

Intersecting D-branes, Fluxes and ``Realistic'' Particle Physics

I. Supersymmetric Standard Model constructions w/ D-branes

Recent progress w/ systematic constructions: w/ I. Papadimitriou '03

w/ T. Li and T. Liu, hep-th/0403061

w/ P. Langacker, T. Li, and T. Liu, hep-th/0407178

II. D-branes and Fluxes (moduli stabilization)

Standard-like Models with 3 & 4-chiral families & up-to 3-units of flux

w/ T. Liu hep-th/0409032; w/ T. Li and T. Liu, hep-th/0501041

Phenomenology of flux models w/P.Langacker,T.Li and T.Liu, to appear

Pedagogical review

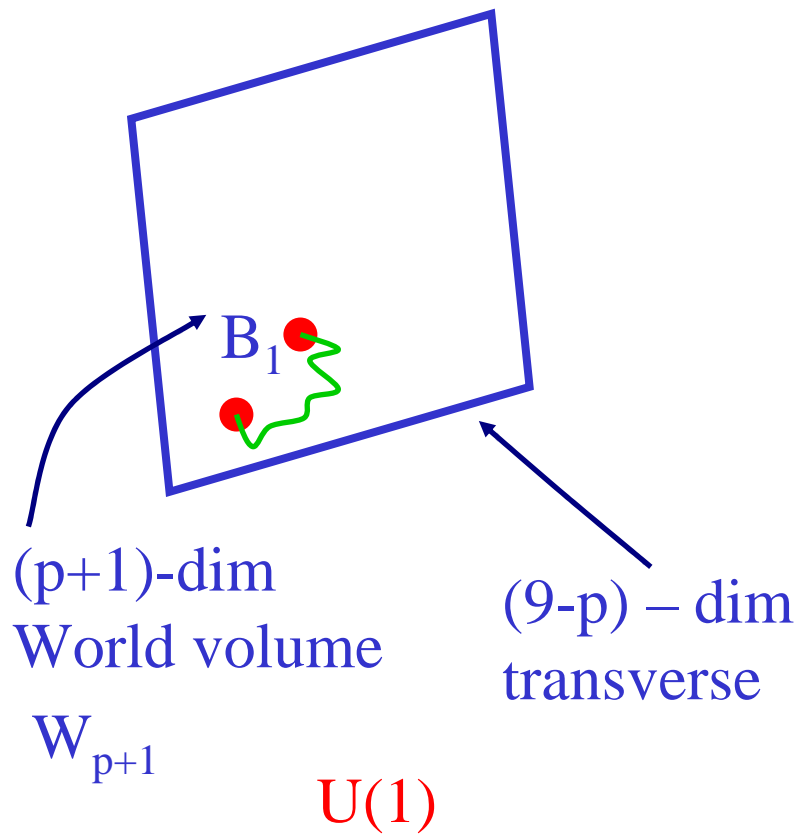
w/R. Blumenhagen,P.Langacker&G. Shiu, hep-th/0502005

Outline

- **Constructions w/ intersecting D-branes:**
 - Geometric origin of non-Abelian gauge symmetry & chirality**
 - [Standard Model $SU(3)_C \times SU(2)_L \times U(1)_Y$ & 3-families: $Q_L \sim (\underline{3}, \underline{2}, 1/6)$ –quarks $L \sim (\underline{1}, \underline{2}, -1)$ –leptons]
- **Supersymmetric intersecting D-branes on orbifolds:**
 - explicit constructions of **supersymmetric Standard Models** (spectrum, couplings)
 - systematic constructions
- **Moduli stabilization – Fluxes**
 - explicit examples of **Standard Models w/ fluxes**
- **Conclusions/outlook**

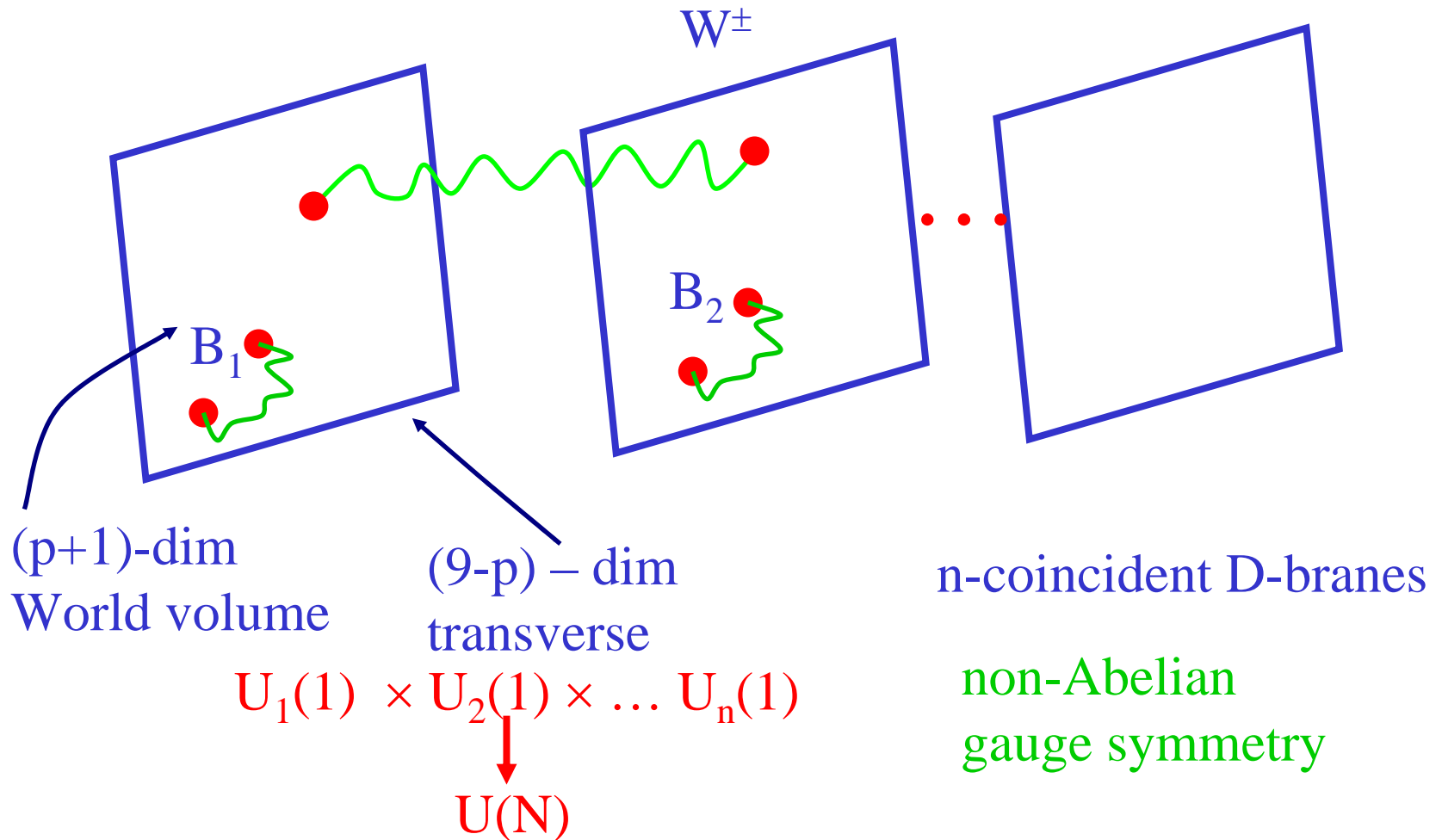
D-branes & non-Abelian gauge theory

D p-branes



D-branes & non-Abelian gauge theory

D p-branes



Compactification

D=10

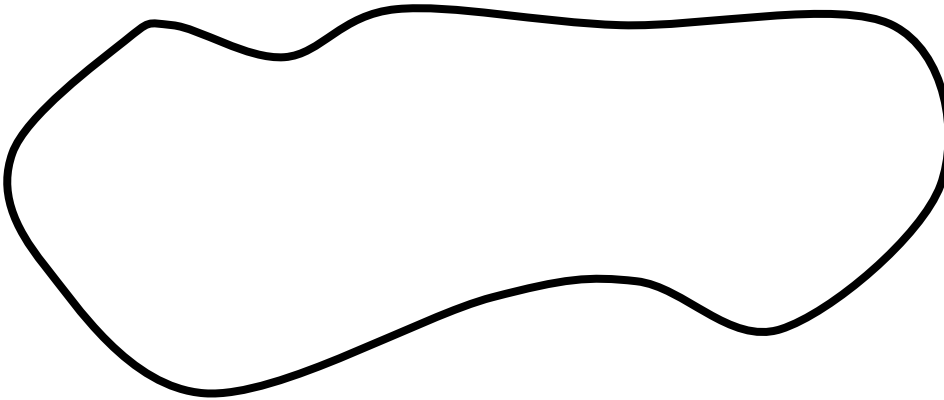


D=4

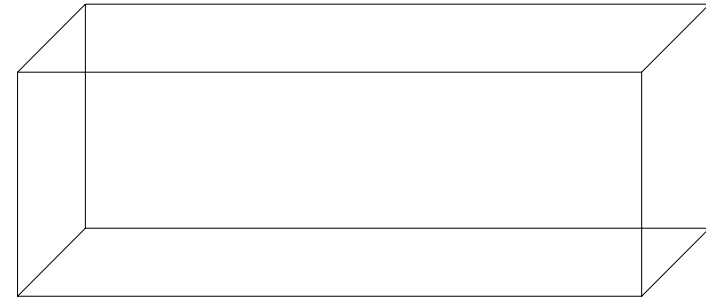
&

N=1 supersymmetry

X_6 - Calabi-Yau \times $M_{(1,3)}$ Minkowski



\times



Compactification

D=10

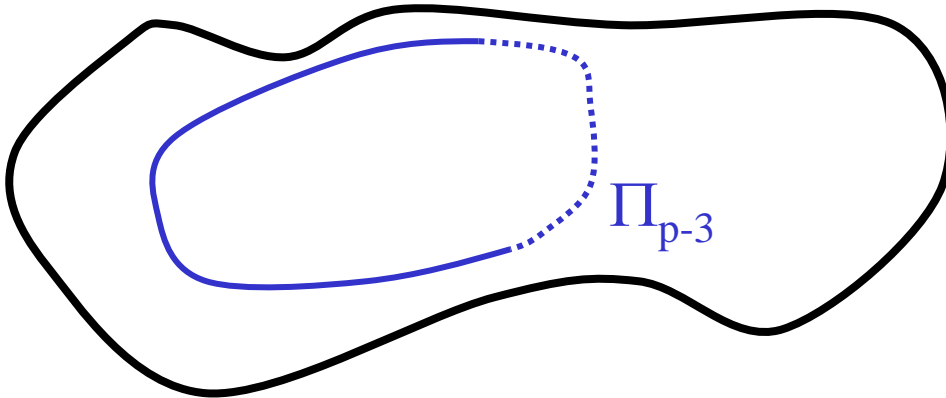


D=4

&

N=1 supersymmetry

X_6 - Calabi-Yau \times $M_{(1,3)}$ Minkowski



\times



D p-branes – $W_{p+1} \equiv \Pi_{p-3} \times M_{(3,1)}$
 Wrap – (p-3) cycles of X_6

Compactification

D=10

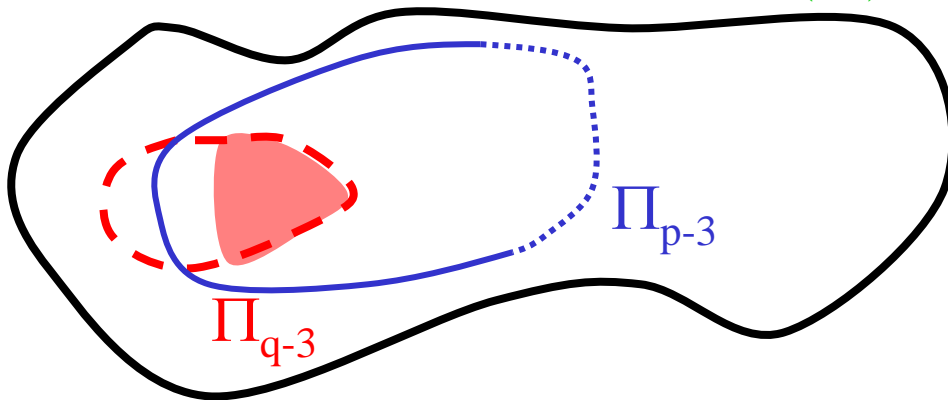


D=4

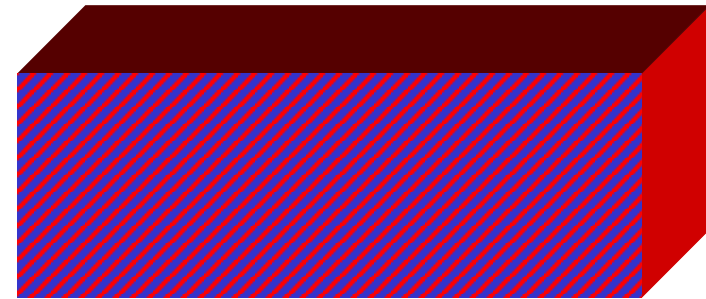
&

N=1 supersymmetry

X_6 - Calabi-Yau \times $M_{(1,3)}$ Minkowski



\times



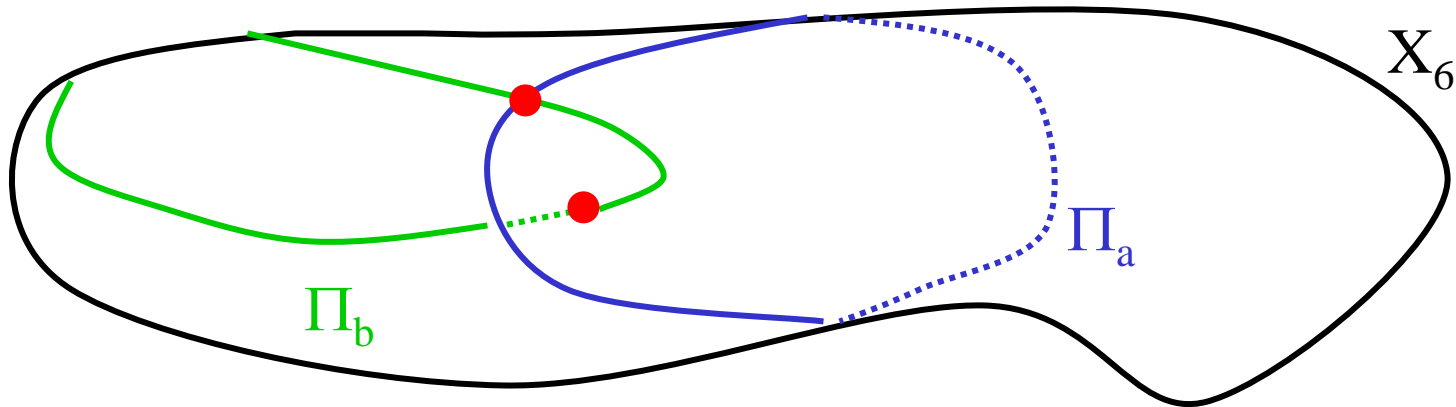
D p-branes – $W_{p+1} \equiv \Pi_{p-3} \times M_{(3,1)}$
 Wrap – (p-3) cycles of X_6

D q-branes
 Wrap (q-3) cycles

$\left. \begin{array}{l} \Pi_{q-3} \cap \Pi_{p-3} \\ \Pi_{q-3} \subset \Pi_{p-3} \end{array} \right\} \text{Rich structure}$

Focus on D6-branes – Realistic Particle Physics

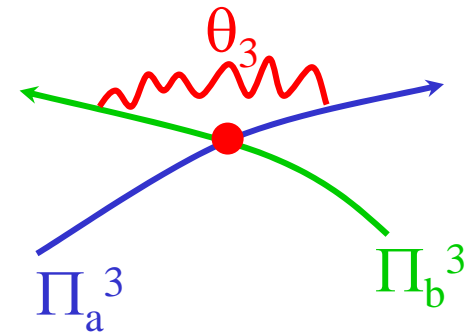
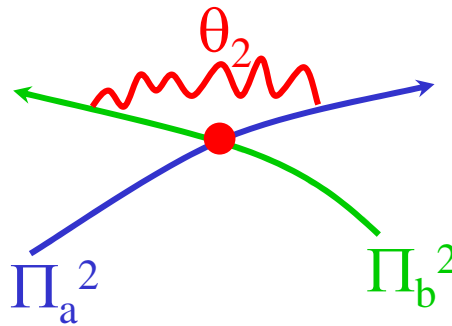
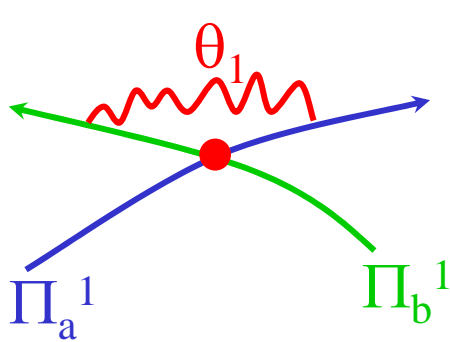
wrap 3-cycles Π



In internal space intersect at points:

$[\Pi_a] \circ [\Pi_b]$ - **topological number**

$\Pi_a = \Pi_a^1 \otimes \Pi_a^2 \otimes \Pi_a^3$ – **Factorizable 3-cycles**



At each intersection – massless 4d fermion ψ !
Geometric origin of chirality!

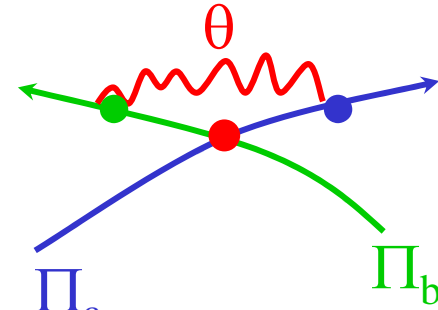
Berkooz, Douglas & Leigh '96

Engineering of Standard Model

N_a - D6-branes wrapping Π_a

N_b - D6-branes wrapping Π_b

$$\Psi \sim \left(\begin{array}{c} U(N_a) \\ N_a \end{array} \right) \times \left(\begin{array}{c} U(N_b) \\ \overline{N_b} \end{array} \right) - [\Pi_a]^\circ[\Pi_b] - \text{number of families}$$



$$N_a = 3, \quad N_b = 2, \quad [\Pi_a]^\circ[\Pi_b] = 3$$

$$U(3)_C \times U(2)_L$$

$\Psi \sim (3, 2) - 3$ copies of left-handed quarks

&

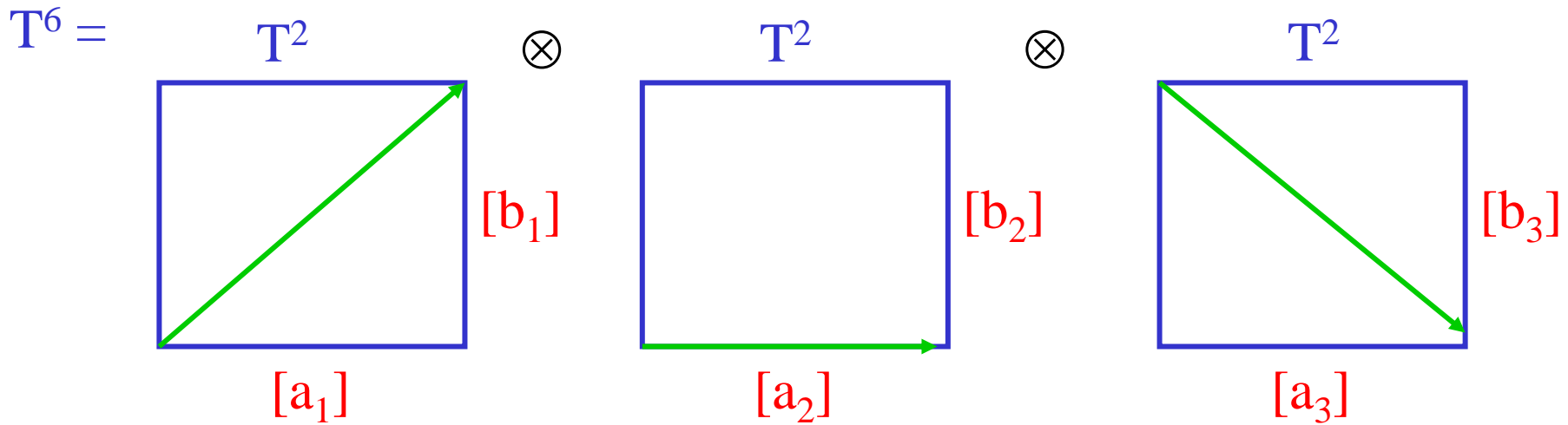
global consistency conditions & supersymmetry (later)



Building Blocks of the Supersymmetric Standard Model

Toroidal/Orbifold compactifications (calculation of spectrum w/ CFT-techniques)

$$T^6 / (Z_N \times Z_M)$$



$$(n_a^i, m_a^i) =$$

$$(1, 1)$$

$$(1, 0)$$

$$(1, -1)$$

$$[\Pi_a] =$$

$$[\Pi_a^1]$$

$$\otimes$$

$$[\Pi_a^b]$$

$$\otimes$$

$$[\Pi_a^c]$$

$$[\Pi_a^i] = n_a^i [a_i] + m_a^i [b_i]$$

homology class
of 3-cycles

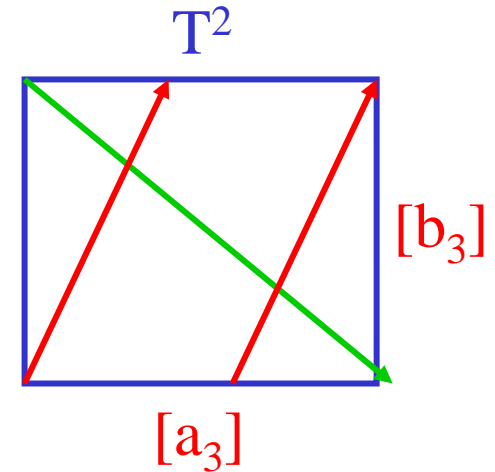
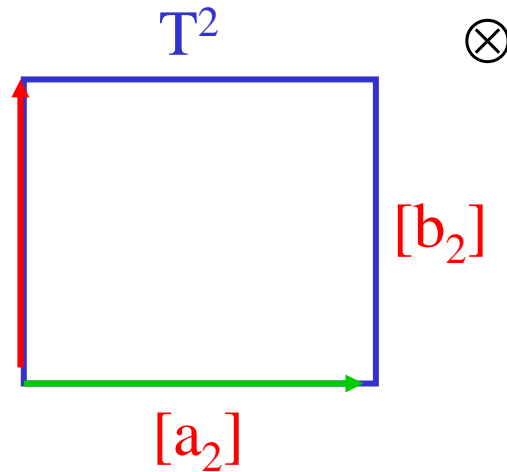
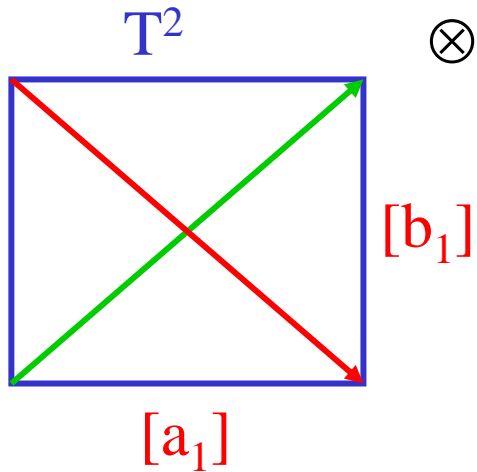
$$[N_a, n_a^i, m_a^i]$$

Toroidal/Orbifold compactifications

$$T^6 / (Z_N \times Z_M)$$

CFT-technique

$$T^6 =$$



$$(n_a^i, m_a^i) =$$

$$(1, 1)$$

$$(1, 0)$$

$$(1, -1)$$

$$[\Pi_a] =$$

$$[\Pi_a^1]$$

$$\otimes$$

$$[\Pi_a^b]$$

$$\otimes$$

$$[\Pi_a^c]$$

$$[\Pi_a^i] = n_a^i [a_i] + m_a^i [b_i]$$

$$[N_a, n_a^i, m_a^i] \quad [N_b, n_b^i, m_b^i]$$

homology class
of 3-cycles

Intersection number: $I_{ab} = [\Pi_a] \circ [\Pi_b] = \prod_{i=1}^3 (n_a^i, m_b^i - n_b^i, m_a^i)$

Global Consistency Conditions

Cancellation of Ramond-Ramond (RR) Tadpoles

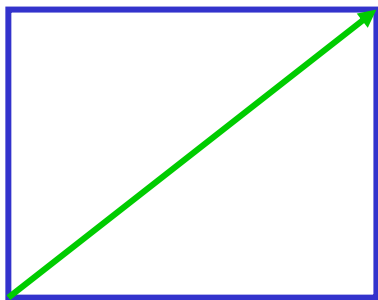
Blumenhagen, Görlich, Körs & Lüst '00

D6-brane – source for $C(7)$

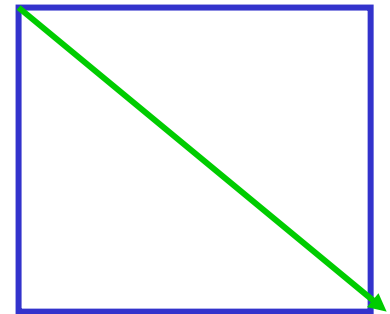
eq. for $C(7)$ Gauss law for D6-charge conservation

$$\mathbf{N}_a \quad [\Pi_a] \quad = \quad 0$$

Impossible to satisfy of CY spaces (‘total’ tension~charge=0)



..



Global Consistency Conditions

Cancellation of Ramond-Ramond (RR) Tadpoles

Blumenhagen, Görlich, Körs & Lüst '00

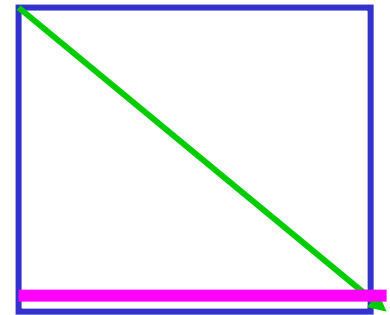
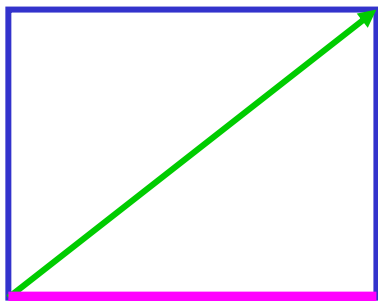
D6-brane – source for $C(7)$

eq. for $C(7)$ Gauss law for D6-charge conservation

$$\mathbf{N}_a \quad [\Pi_a] \quad = \quad 0$$

Impossible to satisfy of CY spaces (‘total’ tension = charge = 0)

Orientifold plane - fixed planes w/ negative RR charge



Global Consistency Conditions

Cancellation of Ramond-Ramond (RR) Tadpoles

Blumenhagen, Görlich, Körs & Lüst '00

D6-brane – source for $C(7)$ - RR potential

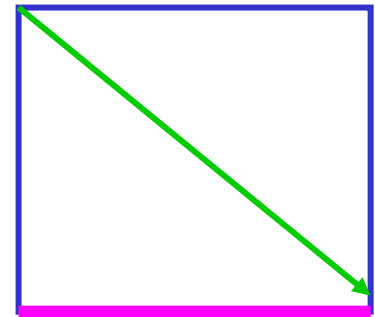
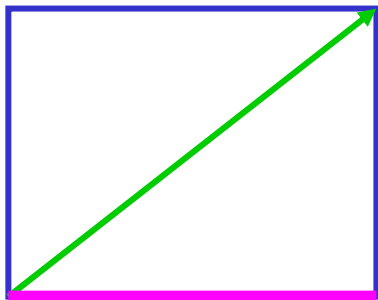
eq. for $C(7)$ Gauss law for D6-charge conservation

$$\mathbf{N}_a \left([\Pi_a] + [\Pi_a'] \right) = -4 [\Pi_{O6}] *$$

* Constraints on wrapping numbers

Impossible to satisfy of CY spaces (‘total’ tension = charge = 0)

Orientifold plane - fixed planes w/ negative D6- charge



Global consistency conditions
for toroidal/orbifold compactifications

$$\sum_a N_a n_a^1 n_a^2 n_a^3 = 16$$

$$\sum_a N_a n_a^1 m_a^2 m_a^3 = 16$$

$$\sum_a N_a m_a^1 n_a^2 m_a^3 = 16$$

$$\sum_a N_a m_a^1 m_a^2 n_a^3 = 16$$

Spectrum on toroidal orientifolds

Sector	Representation
$ab + ba$	$I_{ab} (\square_a, \bar{\square}_b)$ fermions
$ab' + b'a$	$I_{ab'} (\square_a, \square_b)$ fermions
$aa' + a'a$	$\frac{1}{2}(I_{aa'} - \frac{1}{2}I_{a,O}) \square\square$ fermions $\frac{1}{2}(I_{aa'} + \frac{1}{2}I_{a,O}) \begin{array}{ c } \hline \square \\ \hline \end{array}$ fermions

Non-Supersymmetric Standard-like Models (infinitely many)

Blumenhagen, Gorlich, Kors & Lust '00-01

Aldazabal, Franco, Ibanez, Rabadan & Uranga '00-'01

·
·
·

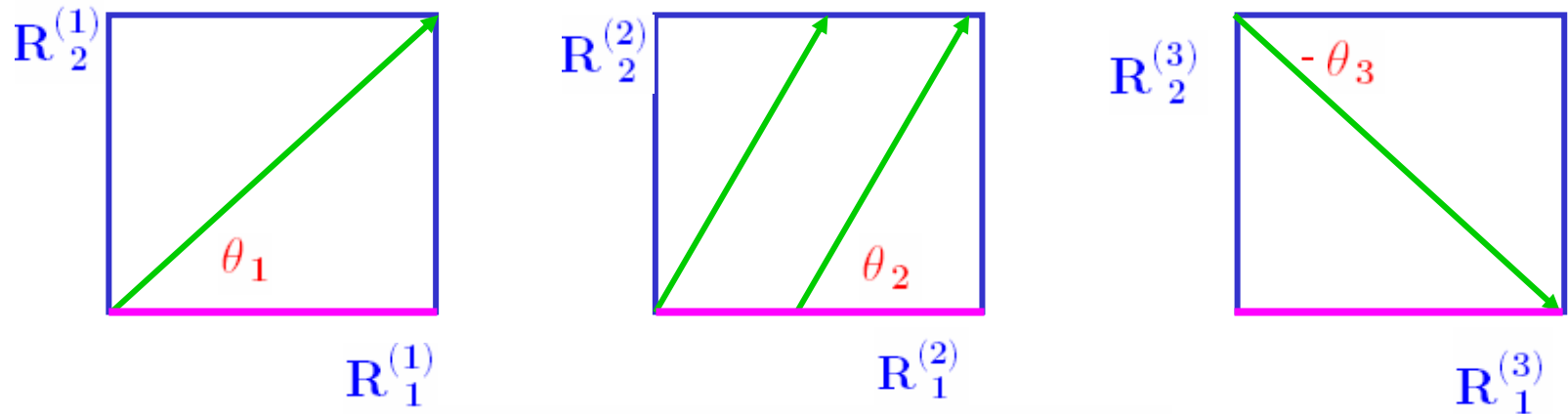
$M_{\text{string}} \sim M_{\text{planck}}$ large NS-NS tadpole
large radiative corrections



Supersymmetric Standard-like Models (constrained)

w/ G. Shiu & A. Uranga '01

Supersymmetry (toroidal example)



$$\theta_1 + \theta_2 + \theta_3 = 0$$

$$\arctan\left(\frac{m_1}{n_1}\chi_1\right) + \arctan\left(\frac{m_1}{n_1}\chi_1\right) + \arctan\left(\frac{m_1}{n_1}\chi_1\right) = 0$$

Constraints on complex structure moduli- $U_i \sim \chi_i = \frac{R_2^{(i)}}{R_1^{(i)}}$

$$\{\theta_i^a\} \neq 0 \quad U(N_a)$$

$$\{\theta_i^a\} = 0 \quad Sp(N_a)$$

Original Model ($Z_2 \times Z_2$ orientifold)

SM \times **U(1)**' \times **U(1)**'' \times **Sp(2)** \times **Sp(2)** \times **Sp(4)**

~ electroweak scale

'' Hidden Sector''

+ 3-families

beta-functions $\beta < 0$

- 12 pairs of Higgs doublets

infrared strong dynamics:

- chiral exotics

gaugino condensation:

(SM branes intersect w/hidden sector)

SUSY breaking, $\{S, U_i\}$ - moduli stabilisation

w/P. Langacker and J. Wang '03

-3chiral superfields on each set of D-branes-

-brane moduli (due to non-rigid cycles)

[3-adjoints for U(N); 3-antisymmetric rep. for Sp(N)]

'' a blessing''

and

'' a curse''



Brane splitting-

Flat directions in moduli space

Gauge symmetry breaking

Further Developments

(i) Systematic Construction - $Z_2 \times Z_2$ orientifolds:

(a) More Standard-like Models (4)

SM \times $U(1)_{B-L-T_{3R}}$ \times $U(1)'$ \times “Hidden Sector”

Fewer exotics, 8-pairs of Higgs doublets

w/I. Papadimitriou'03

(b) Systematic search for **left-right symmetric models** w/realistic features (11)

Only SM at electroweak scale; 2 models w/ only 2-Higgs doublets;

2-models with $g_{2L}=g_{2R}$;

w/T. Li and T. Liu hep-th/0403061

(c) Standard-like Models w/ **electroweak $Sp(2f)_L \times Sp(2f)_R$ sector** (3)

Splitting of branes parallel w/ O_6 planes;

$f=4$ -family model w/no chiral exotics, $g_{2L}=g_{2R}$

w/P. Langacker, T. Li & T.Liu hep-th/0407178

(ii) Other orientifolds

(a) Z_4 -orientifold (1) - brane recombination Blumenhagen, Gorlich & Ott'03

(b) $Z_4 \times Z_2$ -orientifold (1) - brane recombination Honecker'03

(c) Z_6 -orientifold - just SM (1)-Yukawa couplings (?) Honecker & Ott '04

Further Developments

(i) Systematic Construction - $Z_2 \times Z_2$ orientifolds:

(a) More Standard-like Models (4)

SM \times $U(1)_{B-L-T_{3R}}$ \times $U(1)'$ \times “Hidden Sector”

Fewer exotics, 8-pairs of Higgs doublets

w/I. Papadimitriou'03

(b) Systematic search for **left-right symmetric models** w/realistic features (11)

Only SM at electroweak scale; 2 models w/ only 2-Higgs doublets;

2-models with $g_{2L}=g_{2R}$;

w/T. Li and T. Liu hep-th/0403061

(c) Standard-like Models w/ **electro-weak $Sp(2f)_L \times Sp(2f)_R$ sector** (3)

Splitting of branes parallel w/ O planes;

$f=4$ -family model w/no chiral exotics, $g_{2L}=g_{2R}$

w/P. Langacker, T. Li & T. Liu hep-th/0407178

(ii) Other orientifolds

(a) Z_4 -orientifold (1) - brane recombination Blumenhagen, Gorlich & Ott'03

(b) $Z_4 \times Z_2$ -orientifold (1)- brane recombination Honecker'03

(c) Z_6 -orientifold (1) -Yukawa couplings (?) Honecker & Ott '04

Building blocks of Pati-Salam Models

$$\begin{array}{l}
 \text{U}(4)_C \times \text{U}(2)_L \times \text{U}(2)_R \times \underbrace{\text{Sp}(2n_1) \times \text{Sp}(2n_2) \times \dots}_{\text{at least two confining group factors}} \\
 3 \quad (4, 2, 1) \\
 3 \quad (4, 1, 2) \quad \text{(SUSY breaking, moduli stabilisation)}
 \end{array}$$

Symmetry breaking:

$$\text{SU}(4)_C \times \text{SU}(2)_L \times \text{SU}(2)_R \times [\text{U}(1)_C \times \text{U}(1)_L \times \text{U}(1)_R]$$

↓ brane splitting

↓ brane (anomalous, $M_{Z'} \sim M_{\text{string}}$) splitting

$$\text{SU}(3)_C \times \text{U}(1)_{B-L} \quad \text{U}(1)_{T_{3R}}$$

vector pair $D_R = (4, 1, 2)$ D- and F-flat Higgsing
 $D_L = (4, 2, 1)$ (brane recombination)

$$\text{SU}(3)_C \times \text{SU}(2)_L \times \text{U}(1)_Y$$

Just Standard Model!

Brane Splitting || w/orientifold planes

[f-family SM from $Sp(2f)_L \times Sp(2f)_R$ electroweak sector]

Splitting of branes in
one, two, three
toroidal direction



VEV's to
one, two, three
(antisymm. rep.) moduli

Typical: $Sp(4k) \xrightarrow{\text{one}} Sp(2k) \times Sp(2k)$
 $\xrightarrow{\text{two}} Sp(2k)$
 $\xrightarrow{\text{three}} U(k),$

[$Sp(4k+2) \rightarrow Sp(2) \times Sp(4k)$
not suitable, e.g., 3-families]

$f=4:$	$U(4)_C \times Sp(8)_L \times Sp(8)_R$	\longrightarrow	$U(4)_C \times U(2)_L \times U(2)_R$
1	$(4, 8, 1)$	\longrightarrow	4 $(4, 2, 1)$
1	$(\bar{4}, 1, 8)$	\longrightarrow	4 $(\bar{4}, 1, 2)$
	one-family		four-families
$f=2:$	$U(4)_C \times Sp(4)_L \times Sp(4)_R$	\longrightarrow	$U(4)_C \times Sp(2)_L \times Sp(2)_R$
1	$(4, 4, 1)$	\longrightarrow	2 $(4, 2, 1)$
1	$(\bar{4}, 1, 4)$	\longrightarrow	2 $(\bar{4}, 1, 2)$
	one-family		two-families

Chirality change due to splitting from orientifold singularity

Four-family Standard Model

Table 2: D6-brane configurations and intersection numbers for the four-family Standard-like model. In the table, χ_i is the complex modulus for the i -th torus, and β_i^g is the beta function for the i -th Sp group from the i -th stack of branes.

I	$[U(4)_C \times Sp(8)_L \times Sp(8)_R]_{observed} \times [U(4) \times Sp(8) \times Sp(8)]_{hidden}$									
stack	N	$(n^1, l^1) \times (n^2, l^2) \times (n^3, l^3)$	$n_{\square\square}$	n_{\square}	b	c	d	d'	1	2
a	8	$(1, 0) \times (1, 1) \times (1, -1)$	0	0	1	-1	0	0	0	0
b	8	$(0, 1) \times (1, 0) \times (0, -1)$	0	0	-	0	0	0	0	0
c	8	$(0, 1) \times (0, -1) \times (1, 0)$	0	0	-	-	0	0	0	0
d	8	$(0, 1) \times (1, -1) \times (1, -1)$	0	0	-	-	-	0	-1	1
1	8	$(1, 0) \times (1, 0) \times (1, 0)$	$\chi_2 = \chi_3 = 1$ $\beta_1^g = \beta_2^g = -4$							
2	8	$(1, 0) \times (0, -1) \times (0, 1)$								

no inter-
section w/
hidden sector
**no chiral
exotics!**

$Sp(8)_L \times Sp(8)_R$ 1-Higgs (8,8), one-family confining ``hidden sector
 \downarrow brane splitting \downarrow brane splitting \downarrow
 $U(2)_L \times U(2)_R$ 16-Higgs (2,2), four-families
 \downarrow
 $U(1)_L$ broken at electroweak scale

Three-family SM model w/Sp (2)_L x Sp(2)_R directly (Z₂ x Z₂ orientifold)

III	$[U(4)_C \times SU(2)_L \times SU(2)_R]_{observable} \times [U(2)^* \times Sp(8)]_{hidden}$								
stack	N	$(n^1, l^1) \times (n^2, l^2) \times (n^3, l^3)$	$n_{\square\square}$	n_{\square}	b	c	d	d'	2
a	8	$(1, 0) \times (1, 3) \times (1, -3)$	0	0	3	-3	0	0	0
b	2	$(0, 1) \times (1, 0) \times (0, -2)$	0	0	-	0	-6	6	0
c	2	$(0, 1) \times (0, -1) \times (2, 0)$	0	0	-	-	-6	6	0
d	4	$(2, -1) \times (1, 3) \times (1, 3)$	$\chi_1 = 24\chi_3 / (4 - 9\chi_3^2)$						
2	8	$(1, 0) \times (0, -1) \times (0, 2)$							

non-zero Intersections w/hidden sector chiral exotics

wrapping nos. of SM-proposed for toroidal orientifold (did not cancel RR-tadpoles)

Cremades, Ibanez & Marchesano'03

Z₂ x Z₂ orientifold-allows for cancellation of RR-tadpoles

``hidden sector'' unitary symmetry- necessary for RR-tadpole cancellation

*U(2)-no global discrete Witten anomaly (original U(1)-Witten anomaly)

w/ Langacker, Li & Liu hep-th/0407178

[one torus tilted: 2 Higgs (2,2), Yukawa couplings give mass to 2nd and 3rd family]

Moduli Stabilization

I. ``Hidden sector'' strong dynamics ($\beta < 0$)- gaugino condensation

$$f_a = n_a^1 n_a^2 n_a^3 S - m_a^1 n_a^2 n_a^3 U_1 - n_a^1 m_a^2 n_a^3 U_2 - n_a^1 n_a^2 m_a^3 U_3$$

↓ gauge kin. function dilaton complex structure moduli

Example of S, U_i-fixed, SUSY broken

w/Langacker&Wang'03

II. Supergravity Fluxes:

Type IIA- less understood; study of superpersymmetry conditions

examples of nearly Kahler spaces and **chiral non-Abelian D-brane sector (no time!)**

w/K. Behrndt hep-th/0308045, 0403049, 0407163

Type IIB- examples of SM with fluxes

Marchesano&Shiu hep-th/0408058,0409132

w/T.Liu/hep-th/0409032, w/T.Li&T.Liu, hep-th/0501041

Supersymmetry conditions for general fluxes (w/components in the internal space & warped metric Ansatz):

$$ds_{10}^2 = \exp(A(y)) \left[ds_4^2 + \exp(B(y)) (h_{mn} dy^m dy^n) \right]$$

AdS₄ ↓

↓

(i) **SU(3) structures: internal space nearly Kahler**
unique solution w/ all fluxes turned on; warp factor and dilaton fixed;

Example: coset space $[SU(3)]^3/SU(2) \sim S^3 \times S^3$ allows for **non-Abelian chiral**
 intersecting D6-brane sector

(within M-theory c.f., Acharya, Denef, Hofman & Lambert '03)

H₃-homology non-trivial;

{(1,0); (0,1); (-1,-1)}-Total homology 0!

Supersymmetric calibrated 3-cycles wrapped by D6-branes **without orientifold planes!**

& orbifolding of $S^3 \times S^3$

$$\begin{array}{l}
 U(N) \times U(N) \times U(N) \\
 \Psi_{1\sim} (N, \bar{N}, 1) \\
 \Psi_{2\sim} (\bar{N}, 1, N) \\
 \Psi_{3\sim} (1, N, \bar{N})
 \end{array}$$

Supersymmetry conditions for general fluxes (w/components in the internal space & Freund-Rubin Ansatz & warped metric Ansatz):

$$ds_{10}^2 = \exp(A(y)) \left[ds_4^2 + \exp(B(y)) (h_{mn} dy^m dy^n) \right]$$

↓
AdS4

↓

(i) SU(3) structures: internal space nearly Kahler
unique solution w/ all fluxes turned on; warp factor and dilaton fixed

Example: coset space **S3 x S3- non-Abelian chiral intersecting D6-brane sector**
(within M-theory c.f., Acharya, Denef, Hofman & Lambert '03)

Minkowski

(ii) SU(2) structures: example of conformally flat internal space

$A+iB=F(u+iv)$; $\Phi(u,v)$ & explicit fluxes; (u,v) –coordinates of an internal two-torus

Difficulties in accommodating orientifold/orbifold projection for D-brane sector

Type IIB theory

&

Fluxes

[D1,D3,D5,D7-branes]

[C(2n) – RR potentials]

Fluxes better understood:

supersymmetry conditions,
back-reaction due to fluxes,
potential for moduli etc.

Gukov, Vafa & Witten '99

Sethi et al.

Giddings, Kachru & Polchinski '01

Kachru, Kallosh, Linde & Trivedi '03

rich phenomenological studies;
cosmology; landscape etc.

E.g.: **specific flux:**

$$G_3 = F_3 - \tau H_3$$

RR-3form dilaton/axion NS-NS-3form

Supersymmetry:

self-dual, primitive (2,1) form

Four-dim **superpotential:**

$$W \sim \int \Omega \wedge G_{(3)} = f^I p_I$$

complex structure moduli

Type IIA: Intersecting D6-branes

$$\downarrow \text{T-duality } (R_1^{(i)} \rightarrow \frac{\alpha'}{R_1^{(i)}})$$

Type IIB: Magnetized D9-branes

Cascales&Uranga'03

Blumenhagen,Lust&Taylor'03

$$\{ N_a, (n_a^i, m_a^i) \}$$

$$m_a^i \frac{1}{2\pi} \int_{T^2_i} F_a^i = n_a^i$$

U(1)-D-brane magnetic field

$$Q3_a = N_a n_a^1 n_a^2 n_a^3,$$

$$(Q7_i)_a = N_a n_a^i m_a^j m_a^k, \quad i \neq j \neq k$$

Flux: $G_3 = F_3 - \tau H_3$

$$N_{\text{flux}} = \frac{1}{(4\pi^2 \alpha')^2} \frac{i}{2\tau_I} \int_{X_6} G_3 \wedge \overline{G}_3$$

Contributes to QD3 charge

Quantisation conditions: $N_{\text{flux}} = n_f N_o \quad n_f \in \mathbf{Z} \quad N_o = 64$

Specific to $Z_2 \times Z_2$ orbifold

Global consistency conditions

For toroidal/orbifold compactifications

$$\sum_a N_a n_a^1 n_a^2 n_a^3 = 16$$

$$\sum_a N_a n_a^1 m_a^2 m_a^3 = 16$$

$$\sum_a N_a m_a^1 n_a^2 m_a^3 = 16$$

$$\sum_a N_a m_a^1 m_a^2 n_a^3 = 16$$

D-branes & Fluxes (Type IIB)

Global consistency conditions
for toroidal/orbifold compactifications

$$Q_{D3} \quad \sum_a N_a n_a^1 n_a^2 n_a^3 = 16 \quad -N_{\text{flux}}$$

$$Q_{D7_1} \quad \sum_a N_a n_a^1 m_a^2 m_a^3 = 16$$

$$Q_{D7_2} \quad \sum_a N_a m_a^1 n_a^2 m_a^3 = 16$$

$$Q_{D7_3} \quad \sum_a N_a m_a^1 m_a^2 n_a^3 = 16$$

$$N_{\text{flux}} = N_{\text{flux}}$$

More Constrained !

Three-family SM model w/Sp(2)_L x Sp(2)_R directly (Z₂ x Z₂ orientifold)

III	[U(4) _C × SU(2) _L × SU(2) _R] _{observable} × [U(2) [*] × Sp(8)] _{hidden}								
stack	N	(n ¹ , l ¹) × (n ² , l ²) × (n ³ , l ³)	n _{□□}	n _□	b	c	d	d'	2
a	8	(1, 0) × (1, 3) × (1, -3)	0	0	3	-3	0	0	0
b	2	(0, 1) × (1, 0) × (0, -2)	0	0	-	0	-6	6	0
c	2	(0, 1) × (0, -1) × (2, 0)	0	0	-	-	-6	6	0
d	4	(2, -1) × (1, 3) × (1, 3)	$\chi_1 = 24\chi_3 / (4 - 9\chi_3^2)$ $\chi_2 = \frac{1}{2}\chi_3, \beta_2^g = -5$						
2	8	(1, 0) × (0, -1) × (0, 2)							

Non-zero
Intersections
w/hidden sector-
Chiral exotics

wrapping nos. of SM-proposed for toroidal orientifold (did not cancel RR-tadpoles)

Cremades, Ibanez & Marchesano'03

Z₂ x Z₂ orientifold-allows for cancellation of RR-tadpoles

"hidden sector" unitary symmetry- necessary for RR-tadpole cancellation

*U(2)-D9-brane w/ negative D3-charge contribution

w/ Langacker, Li & Liu hep-th/0407178

Three-family SM model w/Sp(2)L x Sp(2)R directly (Z2xZ2orientifold) & Fluxes

III	$[U(4)_C \times SU(2)_L \times SU(2)_R]_{observable} \times [U(2)^* \times Sp(8)]_{hidden}$								
stack	N	$(n^1, l^1) \times (n^2, l^2) \times (n^3, l^3)$	$n_{\square\square}$	n_{\square}	b	c	d	d'	2
a	8	$(1, 0) \times (1, 3) \times (1, -3)$	0	0	3	-3	0	0	0
b	2	$(0, 1) \times (1, 0) \times (0, -2)$	0	0	-	0	-6	6	0
c	2	$(0, 1) \times (0, -1) \times (2, 0)$	0	0	-	-	-6	6	0
d	4	$(2, -1) \times (1, 3) \times (1, 3)$	$\chi_1 = 24\chi_3 / (4 - 9\chi_3^2)$						
2	8	$(1, 0) \times (0, -1) \times (0, 2)$							

Non-zero Intersections w/hidden sector Chiral exotics

wrapping nos. of SM-proposed for toroidal orientifold (did not cancel RR-tadpoles)

Cremades, Ibanez & Marchesano'03

Z2 x Z2 orientifold-allows for cancellation of RR-tadpoles

``hidden sector'' unitary symmetry- necessary for RR-tadpole cancellation

*U(2)-D9-brane w/ negative D3-charge contribution

w/ Langacker, Li & Liu hep-th/0407178

Marchesano & Shiu, hep-th/0408058,0409132

U(1) x U(1) nf=1 flux units

[no untilted tori- 1 Higgs (2,2); Yukawa couplings give mass to 3rd family only; chiral exotics]

f-family Standard Model w/Sp(2f)_L x Sp(2f)_R & n_f-units of flux

w/T. Liu hep-th/0409032

TABLE VII: D-brane configurations and intersection numbers for the consistent f -family Standard-like Models with n_f -units of quantized flux. χ_i is the Kähler modulus for the i^{th} two-torus, β_j^g is the beta function for the Sp group from the j^{th} stack of branes. The allowed models have $f = 2, 4$ with $(n_f)_{\text{max}} = 2, 1$, respectively.

[U(4) _C × Sp(2f) _L × Sp(2f) _R] _o × [U(2) × Sp(8(4 - $\frac{f}{2}$) ² + 16 - 32n _f)] _h									
j	N	(n ¹ , m ¹)(n ² , m ²)(n ³ , m ³)	n \square	n \square	b	c	d	d'	1
a	8	(1,0)(1,1)(1, -1)	0	0	1	-1	(4 - $\frac{f}{2}$) ² - 1	-(4 - $\frac{f}{2}$) ² + 1	0
b	8	(0,1)(1,0)(0, -1)	0	0	-	0	2(4 - $\frac{f}{2}$)	-2(4 - $\frac{f}{2}$)	0
c	8	(0,1)(0, -1)(1,0)	0	0	-	-	2(4 - $\frac{f}{2}$)	-2(4 - $\frac{f}{2}$)	0
d	4	(-2, -1)(4 - $\frac{f}{2}$, 1)(4 - $\frac{f}{2}$, 1)	$\chi_1 = (16 - 2f)\chi_3 / (\chi_3^2 - (4 - \frac{f}{2})^2)$						
1	8(4 - $\frac{f}{2}$) ² + 16 - 32n _f	(1,0)(1,0)(1,0)	$\chi_2 = \chi_3, \beta_1^g = -5$						

intersections
w/hidden sector
chiral exotics

n_f=1, f=4: Sp(8)_L x Sp(8)_R

brane splitting →

U(2)_L x U(2)_R

n_f=2, f=2: Sp(4)_L x Sp(4)_R

brane splitting →

Sp(2)_L x Sp(2)_R

* U(2) w/ specific wrapping nos to cancel flux contrib. to Q_{D3} charge

A number of models have all toroidal Kahler moduli fixed due to SUSY constraints OR in some cases the "hidden sector" has confining Sp-type gauge symmetry (negative β function), leading to gaugino condensation:

$$W_{eff} = \frac{\beta_1^g \Lambda^3}{32e\pi^2} \exp\left(\frac{8\pi^2}{\beta_1^g} f_W\left(\frac{V_6}{g_s}\right)\right) + W_o$$

Kahler modulus flux contrib. (fixed complex structure moduli)

Kahler modulus - stabilised & SUSY restored (a la KKLT), however since $n_f=1,2,3$
 $W_o \sim (M_{string})^3$ and thus the volume size- string size
 The other two toroidal Kahler moduli - fixed by SUSY conditions for D-branes



An explicit chiral SM-like construction w/all toroidal moduli stabilised.

{However, twisted closed sector moduli not stabilised.
 D-brane sector moduli: brane splitting moduli (non-chiral)-massive due to flux back-reaction; brane recombination moduli could combine w/ Kahler moduli to form D- and F-flat directions with Kahler moduli-problem! }

SUSY breaking  **anti D3-branes** (a la KKLT)

New Sets of Flux Models: D9-branes w/ negative D3 charge part of the Standard Model

Gauge symmetry: $U(4)_C \times U(2)_L \times U(2)_R \times Sp(2N_1) \times Sp(2N_2) \dots$
 or $(Sp(2)_L)$ or $(Sp(2)_R)$ $\underbrace{\hspace{10em}}$ ``Hidden sector''

SM sector contains D-branes with negative D3-charge

New models (on the order of 20) of three- and four-family Standard Models with up to 3-units of quantized flux.

Three -family SM with 3- units of flux (supersymmetric)

Table 5: D-brane configurations and intersection numbers for $Model - T_3 - 1$.

$Model - T_3 - 1$	$[U(4)_C \times U(2)_L \times U(2)_R]_{Observable}$								
j	N	$(n^1, m^1)(n^2, m^2)(n^3, m^3)$	$n_{\square\square}$	n_{\square}	b	b'	c	c'	Kähler moduli
a	8	(1, 0)(1, 1)(1, -1)	0	0	-3	1	12	-10	$\chi_3 = \chi_2 = 2\chi_1$
b	4	(1, 1)(2, -1)(1, 0)	-2	2	-	-	6	6	$\chi_3 = 2\sqrt{10}$
c	4	(-2, -1)(4, 1)(3, 1)	-6	-106	-	-	-	-	

Three -family SM with 2- units of flux

Table 6: D-brane configurations and intersection numbers for $Model - T_2 - 1$.

$Model - T_2 - 1$	$[U(4)_C \times U(2)_L \times U(2)_R]_{Observable} \times [Sp(12 - 4n_f)]_{Hidden}$									
j	N	$(n^1, m^1)(n^2, m^2)(n^3, m^3)$	$n_{\square\square}$	n_{\square}	b	b'	c	c'		
a	8	(1, 0)(1, 1)(1, -1)	0	0	-3	1	8	-8		
b	4	(2, 1)(2, -1)(1, 0)	0	0	-	-	0	4		
c	4	(-2, -1)(3, 1)(3, 1)	-44	-64	-	-	-	-		
$(D7)_2$	4	(0, 1)(1, 0)(0, -1)	$\chi_3 = \chi_2 = \chi_1 = \sqrt{21}$							

Three -family SM with 1- units of flux

Table 7: D-brane configurations and intersection numbers for $Model - T_1 - 1$.

$Model - T_1 - 1$	$[U(4)_C \times Sp(2)_L \times U(2)_R]_{Observable} \times [Sp(8)]_{Hidden}$								
j	N	$(n^1, m^1)(n^2, m^2)(n^3, m^3)$	$n_{\square\square}$	n_{\square}	b	c	c'		
a	8	(1, 0)(3, 1)(3, -1)	0	0	-3	3	0		
b	2	(0, 1)(0, -1)(2, 0)	0	0	-	16	-		
c	4	(-2, -1)(4, 1)(3, 1)	-6	-106	-	-	-		
D3	8	(1, 0)(1, 0)(1, 0)	$\chi_2 = \chi_3, \frac{12}{\chi_2^2} + \frac{14}{\chi_1\chi_2}$						

More three-family SM's with 1-unit of flux

Table 8: D-brane configurations and intersection numbers for *Model* – $T_1 - 2$.

<i>Model</i> – $T_1 - 2$		$[U(4)_C \times U(2)_L \times U(2)_R]_{Observable} \times [Sp(8) \times Sp(4)]_{Hidden}$						
j	N	$(n^1, m^1)(n^2, m^2)(n^3, m^3)$	n_{\square}	n_{\square}	b	b'	c	c'
<i>a</i>	8	(1,0)(1,1)(1,-1)	0	0	-3	1	4	-6
<i>b</i>	4	(2,1)(2,-1)(1,0)	0	0	-	-	0	0
<i>c</i>	4	(-2,-1)(2,1)(3,1)	-18	-78	-	-	-	-
<i>D3</i>	8	(1,0)(1,0)(1,0)	$\chi_3 = \chi_2 = \chi_1 = 4$					
<i>(D7)₂</i>	8	(0,1)(1,0)(0,-1)						

Table 9: D-brane configurations and intersection numbers for *Model* – $T_1 - 3$.

<i>Model</i> – $T_1 - 3$		$[U(4)_C \times U(2)_L \times Sp(4)_R]_{Observable} \times [Sp(4)]_{Hidden}$						
j	N	$(n^1, m^1)(n^2, m^2)(n^3, m^3)$	n_{\square}	n_{\square}	b	b'	c	
<i>a</i>	8	(-1,-1)(2,1)(2,1)	-2	-30	3	-5	-4	
<i>b</i>	4	(1,0)(3,1)(1,-1)	4	-4	-	-	0	
<i>c</i>	4	(1,0)(0,1)(0,-1)	0	0	-	-	-	
<i>D3</i>	8	(1,0)(1,0)(1,0)	$3\chi_3 = \chi_2, \frac{12}{\chi_2^2} + \frac{8}{\chi_1\chi_2} = 1$					

Four -family SM with 3-units of flux (supersymmetric)

Table 10: D-brane configurations and intersection numbers for *Model – F₃ – 1*.

<i>Model – F₃ – 1</i>	$[U(4)_C \times U(2)_R \times Sp(4)_L]_{Observable}$							
j	N	$(n^1, m^1)(n^2, m^2)(n^3, m^3)$	$n_{\square\square}$	n_{\square}	b	c	c'	Kähler moduli
<i>a</i>	8	(1, 0)(2, 1)(1, -1)	2	-2	-2	8	-12	$\chi_2 = 2\chi_3$
<i>b</i>	4	(0, 1)(0, -1)(1, 0)	0	0	-	8	-	$\frac{24}{\chi_2^2} + \frac{20}{\chi_1\chi_2} = 1$
<i>c</i>	4	(-2, -1)(4, 1)(3, 1)	-6	-106	-	-	-	

Four-family SM's with 2-units of flux

Table 11: D-brane configurations and intersection numbers for $Model - F_2 - 1$.

$Model - F_2 - 1$		$[U(4)_C \times U(2)_L \times U(2)_R]_{Observable} \times [Sp(4)]_{Hidden}$
j	N	$(n^1, m^1)(n^2, m^2)(n^3, m^3)$
		$n_{\square\square}$ n_{\square} b b' c c'
a	8	(1,0)(2,1)(1,-1)
b	4	(1,1)(2,-1)(1,0)
c	4	(-2,-1)(3,1)(3,1)
$(D7)_2$	4	(0,1)(1,0)(0,-1)
		$\chi_2 = 2\chi_3 = 2\chi_1 = \frac{3}{2}\sqrt{6}$

Table 12: D-brane configurations and intersection numbers for $Model - F_2 - 2$.

$Model - F_2 - 2$		$[U(4)_C \times Sp(4)_L \times U(2)_R]_{Observable} \times [Sp(8) \times Sp(4)]_{Hidden}$
j	N	$(n^1, m^1)(n^2, m^2)(n^3, m^3)$
		$n_{\square\square}$ n_{\square} b c c'
a	8	(1,0)(2,1)(1,-1)
b	4	(0,1)(0,-1)(1,0)
c	4	(-2,-1)(3,1)(3,1)
D3	8	(1,0)(1,0)(1,0)
$(D7)_2$	4	(0,1)(1,0)(0,-1)
		$2\chi_3 = \chi_2$ $\frac{18}{\chi_3^2} + \frac{18}{\chi_1\chi_2} = 1$

Table 13: D-brane configurations and intersection numbers for $Model - F_2 - 3$.

$Model - F_2 - 3$		$[U(4)_C \times U(2)_L \times U(2)_R]_{Observable} \times [Sp(4)]_{Hidden}$
j	N	$(n^1, m^1)(n^2, m^2)(n^3, m^3)$
		$n_{\square\square}$ n_{\square} b b' c c'
a	8	(1,0)(2,1)(1,-1)
b	4	(2,1)(1,-1)(1,0)
c	4	(-2,-1)(3,1)(3,1)
$(D7)_2$	4	(0,1)(1,0)(0,-1)
		$\chi_2 = 2\chi_3 = \frac{1}{2}\chi_1 = 3\sqrt{3}$

Four- family SM's with 1-unit of flux

Table 14: D-brane configurations and intersection numbers for *Model* – $F_1 - 1$.

<i>Model</i> – $F_1 - 1$		$[U(4)_C \times U(2)_L \times Sp(8)_R]_{Observable} \times [Sp(8)]_{Hidden}$					
j	N	$(n^1, m^1)(n^2, m^2)(n^3, m^3)$	$n_{\square\square}$	n_{\square}	b	b'	c
a	8	(1,0)(1,1)(2, -1)	-2	2	4	0	-1
b	4	(-2, -1)(2, 1)(2, 1)	-10	-54	-	-	-4
c	8	(0,1)(0, -1)(1,0)	0	0	-	-	-
$(D7)_2$	8	(0,1)(1,0)(0, -1)	$\chi_3 = 2\chi_2, \frac{2}{\chi_2^2} + \frac{6}{\chi_1\chi_2} = 1$				

Table 15: D-brane configurations and intersection numbers for *Model* – $F_1 - 2$.

<i>Model</i> – $F_1 - 2$		$[U(4)_C \times U(2)_L \times U(2)_R]_{Observable} \times [Sp(12) \times Sp(4)]_{Hidden}$						
j	N	$(n^1, m^1)(n^2, m^2)(n^3, m^3)$	$n_{\square\square}$	n_{\square}	b	b'	c	c'
a	8	(1,0)(1,1)(1, -1)	0	0	-4	2	4	-6
b	4	(2,1)(3, -1)(1,0)	-2	2	-	-	0	-4
c	4	(-2, -1)(2, 1)(3, 1)	-18	-78	-	-	-	-
$(D7)_2$	8	(0,1)(1,0)(0, -1)	$\chi_3 = 2\chi_2 = 4\chi_1 = 2\sqrt{19}$					

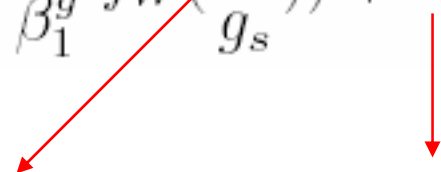
Table 16: D-brane configurations and intersection numbers for *Model* – $F_1 - 3$.

<i>Model</i> – $F_1 - 3$		$[Sp(16)_C \times U(2)_L \times U(2)_R]_{observable}$							
j	N	$(n^1, m^1)(n^2, m^2)(n^3, m^3)$	$n_{\square\square}$	n_{\square}	b	b'	c	c'	Kähler moduli
a	16	(1,0)(1,0)(1,0)	0	0	1	-	-1	-	$\chi_1\chi_3 = 6$
b	4	(2, -1)(0, 1)(3, -1)	-10	10	-	-	64	0	$\frac{\chi_1}{\chi^2} + \frac{12}{\chi_1\chi_2} = 1$
c	4	(-2, -1)(4,1)(1,1)	-6	-58	-	-	-	-	

I. Moduli Stabilization: Toroidal simplex structure moduli-fixed by fluxes.

In some cases all toroidal Kahler moduli fixed by SUSY OR

Examples of two Kahler moduli fixed by SUSY & a hidden sector, w/ negative β function, resulting in gaugino condensation and non-perturbative superpotential:

$$W_{eff} = \frac{\beta_1^g \Lambda^3}{32e\pi^2} \exp\left(\frac{8\pi^2}{\beta_1^g} f_W\left(\frac{V_6}{g_s}\right)\right) + W_o$$


third Kahler modulus

flux contrib.(fixed complex structure moduli)

All toroidal Kahler moduli stabilized & SUSY restored

An explicit chiral SM-like construction w/all toroidal moduli stabilized.

II. Further Phenomenology:

w/P. Langacker, T. Li & T. Liu, to appear

(mainly right) chiral exotics w/ Yukawa couplings to SM Higgs sector (M~ TeV);

Higgs sector non-minimal, allowing for quark and lepton masses

III. Analysis of soft SUSY breaking mass terms:

One- and two-units of fluxes (and no hidden sector strong dynamics) break SUSY-

Camara,Ibanez&Uranga, hep-th/0408064; Lust, Reffert&stieberger, hep-th/0410074;

Kane,Kumar,Lykken&Wang, hep-th/0411125;

Flux SM's with Confining Hidden Sector that stabilizes the left-over Kahler modulus

$Model - F_1 - 5$		$[U(4)_C \times Sp(8)_L \times U(2)_R]_{Observable} \times [Sp(4) \times Sp(4)]_{Hidden}$					
j	N	$(n^1, m^1)(n^2, m^2)(n^3, m^3)$	$n_{\square\square}$	$n_{\begin{smallmatrix} \square \\ \square \end{smallmatrix}}$	b	c	c'
a	8	$(1, 0)(1, 1)(1, -1)$	0	0	-1	6	-4
b	8	$(0, 1)(0, -1)(1, 0)$	0	0	-	3	-
c	4	$(-1, -1)(3, 1)(2, 1)$	-4	-44	-	-	-
$(D7)_1$	4	$(1, 0)(0, 1)(0, -1)$	$\chi_2 = \chi_3, \frac{6}{\chi_3^2} + \frac{5}{\chi_1\chi_3} = 1$				
$(D7)_2$	4	$(0, 1)(1, 0)(0, -1)$	$\beta_{(D7)_1}^g = -3(0), \beta_{(D7)_2}^g = -5(-2)$				

Conclusions/Outlook

- (i) Overview/status of supersymmetric intersecting D-brane constructions w/realistic particle physics:
 - (a) Major progress: development of techniques for consistent constructions on toroidal/orbifold orientifolds (geometric): explicit spectrum & couplings (no time!)
 - (b) Sizable nos of semi-realistic models (on the order of 20); within $Z_2 \times Z_2$ orientifolds - systematic search (w/ SM, 3 families) leading to construction of (most) classes of models there. Ready for landscape study (???)
 - (c) ``The devil is in the details!``:
 - chiral exotics (except a 4-family example)
 - realistic Higgs sector and/or Yukawa couplings [geometric w/hierarchy (no time!)]

(ii) Intersecting D-branes and Fluxes

(a) Type IIA: fluxes less explored, but recent progress:
examples of nearly Kahler internal spaces
w/ chiral non-Abelian intersecting D-brane sector

(b) Type IIB: Chiral SM constructions w/fluxes
intersecting D-branes \rightarrow magnetized D-branes
On the order of 20 SM's with 3- and 4-families and
up to 3-units of quantised flux.
Just scratching the surface!

FULLY REALISTIC CONSTRUCTIONS –at least at the level of
spectrum, coupling and all moduli stabilization (???)

TECHNIQUES TO ADDRESS THE LANDSCAPE
OF REALISTIC MODELS (???)