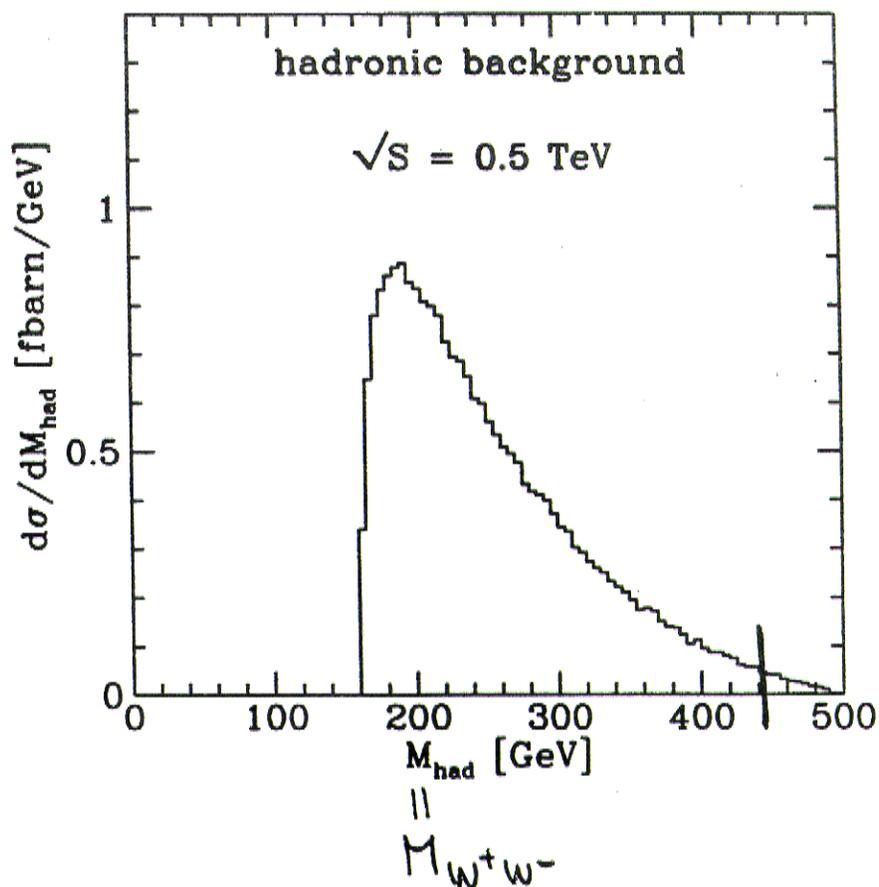
C. Greife

$$\sqrt{s} = 500 \text{ GeV}$$



$$P_{\perp}(\text{aver.}) = \frac{1}{4} \left[|P_{\perp}|^{j+1} + \dots + |P_{\perp}|^{j+4} \right]$$

$e^-e^- \rightarrow W^+W^-e^-e^-$
 in Weizsäcker Williams
 approx.



Make a cut somewhere
 here \rightarrow reduces backgr.
 but not signal

IS THIS COMPATIBLE WITH EVIDENCE

$$\begin{aligned} & \textcircled{\eta^N} \\ & \sim U_{ei} \end{aligned}$$

ON LEPTON FLAVOR VIOLATION:
UNIVERSALITY

A COMPARISON OF

- $\mu^- \rightarrow e^- \bar{\nu}_e \overset{(\gamma)}{\nu}_\mu \iff (A, z) \rightarrow (A, z+1) e^- \bar{\nu}_e$
- $\pi^\pm \rightarrow \mu^\pm \overset{(\gamma)}{\nu}_\mu \iff \pi^\pm \rightarrow e^\pm \overset{(\gamma)}{\nu}_e$
- $\mu^- \rightarrow e^- \bar{\nu}_e \nu_\mu \iff \begin{aligned} e^- &\rightarrow \nu_e \mu^- \overset{(\gamma)}{\nu}_\mu \\ &\rightarrow \nu_e e^- \overset{(\gamma)}{\nu}_e \end{aligned}$

PERMITS A CHECK ON **UNIVERSALITY**

\rightarrow NO SEVERE LIMIT ON $|\eta^{(N)}|$
 $|U_{ei}|$

PARAMETRIZATION OF

$$\begin{aligned} \mu^\pm &\rightarrow e^\pm \gamma, e^\pm e^+ e^- \\ \tau^\pm &\rightarrow \mu^\pm \gamma, e^\pm \gamma \\ \mu(A, z) &\rightarrow e(A, z) \end{aligned}$$

PERMITS SIMILAR ANALYSIS OF
LEPTON FLAVOR VIOLATION

$\mu \rightarrow e \gamma$, eee IS MOST RESTRICTIVE
AND GIVES THE LOWER LIMIT

relative coupling strength

$$r = |V_{ei}^2| / 2 \times 10^{-4}$$

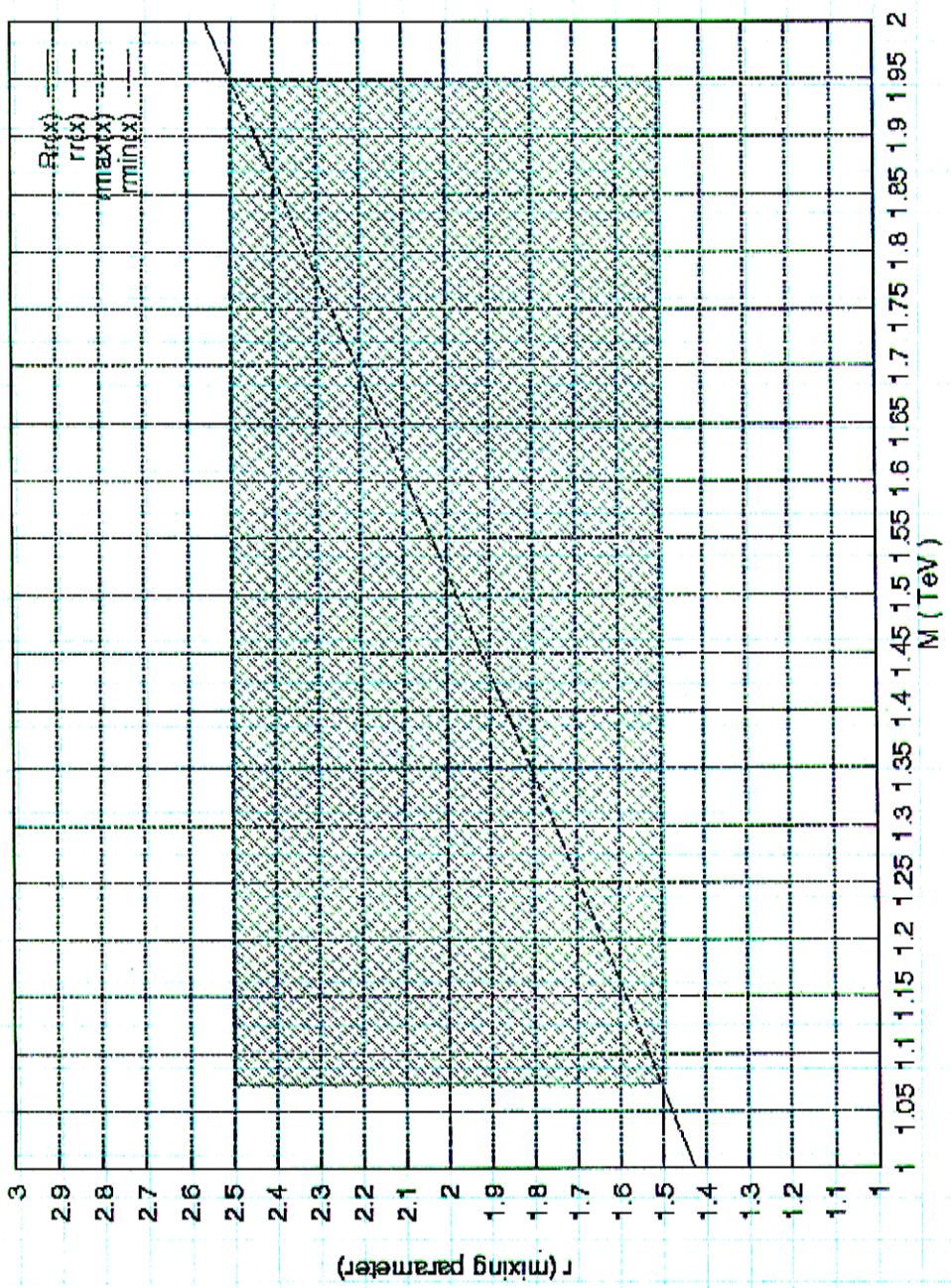


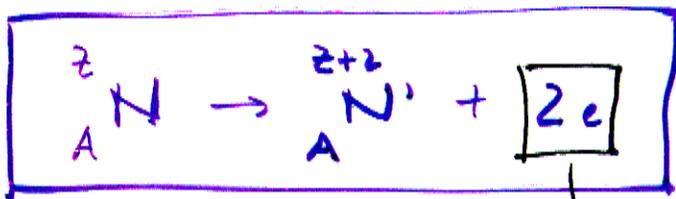
Figure 1: Discovery potential for a heavy neutrino flavor in the coupling and mass parameter space r , M . The range corresponding to $1.5 \leq r \leq 2.5$ is shown as shaded region.

Discovery limit (> 8 events/year) at $\sqrt{s} = 0.5$ TeV e^+e^- colliders

IS SIMILAR INFORMATION AVAILABLE FROM OTHER SOURCES?

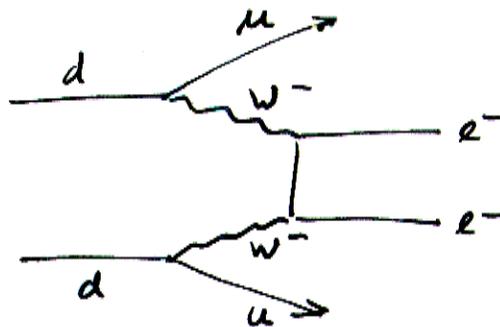
THE CLASSICAL STUDIES OF MAJORANA VS. DIRAC NATURE OF NEUTRINO MASS ARE DONE BY THE SEARCH FOR

NEUTRINO-LESS DOUBLE β DECAY.



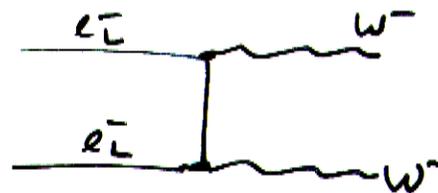
line spectrum

BUT:

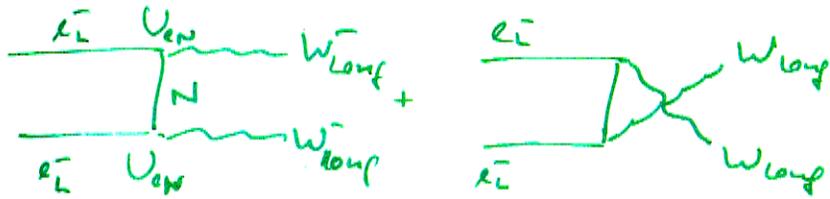


IS **NOT** SIMPLY THE INVERSE

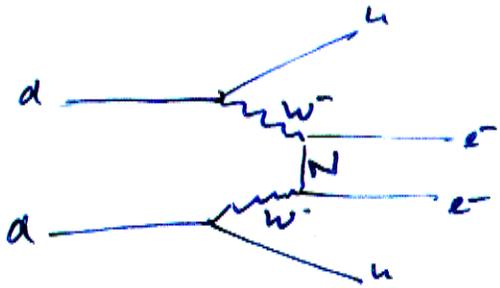
OF



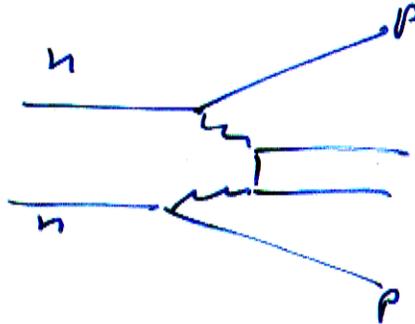
Recall we are comparing



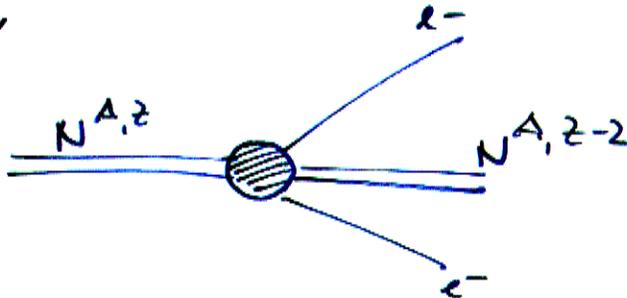
with



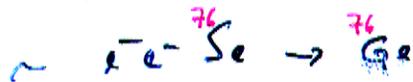
constrained by



constrained by

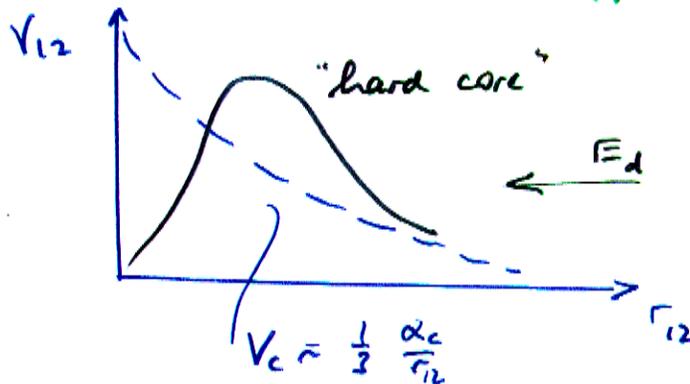


TRUE "INVERSE $\beta\beta$ NOU" WOULD BE ...



TWO d QUARKS FROM 2 NEUTRONS INSIDE THE NUCLEUS
NEED TO APPROACH WITHIN 10^{-16} cm 

THE COLOR COULOMB BARRIER WILL TRY TO
FORBID THAT:



2 neutrons (color-saturated ddu groupings)

will have to approach such that 2 d 's

— one from each n — will be within $\sim 10^{-16}$ cm
of each other

- COLOR FACTOR OF 3
- COULOMB "HARD CORE" PENETRATION
- BREAKING UP COLOR-SATURATED



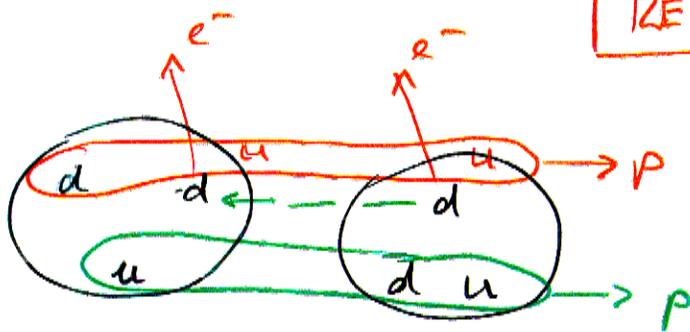
2 possibilities:

○ SPIN - SINGLET $d d$

→ EXCLUSION PRINCIPLE DICTATES

○ COLOR $\bar{6}$ $d d$

REPULSIVE



WE ESTIMATE DEPRESSION

BY A FACTOR OF $> 100!$

○ SPIN - TRIPLET $d d$

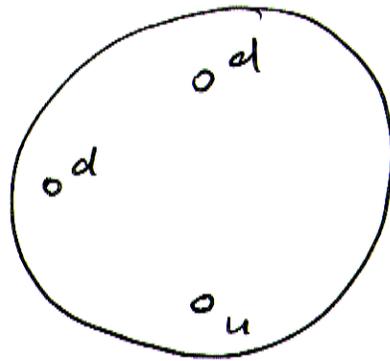
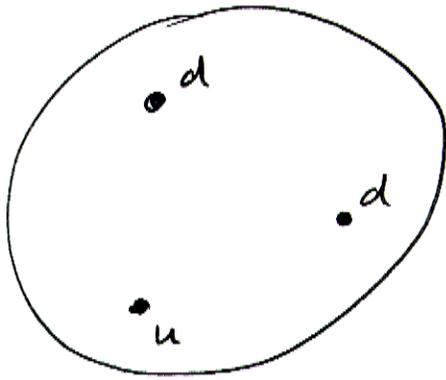
○ COLOR $\bar{3}$ $d d$

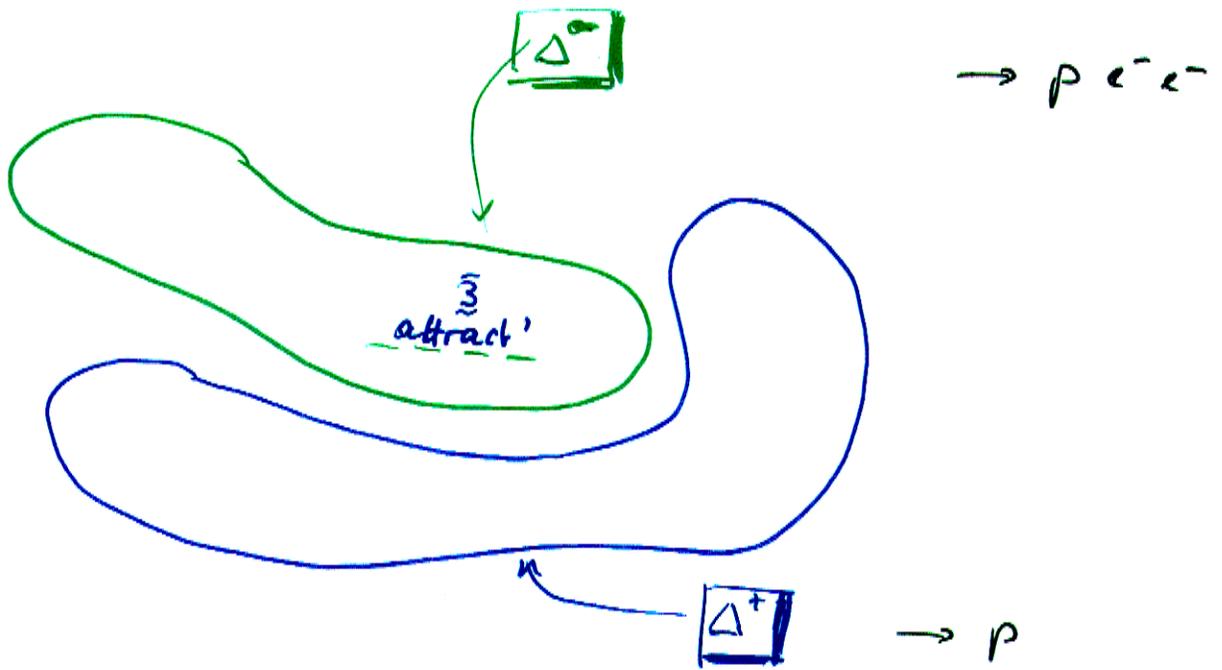
ATTRACTIVE

BUT: ANOTHER SUPPRESSION FROM SPIN dd

$\bar{3}$ CONFIGURATION, POSSIBLE ONLY IN

Δ (inside nucleus)



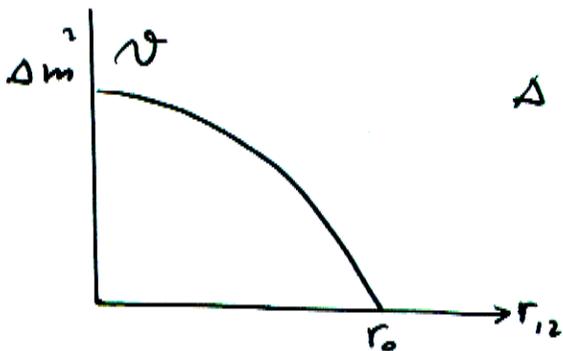


and, of course, the two protons have to find their home in the daughter nucleus



Estimate the threshold ("hard core") to penetrate in this case

$$\frac{S_{dd}}{2} \sim \Delta m^2 \rightarrow p^2 + V$$



$$\Delta m = m(\Delta) - m(n) \approx 0.3 \text{ GeV}$$

$$V_2 \sim \Delta m^2 \left(1 - \frac{v^2}{v_0^2}\right)$$

So, altogether we're looking at a factor

$$\text{for } s \rightarrow nn \rightarrow \Delta^+ \Delta^-$$

with $\Delta m^2 = m_{\Delta}^2 - m_n^2$

$$s \sim \frac{11}{4} \sqrt{\Delta m^2} \tau_{12} (dd)$$

600 MeV

choose $\tau_{12} = 1$ fm for triplet case

$$s = \sqrt{\Delta m^2} \int_0^{\tau_{12}} dr \sqrt{1 - \frac{r^2}{\tau_{12}^2}}$$

→ a more refined treatment leads to a suppression factor of 50-80, to be multiplied by the color suppression factor 3.

BOTH $\left. \begin{array}{l} \text{spin } \underline{1}, \text{ color } \underline{6} \\ \text{spin } \underline{3}, \text{ color } \underline{3} \end{array} \right\}$ eventually lead

to strong suppression of N_H exchange in nuclei

PRESENT OR EXPECTED NON-OBSERVATION OF
 $\beta\beta_{\text{nov}}$ DOES NOT CONSTRAIN $e^- e^- \xrightarrow{N_H} W^- W^-$ SIGNAL

CONCLUSIONS

- THE LINEAR COLLIDER CAN MEASURE W^-W^- PRODUCTION FROM e^-e^- COLLISIONS, MEDIATED BY HEAVY MAJORANA NEUTRINOS.
- SIGNALS ARE UNMISTAKEABLE.
- ENERGIES, LUMINOSITIES OF TESLA, ILC ARE SUFFICIENT.
- EASY POLARIZATION SWITCH FROM $e_L e_L$ TO $e_L e_R$ OR $e_R e_R$ IS VITAL FOR SIGNAL IDENTIFICATION, BACKGROUND SUPPRESSION.
- A SIGNAL FOR N_H OF TEV MASS WILL ALSO ESTABLISH A 10^{-16} cm^2 LOOK AT QUARK-QUARK INTERACTIONS IF N_H IS NOT MEDIATING $\beta\beta_{\text{no } \nu}$
- A N_H SIGNAL WILL HELP TO RESOLVE TWO UNEXPLAINED ODDITIES OF THE S.M. :

$$m_\nu \approx 0$$

$$m_D \text{ vs. } m_H$$

AND DON'T FORGET:

THE CHARACTERISTIC ENERGY
DEPENDENCE OF

$$e^-e^- \xrightarrow{N_m} W^-W^-$$

GIVES A DIRECT MEASUREMENT OF m_{Nm}
AND MIXING PARAMETERS
 U_{ei}

whereas

a signal from $\beta\beta_{\text{nov}}$ is interpretable
by a multiplicity array of processes other
than ν_n - (SUSY graphs, ...)

gives no decisive evidence.

(→ Oxford pres,