

# 6D Muon Ionization Cooling with an Inverse Cyclotron

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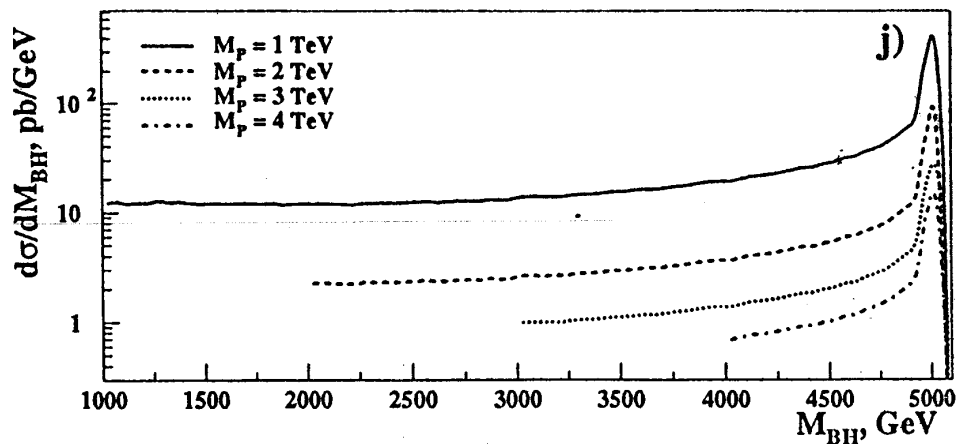
**COOL 05 – International Workshop on  
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## Introduction

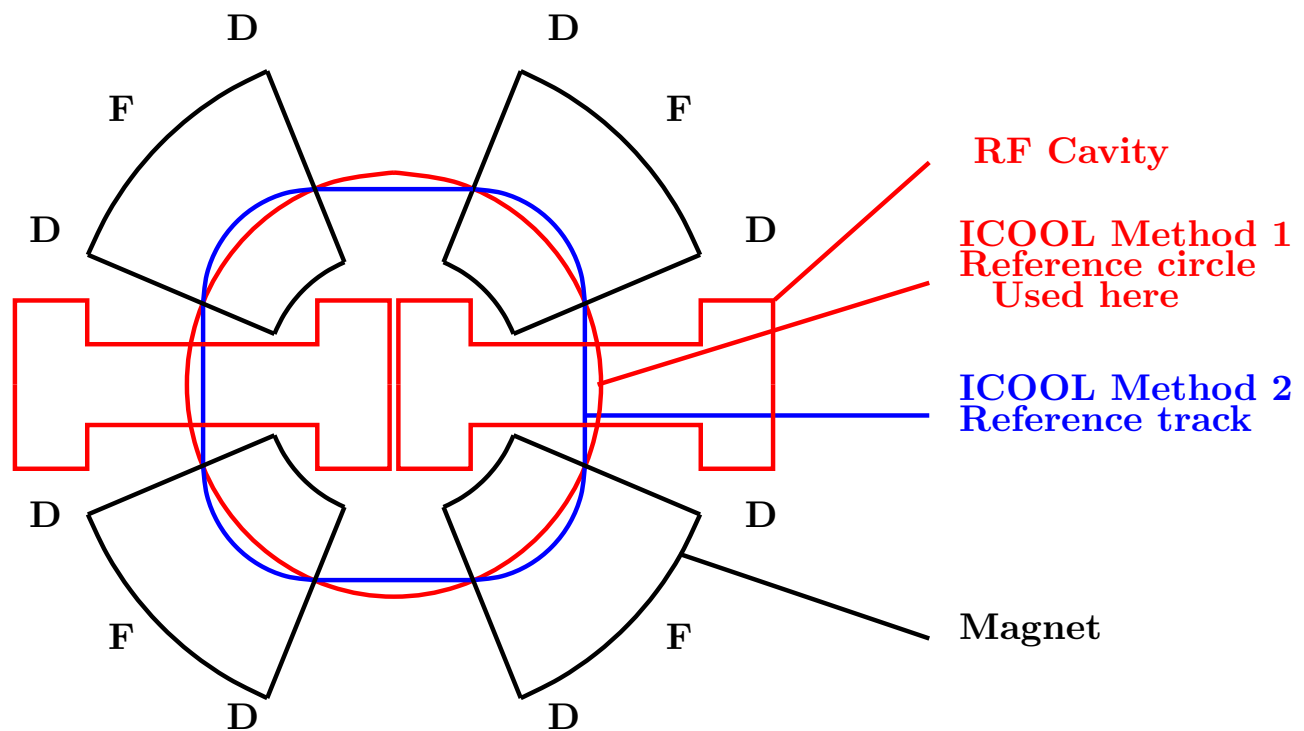
- Ionization cooling is useful for  $\nu$  factories  
( $\mu^- \rightarrow e^- \bar{\nu}_e \nu_\mu$  and  $\mu^+ \rightarrow e^+ \nu_e \bar{\nu}_\mu$ )  
and required for muon colliders.
- A muon collider needs  $10^6$  in cooling.
- $50 \times 6D$  Muon Cooling. Palmer et al.,  
“RFOFO Ionization Cooling Ring,”  
Phys. Rev. ST Acc. Beam 8 (2005) 061003.
- Muon Collider Physics.  
Scanning and splitting  $A^0/H^0$  Higgs.  
Energy Frontier.  
Precision Black Hole Production.

## Physics with Black Hole Systems of Known Mass at a Muon Collider

- Only  $\mu^+\mu^-$  might produce black holes/initial gravitons of known mass.
- Known mass could be critical in measuring: Quantum Black Hole Remnants, Scanning production turn on, Initial/final gravitons as missing energy.
- The ILC  $e^+e^-$  energy is too low.
- CLIC  $e^+e^-$  suffers from beamstrahlung. 5 TeV spectrum from Greg Landsberg.

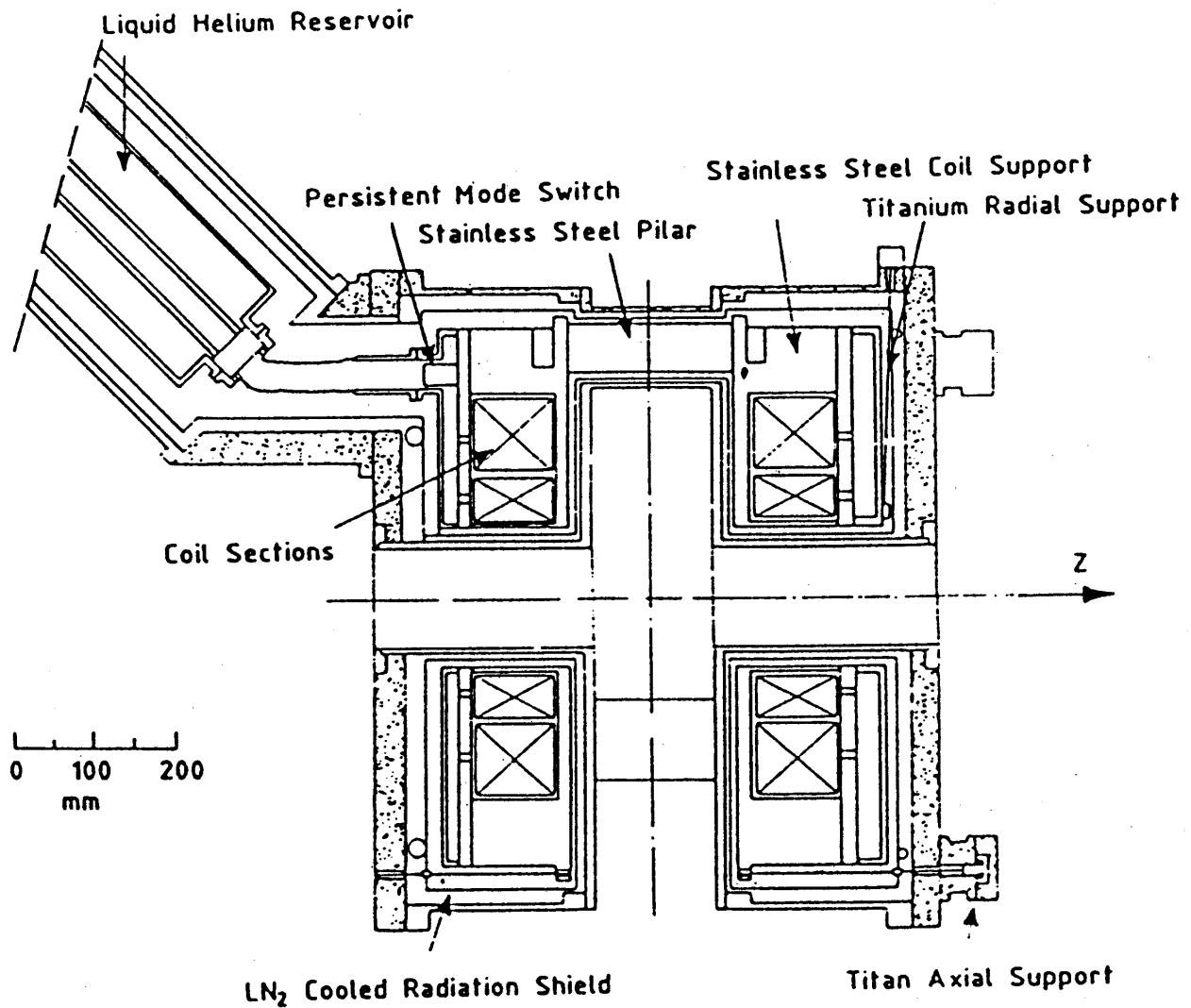


# Large Admittance Sector Cyclotron



- **COOL 05: A. Garren, H. Kirk, S. Kahn, “6D Cooling of a Circulating Muon Beam.”**

# LEAR $\bar{p}$ Azimuthally Symmetric 3 Tesla Cyclotron



- NIM A278 (1989) 368.

## LEAR $\bar{p}$ Azimuthally Symmetric 3 Tesla Cyclotron

- $dE/dx$  Injection radius = 120 mm,  
 $p = 105 \text{ MeV}/c$ , 0.3 mbar hydrogen
- $\bar{p}$  adiabatically spiral to the center.
- Swarm:  $KE = 2 \text{ keV}$ ;  $r, h = 15, 40 \text{ mm}$
- 20 microsecond spiral time for 0.3 mbar
- 1 microsecond spiral time for 10 mbar
- Pulsed axial electric kicker  
80 ns pulse, 20 ns rise, 500 V/cm  
Anti-protons moves 32 cm in 500 ns  
Lighter muons will go farther ( $F=ma$ )
- A bunch train is coalesced into a swarm.

## Halliday and Resnick

- Cyclotron frequency

$$f = \omega/2\pi = qB/2\pi m$$

- $f_{\bar{p}} / f_{\mu} = 938/106 = 8.8$

1  $\mu\text{S}$  spiral  $\rightarrow$  0.11  $\mu\text{S}$  spiral

## LEAR→PSI: NIM A394 (1997) 287

- A New Method to Produce Negative Muon Beam of keV energies
- Foil: 3 nm of nickel ( $3 \mu\text{g}/\text{cm}^2$ ) on Formvar 30 min. of sputtering – Franz Kottmann

### Cyclotron trap at PSI

$10^5 \mu^-/\text{s}$  @ 20...50 keV  
scale by  $10^6 \rightarrow N_{\mu^-} = 10^{11} / \text{s}$

$v_{\mu^-} = 1.5 - 30 \text{ cm}/\mu\text{s}$

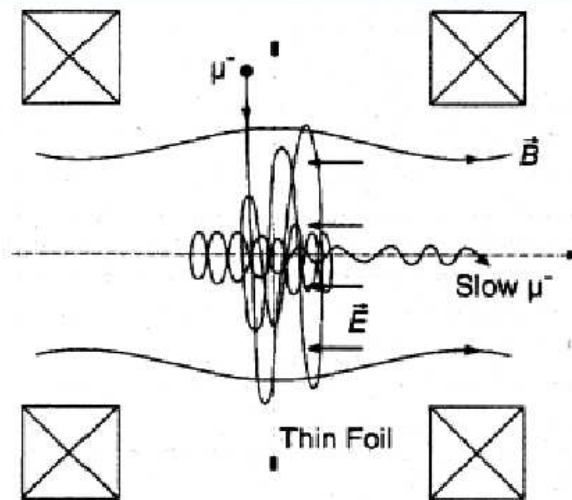


Fig. 2. Principle of the extraction method.



# Damped Harmonic Oscillator

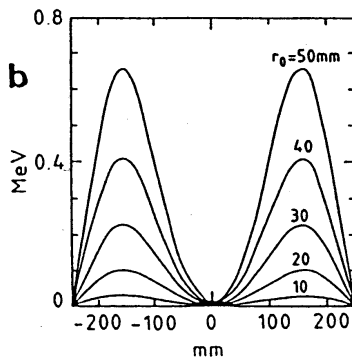
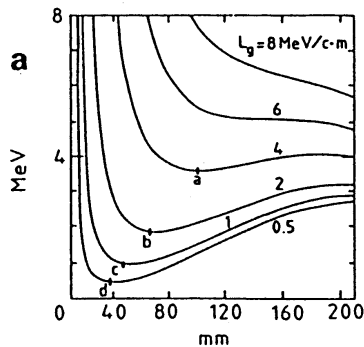
- Generalized Angular Momentum

$$L_g = L_z - e r A_\theta, \quad \text{NIM A278 (1989) 368}$$

- Quasipotential Well,  $\eta = e/M$

$$U(r,z) = V(r,z) - (1/2\eta r^2) (L_g/M + \eta r A_\theta)^2$$

- (a)  $U'(r,0)$ [MeV] vs  $r$  [mm] for various  $L_g$   
a, b, c, and d are stable orbit radii
- (b)  $[U'(r_0,z) - U'(r_0,0)]$  [MeV] vs  $z$  [mm] for various  $r_0$
- Muons are ferried by the well to a central swarm.



## Space Charge

- Put  $10^{12}$  muons at a point

Take  $B = 1.0$  Tesla

$$F = m v^2 / r = qQ / 4\pi\epsilon_0 r^2 + qvB$$

$$r = [mv^2 \pm \sqrt{m^2v^4 - 4(qvB)(qQ/4\pi\epsilon_0)}] / (2qvB)$$

$$r(15 \text{ MeV}/c, .14c) = 48 \text{ mm}$$

$$r(6 \text{ MeV}/c, .06c) = 14 \text{ mm}$$

$$r(5 \text{ MeV}/c, .05c) = \text{imaginary}$$

- Ionized gas can automatically neutralize space charge! Phys. Rev. 72 (1947) 989, Lloyd Smith, W. Parkins, A. Forrester, “On Separation of Isotopes in Quantity by Electromagnetic Means.”

## Avoid Slow Muon Capture

- Slow muons like to stick to hydrogen

- Positive muons

Helium gas to inhibit muonium formation.

- Negative muons

Deuterium gas. Fusion frees muons.

10% sticking factor.

$d + d \rightarrow {}^3\text{He} + n + 3.3 \text{ MeV}$  or  $t + p + 4.0 \text{ MeV}$ .

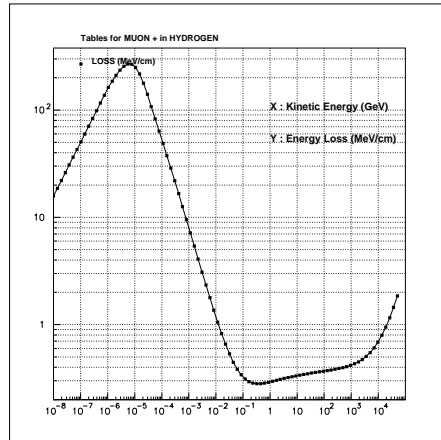
L. Ponomarev, Contemp. Phys. 31 (1990) 219

- Lower gas pressure so muons won't range out before they spiral all the way in.
- Lower gas pressure so a lower electric field can kick a swarm out after it has built up.

## Busch's Theorem and Ejection

- Accelerator Physics and Engineering  
A. W. Chao and M. Tigner, page 101
- $\dot{\phi} = [e/2\pi \gamma m r^2(s)][\Phi(s) - \Phi_k]$   
 $\phi$  is the azimuthal angle  
 $r(s)$  is the radius of the beam edge  
 $\Phi(s)$  is the magnetic flux ( $\pi r^2 B_s$ ) at  $s$   
 $\Phi_k$  is the flux ( $\pi r^2 B_k$ ) at the cathode
- $L_z = r^2 \gamma m \dot{\phi} = -e B r^2 / 2 = x p_y - y p_x$
- $L_z = 0.3 (0.5 \text{ Telsa}) (0.05 \text{ m})^2 / 2 = .0002$
- $L_z = 200 \text{ MeV}/c - \text{mm}$
- $L_z = 4 \text{ MeV}/c \times 50 \text{mm}$
- An 4 MeV/c kick is moderately large.
- Accelerate, reverse/increase B, absorb  $L_z$ .

# Initial GEANT Simulations



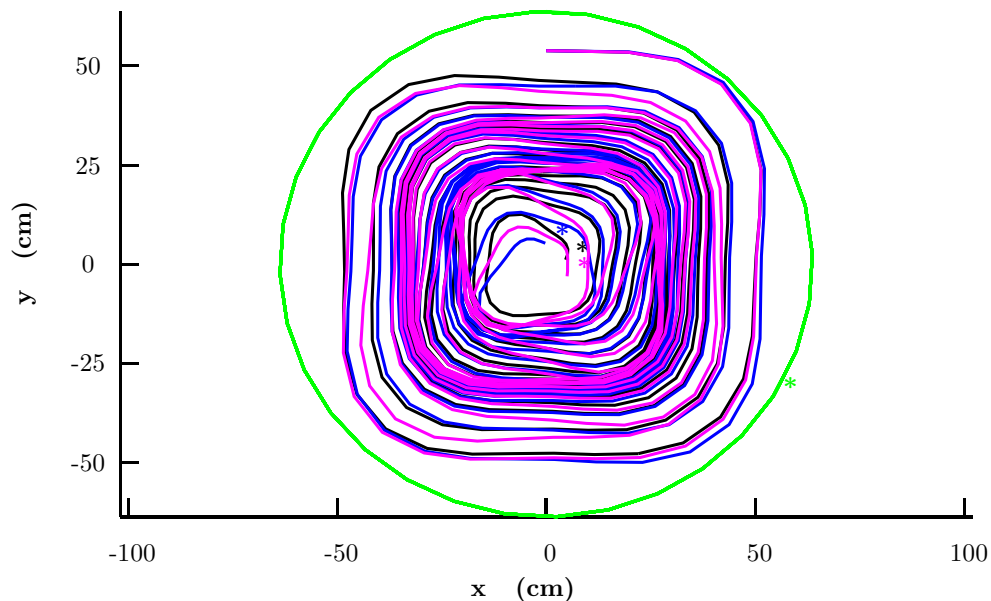
- $\mu^+$   $dE/dx$  (MeV/cm) vs. KE (GeV) in LH<sub>2</sub>



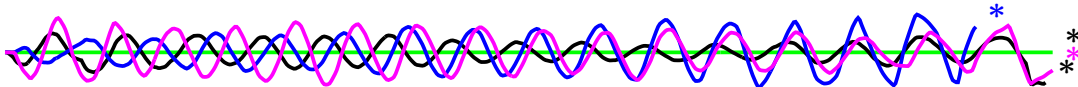
- Muon spirals in 50 atm of H<sub>2</sub>, uniform B

## Single Turn Energy Loss Injection

- Four Magnet (1.8T) Sector Cyclotron. Soft edged fields, ICOOL simulation. Multiple scattering and straggling on. Radial LiH wedges surrounded by hydrogen. Matter decreases adiabatically with radius. 3 identical 172 MeV/c muons are injected.



- $\pm 5$  cm vertical motion along the 70 m spiral



- Injection scaling relation:  $\Delta p = .3 B \Delta r$ .

## Emittance Reduction Goals

- A muon collider needs  $10^6$  cooling.
- $\epsilon = (\Delta p_x \Delta x) (\Delta p_y \Delta y) (\Delta p_z \Delta z)$
- $\Delta p_x$ : 30 MeV/c  $\rightarrow$  0.3 MeV/c
- $\Delta p_y$ : 30 MeV/c  $\rightarrow$  0.3 MeV/c
- $\Delta p_z$ : 30 MeV/c  $\rightarrow$  0.3 MeV/c
- $\Delta x$ : 70 mm  $\rightarrow$  50 mm
- $\Delta y$ : 70 mm  $\rightarrow$  50 mm
- $\Delta z$ : 10000 mm  $\rightarrow$  50 mm
- In:  $10\times$  transverse cooler, physics/0411123.
- Out: “Frictional  $\mu$  cooling,”  
H. Abramowicz, A. Caldwell, R. Galea, and  
S. Schlenstedt, NIM A546 (2005) 356.

## Summary

- Large admittance sector cyclotron.
- Tangential energy loss injection.
- Absorber  $\rho$  decreases smoothly with  $r$ .
- LiH wedges in low pressure gas.
- Muons ferried in well to center as  $\Delta L \rightarrow 0$ .
- As  $p \rightarrow 0$ ,  $\Delta p \rightarrow 0$ .
- Helium gas inhibits  $\mu^+ e^-$  formation.
- Deuterium gas frees  $\mu^-$  via fusion.
- Central magnetic bottle holds muon swarm.
- A bunch train is coalesced.
- Axial ejection with an electric kicker.