

# DO PRECISION ELECTROWEAK CONSTRAINTS GUARANTEE THAT THE NLC CAN FIND AT LEAST ONE HIGGS BOSON OF A TYPE-II 2HDM?

J. F Gunion, LCWS 2000 (FNAL, Oct. 23 – 29, 2000)

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## OUTLINE

- Define the problematical  $[m_h, \tan \beta]$  parameter space wedges.
- Show the  $\Delta\chi^2$  relative to SM fit.
- How fine-tuned are the parameters.
- What is happening analytically?
- What is the required potential form?
- The  $S, T$  plane picture and the Giga- $Z$  option.
- What are discovery possibilities with increased LC  $\sqrt{s}$ , or at LHC, or in  $\gamma\gamma$  collisions.

## The Model

Type-II CP conserving 2HDM with Higgs bosons  $h^0$ ,  $H^0$ ,  $A^0$  and  $H^\pm$ .

## The No-Discovery Wedges

The Scenario: There is only one light Higgs boson,  $h$ , with  $m_h < \sqrt{s} - 2m_t$  in particular (so that  $b\bar{b}h$  and  $t\bar{t}h$  are both allowed), and it has zero tree-level  $WW/ZZ$  coupling. Either

- $h = A^0$ ; or
- $h = h^0$  and  $\sin(\beta - \alpha) = 0$ .

All other Higgs bosons with substantial tree-level  $WW/ZZ$  couplings are too heavy to be produced.

## Will we see the $h$ ?

### One-loop induced couplings are too small.

$WW \rightarrow h$  is best (no off-shell  $s$  in loop) and one finds  $\sigma(WW \rightarrow A^0)/\sigma(WW \rightarrow h_{SM}) \sim \alpha_W^2 \cot^2 \beta$ .  $\Rightarrow < 50$  events for  $L = 2500 \text{ fb}^{-1}$ .

### Need to consider $t\bar{t}h$ and $b\bar{b}h$

- Sum rules for fermionic couplings imply one or both couplings are ok.

$$(\hat{S}_h^t)^2 + (\hat{P}_h^t)^2 = \left(\frac{\cos \beta}{\sin \beta}\right)^2, \quad (\hat{S}_h^b)^2 + (\hat{P}_h^b)^2 = \left(\frac{\sin \beta}{\cos \beta}\right)^2 \quad (1)$$

where ( $f = t, b$ ) couplings are  $\bar{f}(S_h^f + i\gamma_5 P_h^f)fh$  and

$$\hat{S}_h^f \equiv \frac{S_h^f v}{m_f}, \quad \hat{P}_h^f \equiv \frac{P_h^f v}{m_f}, \quad (2)$$

- But, even  $L = 2500 \text{ fb}^{-1}$  is insufficient even at  $\sqrt{s} = 800 \text{ GeV}$  for 50 events if  $\tan \beta$  is in moderate wedge region.

$L=2500 \text{ fb}^{-1}$ , CP-odd  $h=A^0$

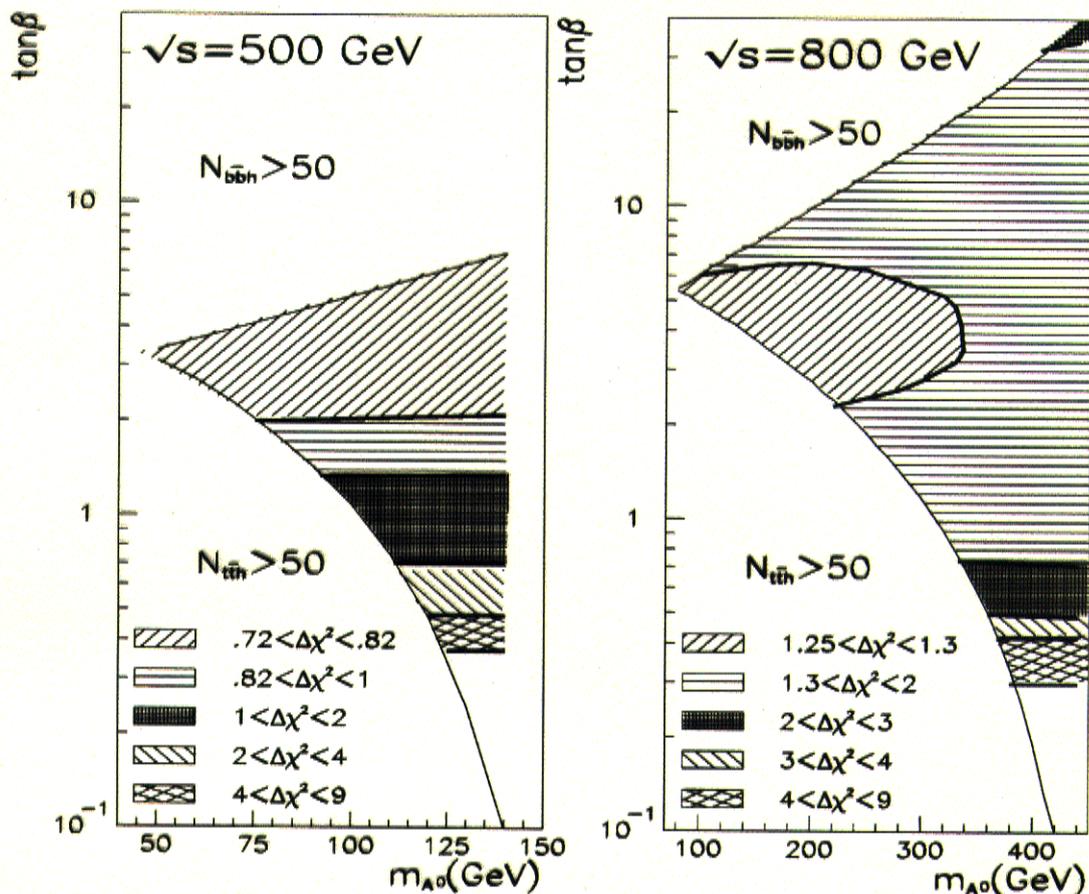


Figure 1: For  $\sqrt{s} = 500 \text{ GeV}$  and  $\sqrt{s} = 800 \text{ GeV}$ , the solid lines show as a function of  $m_{A^0}$  the maximum and minimum  $\tan\beta$  values between which  $t\bar{t}A^0$ ,  $b\bar{b}A^0$  final states will both have fewer than 50 events assuming  $L = 2500 \text{ fb}^{-1}$ . The different types of bars indicate the best  $\chi^2$  values obtained for fits to precision electroweak data after scanning: over the masses of the remaining Higgs bosons subject to the constraint they are too heavy to be directly produced; and over the mixing angle in the CP-even sector.

$L=2500 \text{ fb}^{-1}$ , CP-even  $h=h^0$

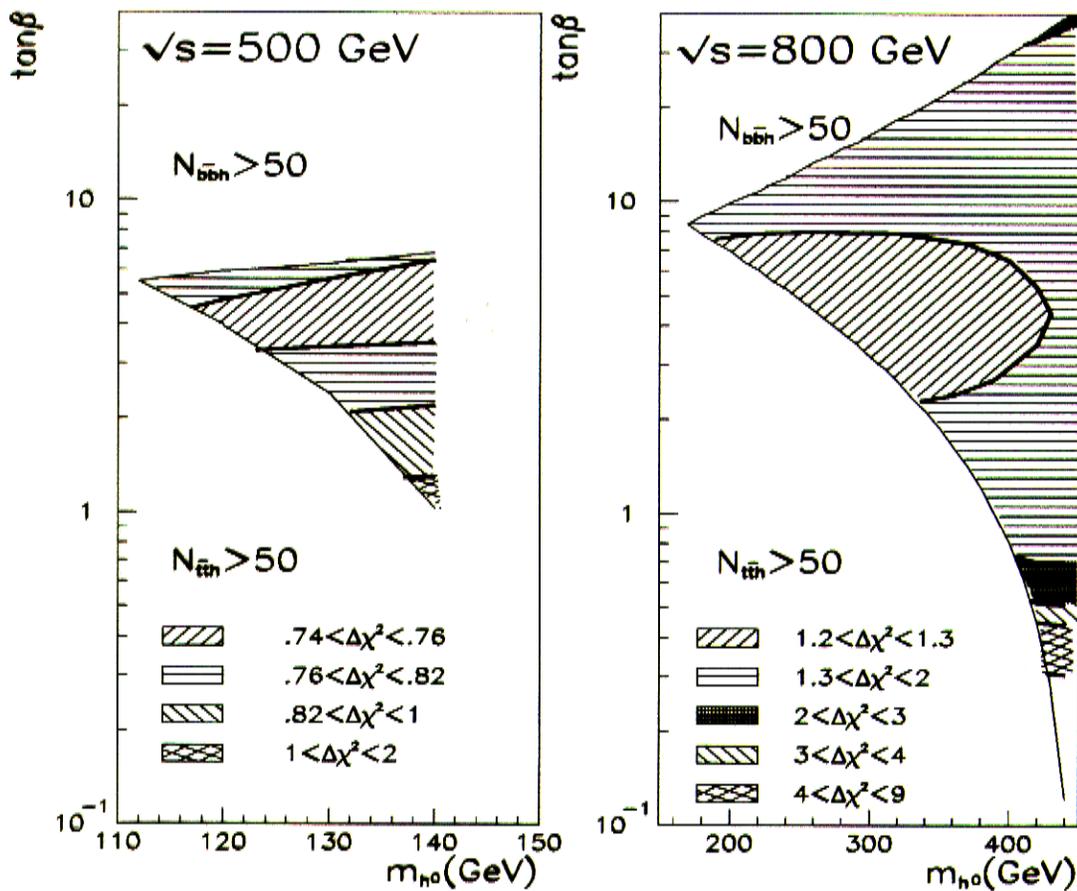


Figure 2: The same as for Fig. 1, except for  $h = h^0$ . The CP-even sector mixing angle is fixed by the requirement  $\sin(\beta - \alpha) = 0$ .

**Conclusion:** the fermionic coupling sum rules do not yield any guarantees. They only restrict the problematical region.

## What about precision electroweak data?

I.e., are wedges ruled out because of bad  $\chi^2$ ? One might think so since the neutral Higgs with  $WW/ZZ$  coupling is required to be heavy. But,  $\Delta\chi^2$  relative to best SM fit is small once  $\tan\beta \gtrsim 1$  (see figures).

The large  $\Delta\chi^2$ 's found for  $\tan\beta < 1$  come from too large an  $R_b$ , although the deviation of  $\Gamma_{\text{tot}}^Z$  also increases.

### Typical case:

$m_{A^0} = 90$  GeV,  $\tan\beta = 2.3$ .

For  $\sqrt{s} = 500$  GeV,  $\Delta\chi_{\text{min}}^2 = 0.78$  is achieved for  $m_{h^0} = \sqrt{s} - 10$  GeV = 490 GeV (i.e. as small as we allow),  $m_{H^0} = 830$  GeV,  $m_{H^\pm} = 850$  GeV, and  $\alpha \sim -0.1\pi$  (corresponding to  $\beta - \alpha \sim \pi/2 \rightarrow h^0 = \text{SM-like}$ ).

In the following table, the observables considered and their pulls are compared for the best fit in this non-discovery case vs. the usual SM fit.

$\Rightarrow$  Some observables are better fit by non-discovery 2HDM parameter choices and some worse. Biggest pull increases are for  $\Gamma_{\text{tot}}^Z$  and  $\Gamma_{\text{had}}^Z/\Gamma_{\text{lep}}^Z$ .

### Sensitivity to inputs:

We have varied inputs such as:

- Whether or not we use running  $m_b$ .
- The value of  $\alpha_s$ .
- The value of  $m_t$ .
- Changing input observable measurements; e.g. using  $m_W^{\text{LEP}}$  from CERN-EXP-2000-016 instead of including LEP2 results of Moriond or Osaka.

$\Rightarrow \Delta\chi^2$  changes resulting from such changes are all  $< 0.1$ .

$\Rightarrow$  We think our results are quite reliable when using SM fit as basis for comparison.

Table 1: Observables considered (TEV stands for Tevatron data) and typical pulls for a 2HDM fit. Pulls are defined as  $(\mathcal{O}_i - \mathcal{O}_i^{\min})/\Delta\mathcal{O}_i$ , where  $\mathcal{O}_i$  is the measured value of a given observable,  $\mathcal{O}_i^{\min}$  is the value for the observable for the best fit choice of parameters, and  $\Delta\mathcal{O}_i$  is the full error (including systematic error) for that observable. The pull results are for  $m_t = 174$  GeV,  $\alpha_s = 0.117$ ,  $m_{A^0} = 90$  GeV,  $\tan\beta = 2.3$ ,  $m_{h^0} = 490$  GeV,  $m_{H^0} = 830$  GeV and  $m_{H^\pm} = 850$  GeV, yielding  $\Delta\chi^2 = 0.78$  relative to the best  $\chi^2$  achieved in the SM-like limit of the 2HDM, for which we also give the pulls for the same  $m_t$  and  $\alpha_s$ . These latter results are quite close to those given in CERN-EXP-2000-016 with the exception of  $m_W^{\text{LEP}}$  for which we have used the Moriond result including LEP2 running. The SM-like 2HDM pulls are essentially identical to those of CERN-EXP-2000-016 if we use  $m_W^{\text{LEP}}$  as quoted there.

$\mathcal{O}$	$m_W^{\text{LEP}}$	$m_W^{\text{TEV}}$	$\sin^2\theta_W^{\text{TEV}}$	$\Gamma_{\text{tot}}^Z$	$\sigma_{\text{had}}^Z$	$\mathcal{A}_e^{\text{LEP}}$
2HDM	0.157	0.880	1.32	-0.972	1.61	0.338
SM	0.370	1.04	1.23	-0.508	1.73	0.167
$\mathcal{O}$	$\mathcal{A}_\tau^{\text{LEP}}$	$\sin^2\theta_{\text{LEP}}^*$	$\Gamma_{\text{had}}^Z/\Gamma_{\text{lep}}^Z$	$A_{FB}^{l\text{LEP}}$	$R_b^{\text{LEP}}$	$R_c^{\text{LEP}}$
2HDM	-0.927	0.522	1.42	0.944	0.733	-0.744
SM	-1.12	0.632	1.13	0.742	0.668	-0.743
$\mathcal{O}$	$A_{FB}^{b\text{LEP}}$	$A_{FB}^{c\text{LEP}}$	$A_{LR}^{b\text{SLD}}$	$A_{LR}^{c\text{SLD}}$	$\sin^2\theta_{\text{SLD}}$	
2HDM	-1.98	-1.22	-0.948	-1.45	-2.26	
SM	-2.29	-1.34	-0.950	-1.46	-1.83	

## Giga-Z?

To increase  $\Delta\chi_{\min}^2 \sim 1$  to  $\Delta\chi_{\min}^2 \sim 3$  need factor of three improvement in both statistical and systematic errors.

Giga-Z factory would probably do the job. More later.

## What if we push up the lightest Higgs mass to $m_h \gtrsim \sqrt{s}$ ?

Table 2: Lower and upper values of  $\tan \beta$ , using the notation  $[\tan \beta_{\min}, \tan \beta_{\max}]$ , at which the given  $\Delta\chi^2_{\min}$  value is crossed for the  $m_h = \sqrt{s} - 10$  GeV cases.

$\Delta\chi^2_{\min}$	1	2	3	4	9
$h = A^0, \sqrt{s} = 500$	[1.8,14]	[0.63,56]	[0.49,75]	[0.44,89]	[0.30, > 110]
$h = A^0, \sqrt{s} = 800$	no	[0.75,47]	[0.46,85]	[0.39,107]	[0.27, > 110]
$h = h^0, \sqrt{s} = 500$	no	[0.92,51]	[0.73,73]	[0.63,86]	[0.45, > 110]
$h = h^0, \sqrt{s} = 800$	no	[1.4,33]	[0.68,78]	[0.55,102]	[0.35, > 110]

While the  $\Delta\chi^2_{\min}$  values increase with increasing  $m_h$ , the  $\Delta\chi^2_{\min}$  values are not bad even if all Higgs are heavy, so long as the other Higgs masses are correlated with one another and  $m_h$  in the best way and  $\alpha$  is chosen appropriately.

**How closely correlated?** i.e. how much fine tuning?

**While the very best  $\Delta\chi^2$  values require careful parameter choices, there are many quite different parameter choices with  $\Delta\chi^2$  not much worse.**

Future Notation:  $H$  is the neutral Higgs that is next-lightest;  $H = h^0$  for  $h = A^0$  and  $H = H^0$  for  $h = h^0$ .

In the  $h = A^0$  case, very often the  $H = h^0$  is SM-like for  $\Delta\chi^2_{\min}$ .

In the  $h = h^0$  case,  $H = H^0$  is automatically SM-like.

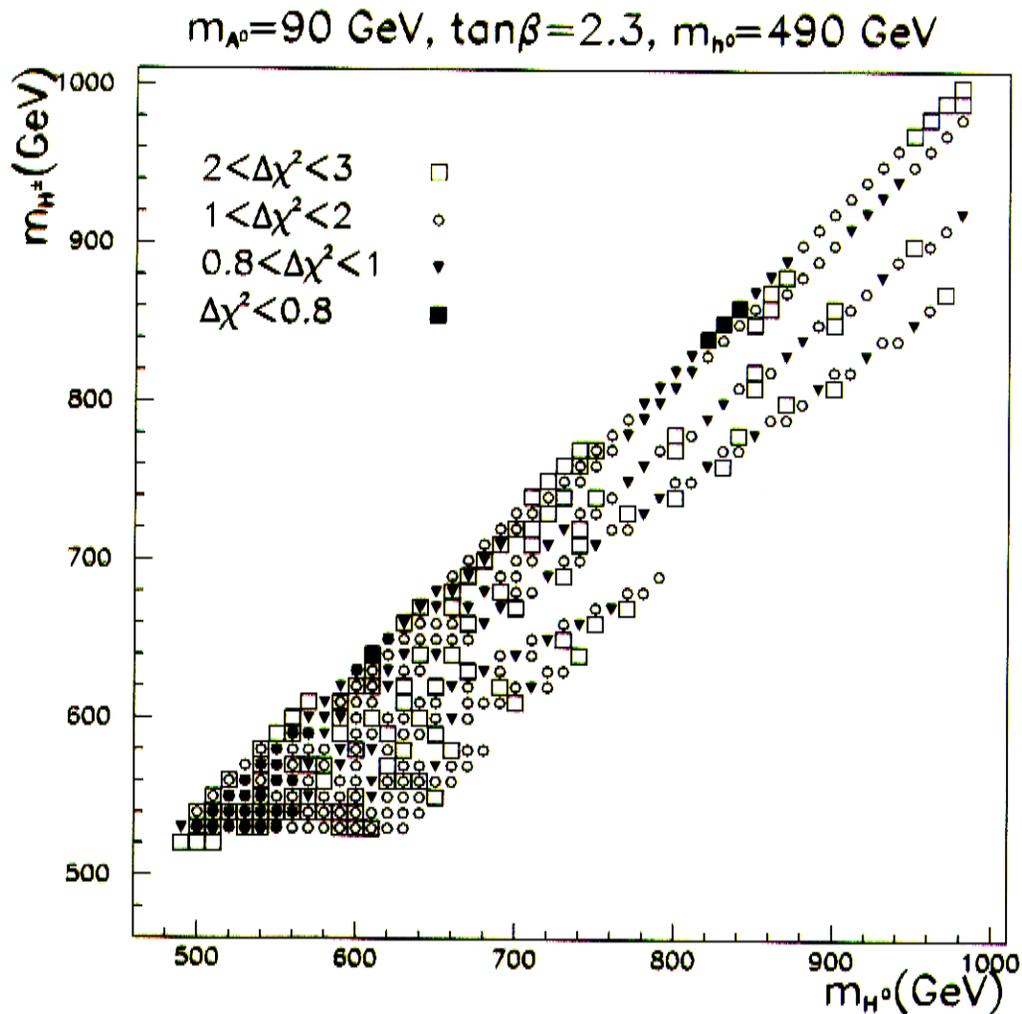


Figure 3: For  $m_{A^0} = 90 \text{ GeV}$ ,  $\tan\beta = 2.3$  and  $m_{h^0} = 490 \text{ GeV}$ , we plot  $m_{H^\pm}$  vs.  $m_{H^0}$  for various ranges of  $\Delta\chi^2$ . Scans in  $m_{H^0}$  and  $m_{H^\pm}$  were done using 10 GeV steps, which leads to some incompleteness in the points for each  $\Delta\chi^2$  range. The scan in  $m_{H^0}$  was limited to  $m_{H^0} < 980 \text{ GeV}$ . Multiple entries at the same  $m_{H^0}, m_{H^\pm}$  location correspond to different  $\alpha$  values.

Note how expanding to  $\Delta\chi^2 = 1$  brings in many very different solutions.

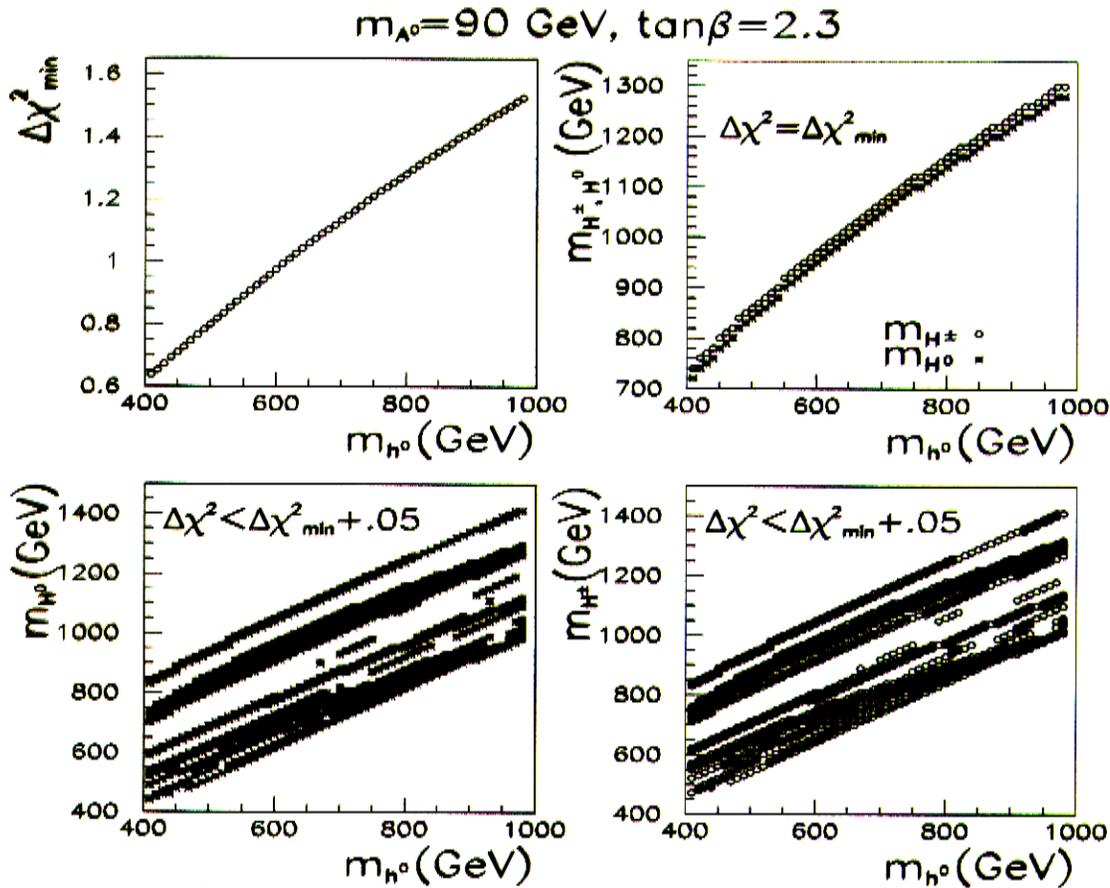


Figure 4: For  $m_{A^0} = 90 \text{ GeV}$  and  $\tan\beta = 2.3$ , we plot vs.  $m_{h^0}$ : a)  $\Delta\chi^2_{\min}$  after scanning over all  $m_{H^0}, m_{H^\pm} > m_{h^0}$  and all  $\alpha$ ; b) the corresponding  $m_{H^0}$  and  $m_{H^\pm}$  values; c) the values of  $m_{H^0}$  for which  $\Delta\chi^2 < \Delta\chi^2_{\min} + 0.05$  is achieved; d) the closely correlated values of  $m_{H^\pm}$  for which  $\Delta\chi^2 < \Delta\chi^2_{\min} + 0.05$  is achieved. Here,  $\Delta\chi^2_{\min}$  is always achieved for  $\alpha = -0.1\pi$  i.e.  $\beta - \alpha \sim \pi/2 \rightarrow$  maximal  $h^0$  coupling to  $ZZ$ .

More on increasing  $m_H$  keeping  $m_h$  and  $\tan\beta$  fixed. Consider case of  $h = A^0$  and  $H = h^0$ .

As  $m_{h^0}$  increases  $\Rightarrow$  slow increase of  $\Delta\chi^2_{\min}$ .

Must maintain small  $m_{H^\pm} - m_{H^0}$  for very best  $\Delta\chi^2$ .

Overall mass scale of  $m_{H^0} \sim m_{H^\pm}$  is quite flexible if allow for just a little extra  $\Delta\chi^2$ ; e.g.,  $m_{H^0} \sim m_{H^\pm} \sim m_{h^0}$  solutions appear.

## How is small $\Delta\chi^2_{\min}$ possible?

Consider  $h = A^0$  and  $H = h^0$ ,  $m_{h^0} > \sqrt{s} - 10$  GeV. For cases such that  $\Delta\chi^2_{\min}$  is achieved with  $\sin^2(\beta - \alpha) \sim 1$ ,

$$\Delta\rho = \frac{\alpha}{16\pi m_W^2 c_W^2} \left\{ \frac{c_W^2 m_{H^\pm}^2 - m_{H^0}^2}{s_W^2} - 3m_W^2 \left[ \log \frac{m_{h^0}^2}{m_W^2} + \frac{1}{6} + \frac{1}{s_W^2} \log \frac{m_W^2}{m_Z^2} \right] \right\} \quad (3)$$

For  $h = h^0$  and  $H = H^0$ , replace  $m_{H^0} \rightarrow m_{A^0}$ ,  $m_{h^0} \rightarrow m_{H^0}$ .

$\Rightarrow$

- For light  $h = A^0$  ( $h^0$ ), small  $m_{H^\pm}^2 - m_{H^0}^2$  ( $m_{H^\pm}^2 - m_{A^0}^2$ ) is always needed for good  $\chi^2$  fits.
- $\Delta\chi^2$  slowly worsens with increasing mass for next lightest Higgs because  $S$  parameter is growing logarithmically.

To good approximation for situations of relevance,

$$S(0) \sim \frac{1}{12\pi} \left( -\frac{5}{3} + \log \frac{m_H^2}{m_W^2} \right), \quad (4)$$

where  $H = h^0$  ( $H = H^0$ ) for  $h = A^0$  ( $h = h^0$ ), respectively.

- But, to repeat: while the best  $\Delta\chi^2$  requires tuning the  $m_{H^\pm}$  mass scale (keeping small splitting with heaviest neutral Higgs) and (for  $h = A^0$  case)  $\alpha$  of CP-even mixing, many other solutions are very nearby.

## Is the required form of the potential natural for small $\Delta\chi_{\min}^2$ ?

The 2HDM potential can be written in terms of the two SU(2) Higgs doublets  $\Phi_1 = (\phi_1^+, \phi_1^0)$  and  $\Phi_2 = (\phi_2^+, \phi_2^0)$  in the form (assuming only soft FCNC-protecting  $Z_2$  symmetry breaking):

$$\begin{aligned}
 V(\Phi_1, \Phi_2) = & -\mu_1^2 \Phi_1^\dagger \Phi_1 - \mu_2^2 \Phi_2^\dagger \Phi_2 - (\mu_{12}^2 \Phi_1^\dagger \Phi_2 + \text{h.c.}) \\
 & + \frac{1}{2} \lambda_1 (\Phi_1^\dagger \Phi_1)^2 + \frac{1}{2} \lambda_2 (\Phi_2^\dagger \Phi_2)^2 + \lambda_3 (\Phi_1^\dagger \Phi_1) (\Phi_2^\dagger \Phi_2) \\
 & + \lambda_4 |\Phi_1^\dagger \Phi_2|^2 + \frac{1}{2} [\lambda_5 (\Phi_1^\dagger \Phi_2)^2 + \text{h.c.}] , \quad (5)
 \end{aligned}$$

where  $\mu_{12}^2$  and  $\lambda_5$  should be chosen real for a CP-conserving Higgs potential. The resulting Higgs masses or mass matrices are then

$$\begin{aligned}
 m_{A^0}^2 &= \frac{\mu_{12}^2}{s_\beta c_\beta} - v^2 \lambda_5, \quad m_{H^\pm}^2 = m_{A^0}^2 + \frac{1}{2} v^2 (\lambda_5 - \lambda_4) \\
 \mathcal{M}^2 &= m_{A^0}^2 \begin{pmatrix} s_\beta^2 & -s_\beta c_\beta \\ -s_\beta c_\beta & c_\beta^2 \end{pmatrix} + v^2 \begin{pmatrix} \lambda_1 c_\beta^2 + \lambda_5 s_\beta^2 & (\lambda_3 + \lambda_4) s_\beta c_\beta \\ (\lambda_3 + \lambda_4) s_\beta c_\beta & \lambda_2 s_\beta^2 + \lambda_5 c_\beta^2 \end{pmatrix} \quad (6)
 \end{aligned}$$

**So long as  $m_{A^0}^2 > 0$ , the CP-conserving minimum is either the only minimum ( $\lambda_5 > 0$ ) or the preferred minimum ( $\lambda_5 < 0$ ).**

For the configurations that minimize  $\Delta\chi^2$ , we always find that  $V$  is close to the form (where  $\lambda_5$  is  $< 0$  in some cases and  $> 0$  in others):

$$V_{\text{quartic}}(\Phi_1, \Phi_2) = \frac{1}{2} \lambda_1 |\Phi_1^\dagger \Phi_1 + \Phi_2^\dagger \Phi_2|^2 - \frac{1}{2} \lambda_5 |\Phi_1^\dagger \Phi_2 - \Phi_2^\dagger \Phi_1|^2, \quad (7)$$

i.e. a weighted sum of the (absolute) squares of the natural symmetric and antisymmetric combinations of the two Higgs doublet fields. This form of the potential guarantees absence of quadratic growth of  $\Delta\rho$  with the masses of the heavier Higgs bosons, i.e. it incorporates a hidden custodial SU(2) symmetry.

## The $S, T$ Plane Picture and Giga- $Z$ .

The 'success' of the 2HDM no-discovery scenarios is easily understood in the  $S, T$  plane.

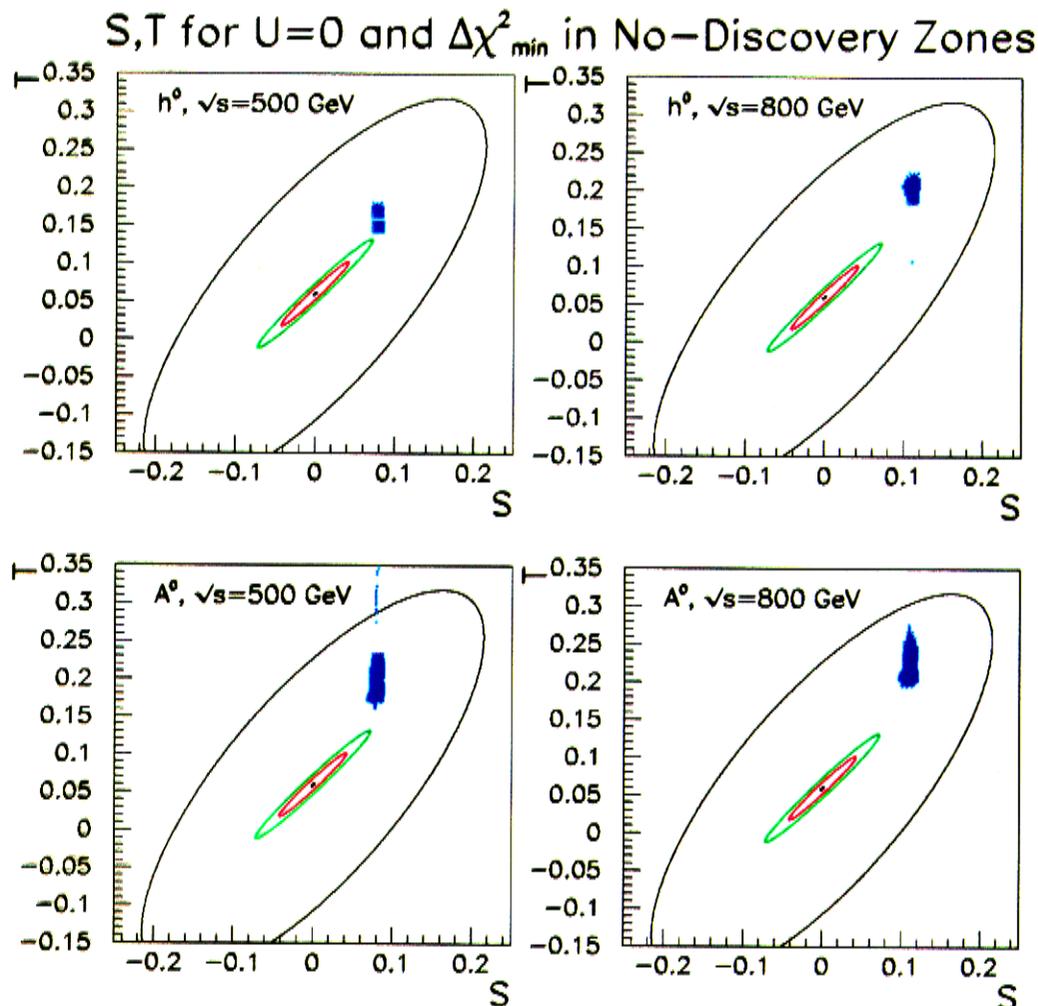


Figure 5: We plot the  $U = 0$  90% CL ellipse in the  $S, T$  plane for a SM Higgs of mass 115 GeV from the latest Erler/Langacker analysis. Also shown are 90% and 99.9% ellipses for Giga- $Z$  using  $U=0$  and error analyses (including correlations) from Erler and from Moenig. The blobs of blue are where our 2HDM no-discovery  $\Delta\chi^2_{\min}$  solutions fall.

### Note:

- 2HDM no-discovery solutions well within current 90% CL ellipse.
- Giga- $Z$  will distinguish, **especially if there is no Higgs discovery at  $\sqrt{s} = 800$ .**
- **Knowing  $U$  will be crucial.** Giga- $Z$  errors shown assume  $m_W$  is measured to 6 MeV using threshold scan.

## Higher energy LC and LHC.

Will increased LC energy or LHC running allow Higgs discovery?

### The $h$ ?

- First, by comparing the  $\sqrt{s} = 500$  GeV and  $\sqrt{s} = 800$  GeV no-discovery wedges, we see that although the  $\tan\beta$  extent of the wedge narrows considerably with increasing  $\sqrt{s}$ , the smallest no-discovery value of  $m_h$  increases rather slowly; thus, one cannot absolutely rely on  $h$  detection at higher LC energy in these scenarios.
- Also, the absence of  $ZZ$  coupling and the moderate value of  $\tan\beta$  implies that the  $h$  will not be detectable at the LHC.

### The other Higgs bosons?

Since  $\chi_{\min}^2$  is always achieved for  $m_H$  at the  $Hb\bar{b}$  threshold and for masses of the other Higgs bosons often much larger than  $m_H$ , the discovery possibilities for the  $H = h^0$  ( $H^0$ ) deserve particular attention in the  $h = A^0$  ( $h^0$ ) cases.

### Cases:

- **Case I:**  $h = A^0$  and  $\Delta\chi_{\min}^2$  when  $H = h^0$  is SM-like.
  - The SM-like  $H = h^0$ .
    - \* For the  $\Delta\chi_{\min}^2$  values of  $m_{h^0}$  and for a substantial range above, the LHC would detect the  $h^0$  in the gold plated  $ZZ \rightarrow 4\ell$  channel.
    - \* As  $e^+e^- \sqrt{s} \rightarrow > 1$  TeV and if  $Zh^0$  and  $\nu\bar{\nu}h^0$  not seen,  $\Rightarrow m_{h^0} \gtrsim 1$  TeV  $\Rightarrow$  strong  $WW$  scattering at LHC and LC.

- \* Precision electroweak fits do not necessarily have particularly bad  $\chi^2$  for such large  $m_{h^0}$  —  $\Delta\chi_{\min}^2$  only increases by  $< 1 - 2$  compared to values obtained for  $m_{h^0} \sim 800$  GeV. (Couplings begin to become non-perturbative and calculations not entirely trustworthy for  $m_{h^0}$  values much above 800 – 900 GeV.)
- \* Although  $b\bar{b}h^0$  opens up as  $\sqrt{s}$  of the LC is increased,  $\sigma(b\bar{b}h^0)$  for a SM-like  $h^0$  is very small at high mass and  $b\bar{b}h^0$  production would not be detectable.

**$\Rightarrow$  Need LC with  $\sqrt{s}$  large enough to probe a strongly interacting  $WW$  sector to be certain of seeing  $H = h^0$  signal.**

- For  $h = A^0$ , the two heaviest Higgs bosons  $H^0$  and  $H^\pm$  have fairly large masses for  $\Delta\chi_{\min}^2$ : 600 – 800 GeV for  $\sqrt{s} = 500$  GeV and  $> 1$  TeV for  $\sqrt{s} = 800$  GeV.
  - \*  $\Rightarrow$  Although  $Z \rightarrow A^0H^0 =$  full strength,  $A^0H^0$  production would become kinematically allowed only with a substantial increase in  $\sqrt{s}$ .
  - \* Small cross sections for Yukawa processes at moderate  $\tan\beta$ ,  $\Rightarrow$  much larger  $\sqrt{s}$  would be needed for  $b\bar{b}H^0$  and  $b\bar{t}H^+ + \bar{b}tH^-$  production. And, much larger  $\sqrt{s}$  would also be required for  $H^+H^-$  and  $t\bar{t}H^0$  production.
  - \* For  $\sqrt{s} = 800$  GeV  $\Delta\chi_{\min}^2$  cases,
    - $\Rightarrow$  A  $\sqrt{s} > 2$  TeV LC needed to see in pair production.
    - $\Rightarrow$  Because of the moderate value of  $\tan\beta$ ,  $\sqrt{s} > 2$  TeV also needed for Yukawa processes.

- \* For moderate  $\tan\beta$  and such large masses,  $H^0$  and  $H^\pm$  detection at the LHC would not be possible due to the smallness of the  $ZZH^0$  and  $WWH^0$  couplings and the very modest size of  $b\bar{b}H^0$  production.

Overall, for the  $h = A^0$  and  $H = h^0$  =SM-like  $\Delta\chi_{\min}^2$  cases, the first focus should be on LHC observation of the  $h^0$  as a resonance or in strong  $WW$  scattering.

- **Case II:**  $h = A^0$ ,  $\Delta\chi_{\min}^2$  achieved for small  $\sin^2(\beta - \alpha)$ , as typified by the moderate  $\tan\beta$ ,  $\alpha \sim 0$  cases.

- The  $H = h^0$  will be hard to detect in the SM-like discovery modes.
- $A^0h^0$  = full strength; observation would be possible when kinematically allowed.

Since our searches required  $\sqrt{s} < m_{h^0} + 10$  GeV,  $\Rightarrow$  need very substantially larger  $\sqrt{s}$  than the assumed value.

- However, in these cases the  $H^0$  has SM-like  $ZZ, WW$  coupling and  $m_{H^0}$  is usually not much larger than  $m_{h^0}$  (which is always  $\sqrt{s} - 10$  GeV for  $\Delta\chi_{\min}^2$ ).

$\Rightarrow H^0$  detection in the gold-plated modes at the LHC or at a  $\sqrt{s} \gtrsim 1$  TeV LC would be possible.

- **Case III:**  $h = h^0, H = H^0$  (with  $H^0$  SM-like); the two heaviest Higgs bosons are the  $A^0$  and  $H^\pm$ .

- $H^0$  detection in gold plated channels should be possible.

- As  $\sqrt{s}$  at the LC is increased,  $h^0 A^0$  production would become kinematically allowed (and be full strength), followed by  $H^+ H^-$  pair production.

- For the moderate  $\tan \beta$  values in question, the Yukawa processes would not be useful (either at the LC or the LHC).

**General Rule:** Good chance of seeing the heavier neutral Higgs with SM-like couplings at  $\sqrt{s} > 1 - 1.5$  TeV LC or at LHC.

**But, no guarantees for  $\sqrt{s} = 800$  GeV.**

## What about $\gamma\gamma$ collisions?

- Assume extreme  $L_{\text{eff}} = 2500 \text{ fb}^{-1}$ .
- Assume superb final state resolution  $\Gamma_{\text{exp}} = 5 \text{ GeV}$ .
- Assume ability to isolate  $b\bar{b}$  final state with no extra jets with high efficiency (**included in above  $L_{\text{eff}}$ !??**).

$\Rightarrow$  Even for low  $h = A^0$  masses (have not yet studied  $h = h^0$ ), there are portions of the wedges for which the  $\gamma\gamma$  signal will be unobservable in the  $b\bar{b}$  final state.

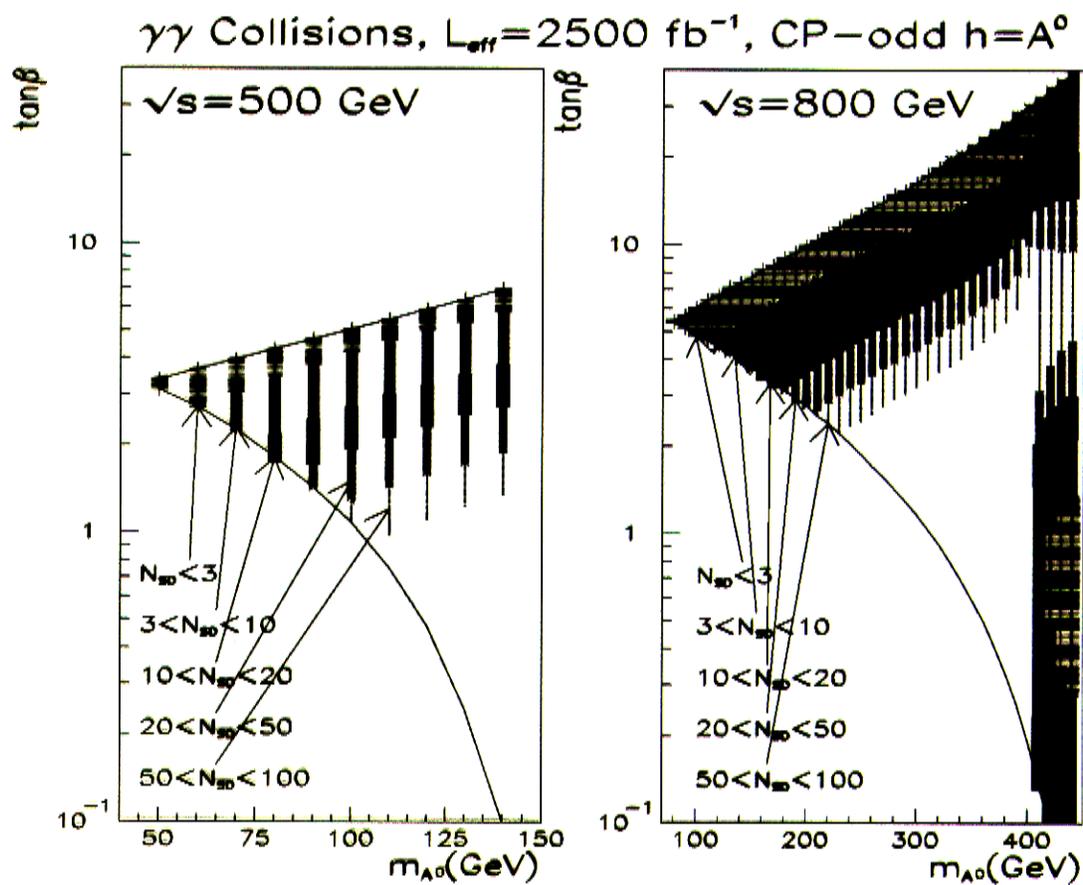


Figure 6: For  $h = A^0$ , we show regions of  $N_{SD}$  levels achieved for a  $b\bar{b}$  signal in  $\gamma\gamma$  collisions assuming  $L_{\text{eff}} = 2500 \text{ fb}^{-1}$  (including tagging and two-jet final state isolation) and an extremely good final state mass resolution of  $\Gamma_{\text{exp}} = 5 \text{ GeV}$ . At each  $[m_{A^0}, \tan\beta]$  point, other 2HDM parameters are taken equal to those that yield  $\Delta\chi_{\text{min}}^2$ .

## CONCLUSIONS

- CP-violating 2HDM can present unpleasant possibilities.
- Giga-Z operation of LC could distinguish between 2HDM no- $e^+e^-$ -discovery scenarios and SM or SM-like 2HDM at  $\gtrsim 99.9\%$  CL, if  $m_W$  threshold scan or other gives  $m_W$  error below 6 MeV.
- $\gamma\gamma$  collisions could allow discovery of the  $h$  (for  $m_h \lesssim 0.8\sqrt{s}$ ) in all but the higher  $\tan\beta$  parts of the no- $e^+e^-$ -discovery wedges.

Of course, the  $m_h \sim \sqrt{s}$  scenarios (which have somewhat higher  $\Delta\chi_{\min}^2$ ) will not be accessible in  $\gamma\gamma$  collisions.