



# Rare B decays at the B Factories

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# Overview

- Motivation
- Semileptonic B Decays
  - Exclusive Decays
    - ❖  $V_{cb}$ ,  $V_{ub}$  and Form Factors
  - Inclusive Decays
    - ❖  $V_{cb}$  &  $V_{ub}$
- Radiative Penguin Decays
  - $b \rightarrow s\gamma$ ,  $b \rightarrow d\gamma$
- Charmless Hadronic B Decays
  - Bounds on  $\Delta S$  and  $\sin 2\beta$  from  $B \rightarrow \eta' K_s$
  - $B^+ \rightarrow K^+ \pi^- \pi^+$
- $B \rightarrow$  Charm Decays via W-exchange and Annihilation
  - $B \rightarrow D_s D_s$
  - $B \rightarrow D_s \phi$
- Conclusions

# CKM matrix and Unitarity Triangle

In the Standard Model, couplings between quarks of different flavour are described by the CKM matrix.

It relates weak to mass eigenstates.

CKM matrix has 4 free parameters:

- 3 Euler angles
- 1 free phase

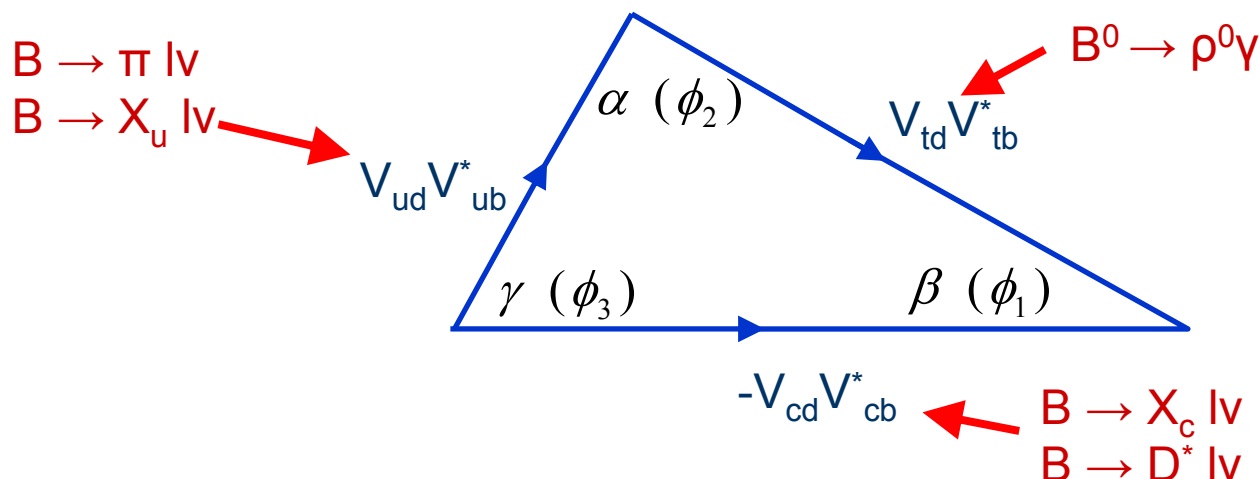
Unitary!

$$V_{\text{CKM}} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

radiative decays

semi-leptonic decays

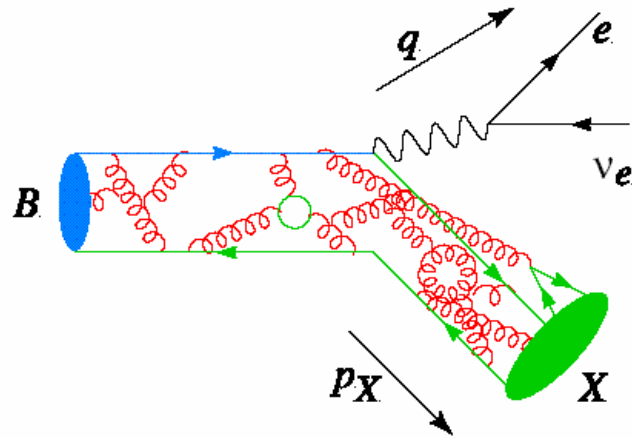
Can be visualised as triangle:



# Semileptonic Decays

## Why semileptonic decays?

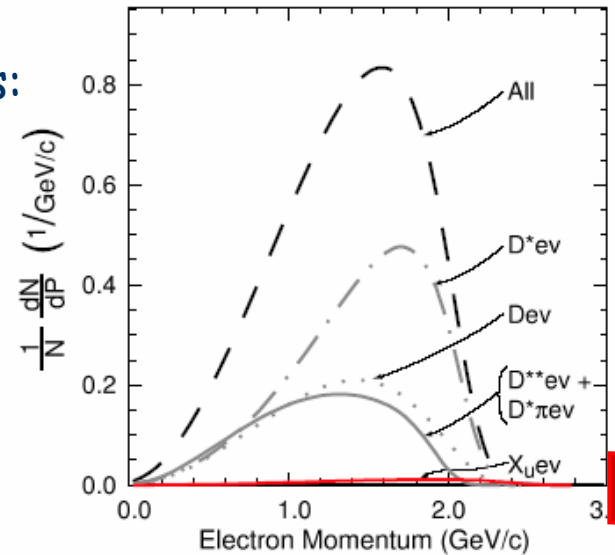
$|V_{ub}|$  and  $|V_{cb}|$  are crucial in testing CKM unitarity and SM mechanism for CP violation



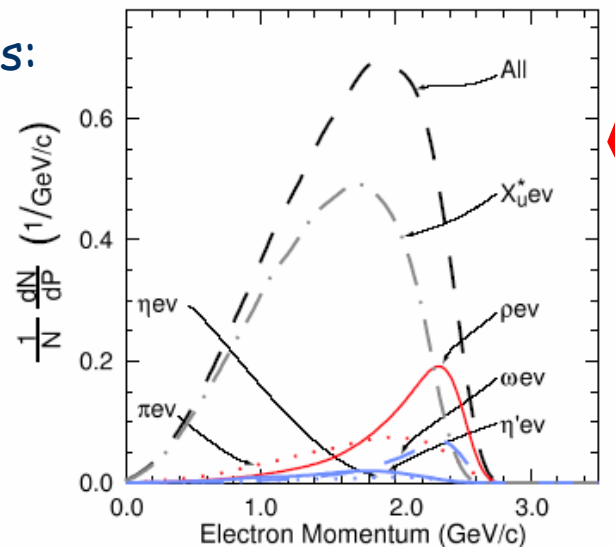
Hadronic and leptonic currents factorise, theoretical uncertainties are under control giving access to  $|V_{ub}|$  and  $|V_{cb}|$

Different uncertainties in inclusive and exclusive decays → study both!

$b \rightarrow c \ell \nu$  transitions:



$b \rightarrow u \ell \nu$  transitions:



# Exclusive $|V_{cb}|$

- In exclusive decays we need formfactors to relate  $B \rightarrow D^* \ell \nu$  decay rate to  $|V_{cb}|$

$$\text{BR}(B \rightarrow D^* \ell \nu) \sim |V_{cb} F_{D^*}(w=1)|^2$$

$w$ :  $D^*$  boost in  $B$  rest frame

- $F(w)$  is calculable at  $w = 1$ , i.e. zero-recoil

- encodes QCD ignorance of hadronisation

- $F(w) = 1$  at the heavy-quark limit ( $m_b = m_c = \infty$ )

- Lattice calculation gives

$$F(1) = 0.919^{+0.030}_{-0.035}$$

Hashimoto et al,  
PRD 66 (2002) 014503

- Shape of  $F(w)$  unknown

- Parameterized with  $\rho^2$  (slope at  $w = 1$ ) and  $R_1, R_2$

- $B \rightarrow D^* \ell \nu$  decay rate in terms of helicity amplitudes is given by:

$$\frac{d\Gamma(B \rightarrow D^* \ell \nu)}{dq^2 d\cos\theta_\ell d\cos\theta_V d\chi} = \frac{3G_F^2 |V_{cb}|^2 P_{D^*} q^2}{8(4\pi)^4 M_B^2} \times$$

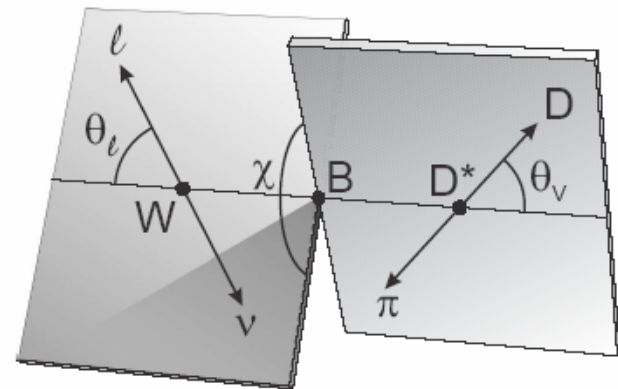
$$\{ H_+^2 (1 - \cos\theta_\ell)^2 \sin^2\theta_V + H_-^2 (1 + \cos\theta_\ell)^2 \sin^2\theta_V$$

$$+ 4H_0^2 \sin^2\theta_\ell \cos^2\theta_V - 2H_+ H_- \sin^2\theta_\ell \sin^2\theta_V \cos 2\chi$$

$$- 4H_+ H_0 \sin\theta_\ell (1 - \cos\theta_\ell) \sin\theta_V \cos\theta_V \cos\chi$$

$$+ 4H_- H_0 \sin\theta_\ell (1 + \cos\theta_\ell) \sin\theta_V \cos\theta_V \cos\chi \}$$

Angular kinematic variables :



The Helicity amplitudes  $H_i$  depend on Form Factor ratios  $R_1$  and  $R_2$

# Exclusive $|V_{cb}|$ : $B \rightarrow D^* \ell \nu$

New!

Extract  $D^* \ell \nu$  form factors from unbinned maximum likelihood fit to full 4-dim PDF

stat. MC stat. syst.

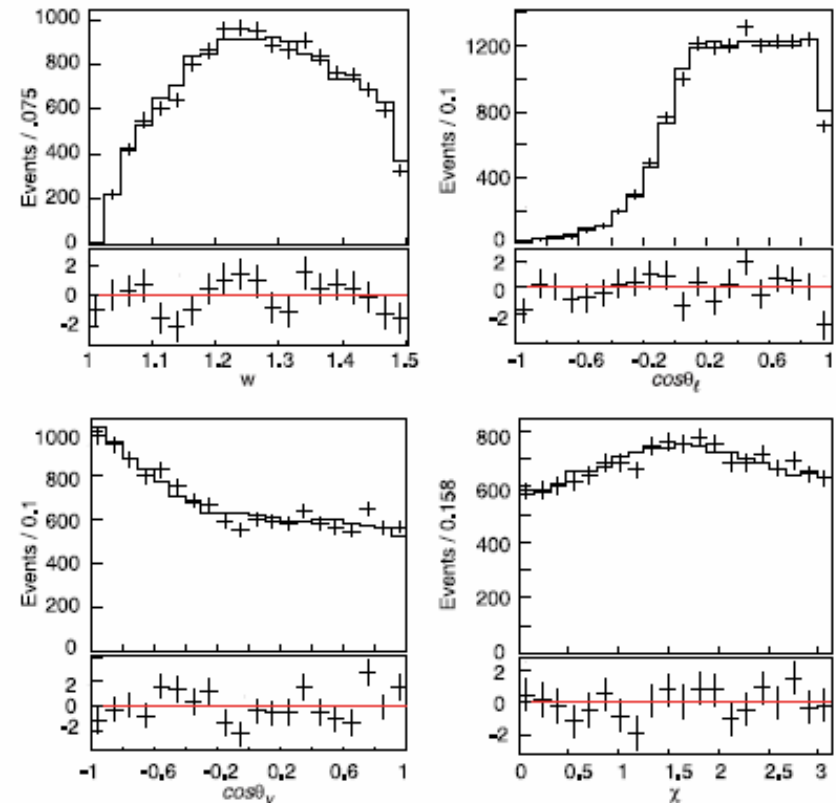
$$\begin{aligned} R_1 &= 1.396 \pm 0.060 \pm 0.035 \pm 0.027, \\ R_2 &= 0.885 \pm 0.040 \pm 0.022 \pm 0.013, \\ \rho^2 &= 1.145 \pm 0.059 \pm 0.030 \pm 0.035, \end{aligned}$$

Compared to FF from previous CLEO measurement, uncertainty on  $|V_{cb}|$  is reduced from +2.9% -2.6%  $\rightarrow \pm 0.5\%$   
Factor 5 improvement of FF uncertainty

Systematic error on  $|V_{cb}|$  from 4.5%  $\rightarrow 3.5\%$

$$|V_{cb}| = 37.6 \pm 0.3(stat) \pm 1.3(syst) {}^{+1.5}_{-1.3}(theory) \times 10^{-3}$$

One dimensional projections of the fit result:



hep-ex/0602023

Also leads to a reduction in systematic error on  $|V_{ub}|$  from Babar endpoint analysis  
Systematic error on BF reduced from 6.7%  $\rightarrow 2.8\%$

# Exclusive $|V_{ub}|$

- Measure specific final states, e.g.,  $B \rightarrow \pi \ell \nu$ ,  $B \rightarrow \rho \ell \nu$ 
  - Can achieve good signal-to-background ratio
  - Branching fractions are  $O(10^{-4}) \rightarrow$  statistics limited
- Need form factors to extract  $|V_{ub}|$

$$\frac{d\Gamma(B \rightarrow \pi \ell \nu)}{dq^2} = \frac{G_F^2}{24\pi^3} |V_{ub}|^2 p_\pi^3 |f_+(q^2)|^2$$

One FF for  $B \rightarrow \pi \ell \nu$   
(massless lepton)

- Theo. Uncertainties complementary to inclusive approach !
- $f_+(q^2)$  calculations exist based on:
  - Lattice QCD ( $q^2 > 16 \text{ GeV}^2$ )
    - ❖ recent “unquenched” calculations  $\rightarrow$  ~11% uncertainty
  - Light Cone Sum Rules ( $q^2 < 14 \text{ GeV}^2$ )  $\rightarrow$  ~10% uncertainty
  - Quark models (ISGW2) ... and other approaches

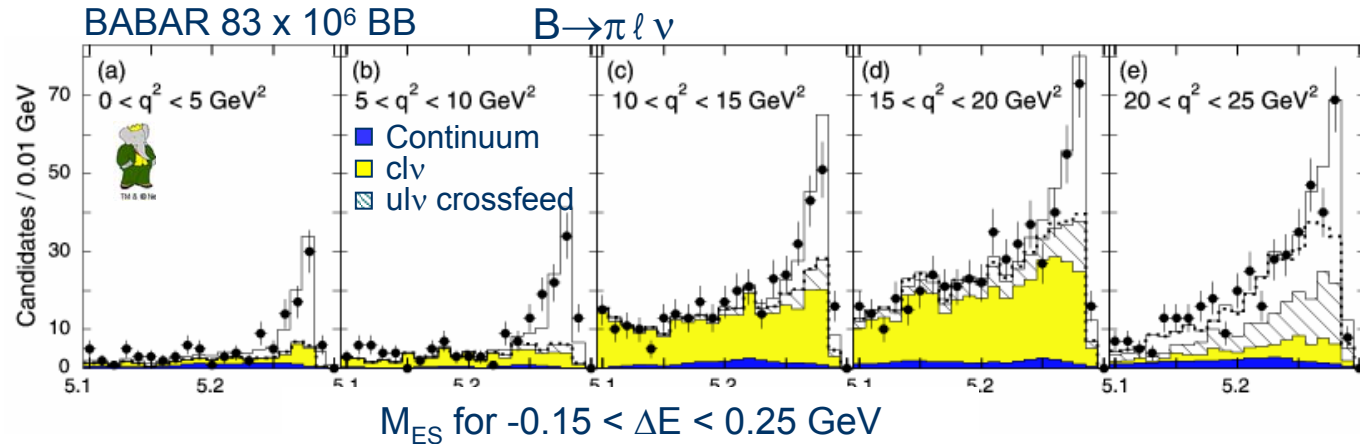
HPQCD  
hep-lat/0408019  
Fermilab  
hep-lat/0409166  
Ball,Zwicky  
hep-ph/0406232

# Exclusive $|V_{ub}|$ : $B \rightarrow \pi \ell \nu$

Babar untagged analysis:

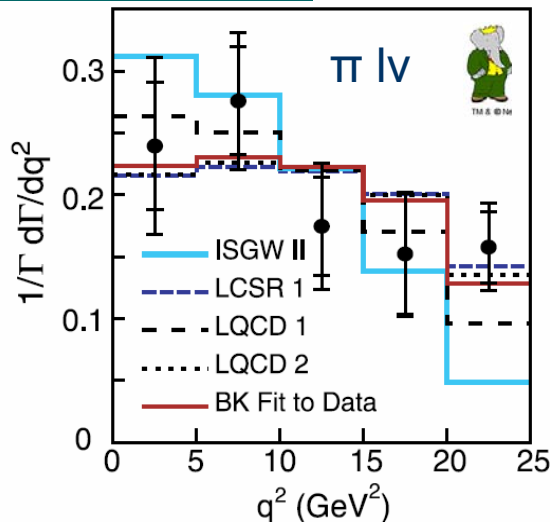
$\nu$  = missing  $(E, \vec{p})$  of the event

Fit of the signal yield using the B mass and  $\Delta E$  in bins of  $q^2$ .

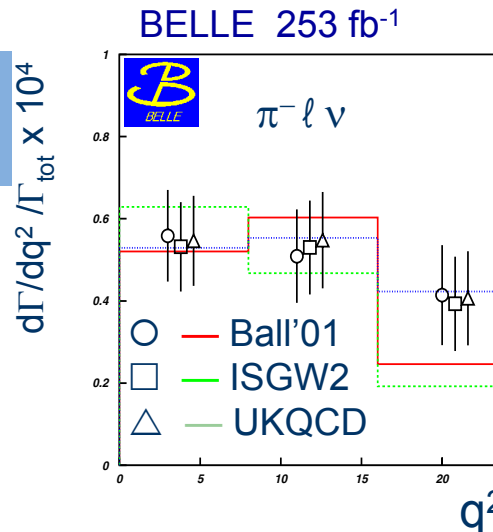


- Measure  $q^2$ -dependence of the form factor
- Compare with theoretical calculations

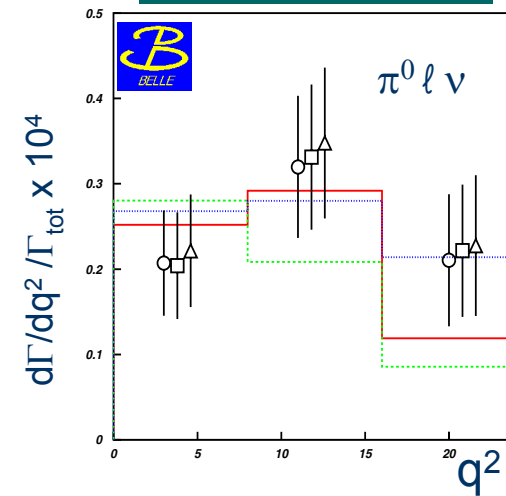
hep-ex/0507003



Belle with  $D^* l \nu$  tag

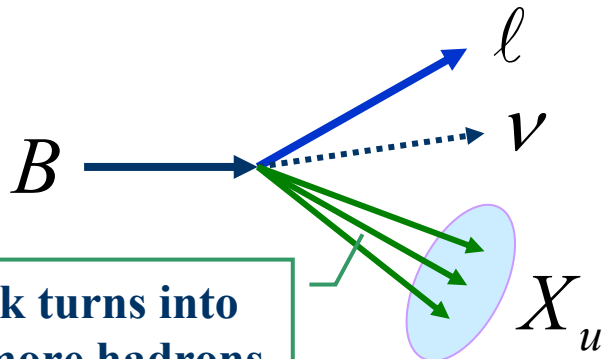


hep-ex/0508018



# Inclusive $b \rightarrow ul\nu$ : Strategies

- We use 3 variables to describe  $B \rightarrow Xl\nu$  decays:



$u$  quark turns into one or more hadrons

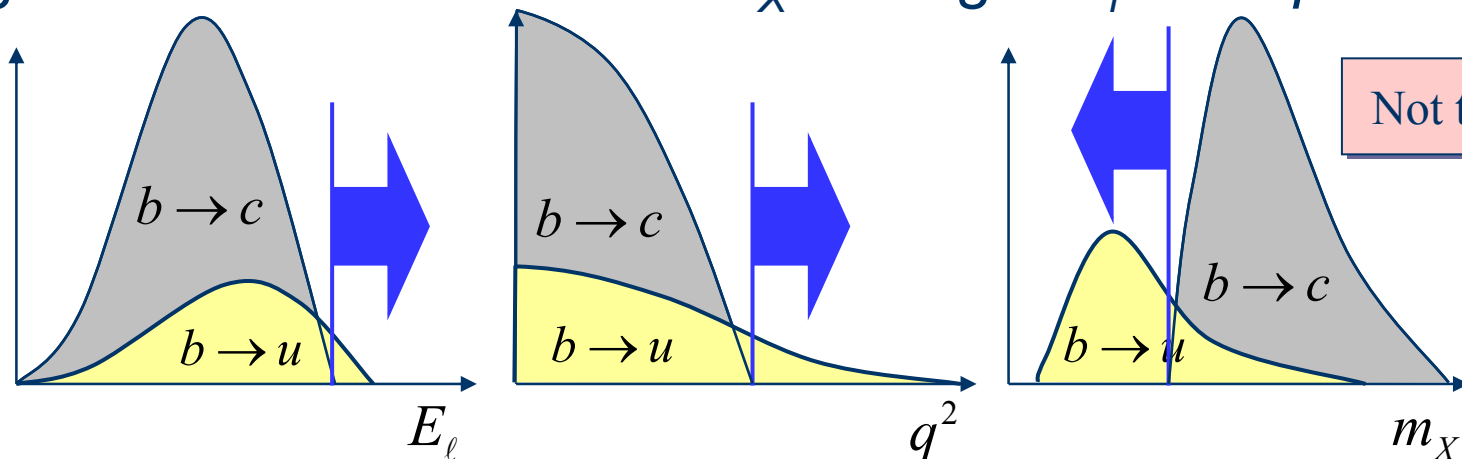
$E_l$  = lepton energy

$q^2$  = lepton-neutrino mass squared

$m_X$  = hadron system mass

Combine cuts on these variables to maximise phase space and minimise theory uncertainty

- Signal events have smaller  $m_X \rightarrow$  larger  $E_l$  and  $q^2$



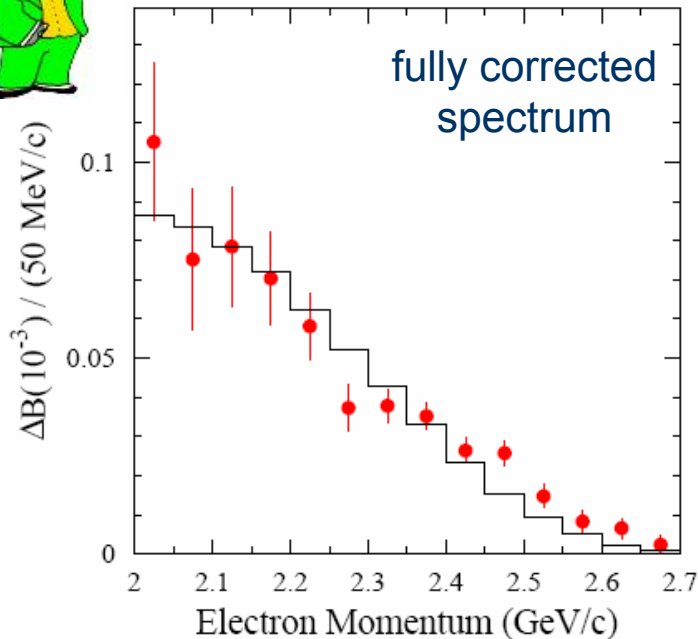
# Inclusive $|V_{ub}|$ : Endpoint

Measure rate in region where  $b \rightarrow cl\nu$  is largely forbidden, previously large extrapolation



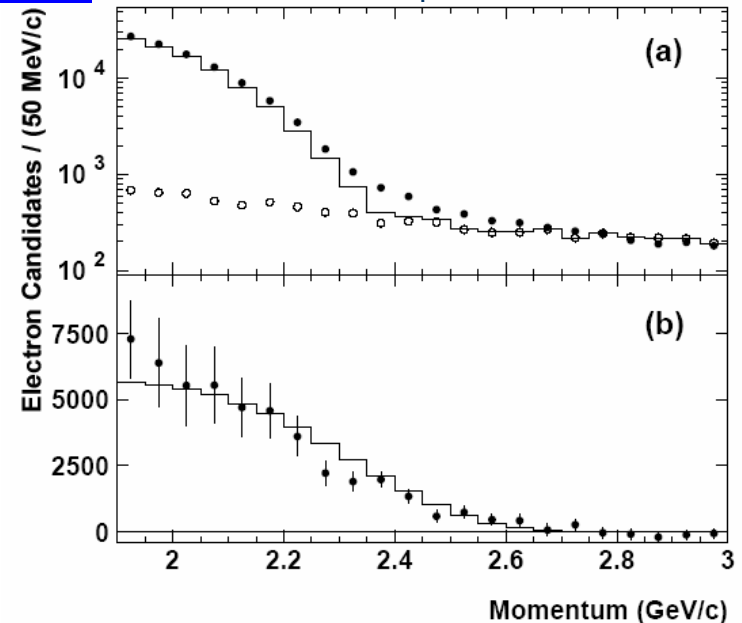
hep-ex/0509040

$2.0 \text{ GeV} < E_l < 2.6 \text{ GeV}$



hep-ex/0504046

$1.9 \text{ GeV} < E_l < 2.6 \text{ GeV}$



Calculations by Bosch, Lange, Neubert & Paz translate partial rate directly into  $|V_{ub}|$ :

Babar:  $|V_{ub}| = (4.44 \pm 0.25_{exp} {}^{+0.42}_{-0.38_{SF}} \pm 0.22_{theory}) \times 10^{-3}$

Belle:  $|V_{ub}| = (5.08 \pm 0.47_{exp} \pm 0.42_{SF} {}^{+0.26}_{-0.23_{theo}}) \times 10^{-3}$

# Inclusive $|V_{ub}|$ : Hadronic B tag

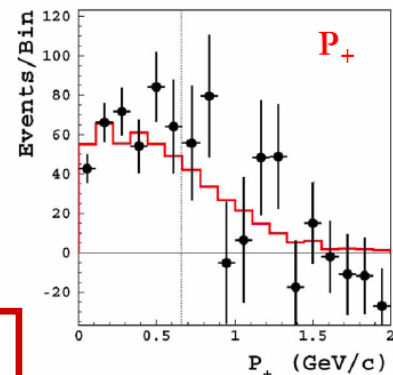
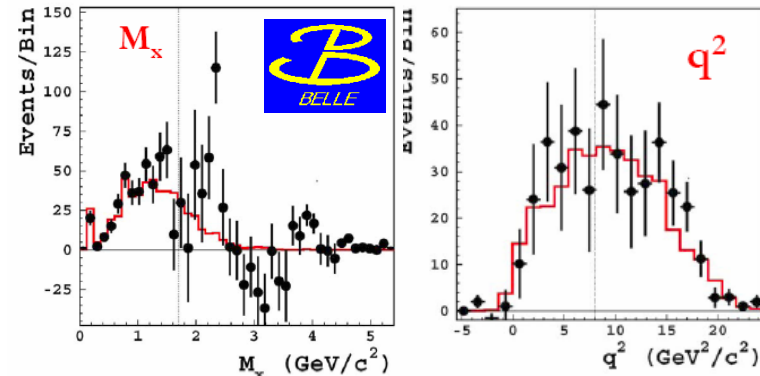
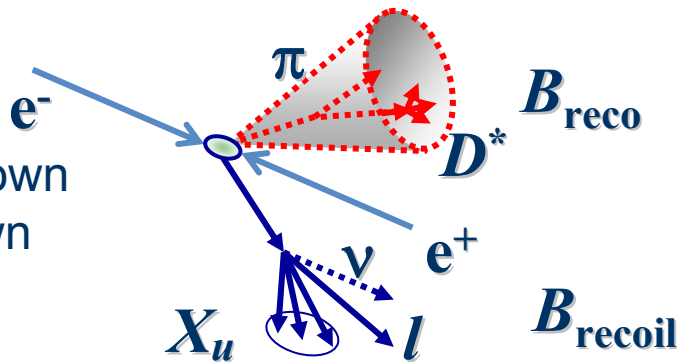
Fully reconstructed  $B$  recoil analysis:

Advantages:

- clean sample
- kinematics known
- B flavour known

Disadvantage:

- low statistics



Calculations of  
Bosch,Lange,Neubert,Paz  
hep-ph/0402094,0504071

Different phase space acceptances  
result in different theory errors!

Belle:

hep-ex/0505088

$\Delta\Phi$	$ V_{ub}  \times 10^3$	stat	syst	$b \rightarrow u$	$b \rightarrow c$	SF	th.
$M_X/q^2$	4.70	5.0	4.4	3.1	2.7	4.2	$+4.8$ $-5.2$
$M_X$	4.09	4.6	3.5	3.1	1.1	4.5	$+3.5$ $-3.8$
$P_+$	4.19	4.7	4.6	3.2	4.4	5.8	$+3.4$ $-3.5$

$M_X < 1.7 \text{ GeV}, q^2 > 8 \text{ GeV}^2$

$M_X < 1.7 \text{ GeV}$

$P_+ = E_X - |p_X| > 0.66$

Babar:

hep-ex/0507017

$$|V_{ub}| = (4.65 \pm 0.24_{\text{stat}} \pm 0.24_{\text{syst}} {}^{+0.46}_{-0.38\text{SF}} \pm 0.23_{\text{th}}) \times 10^{-3}$$

$M_X < 1.7 \text{ GeV}, q^2 > 8 \text{ GeV}^2$

# Inclusive $|V_{ub}|$

New!

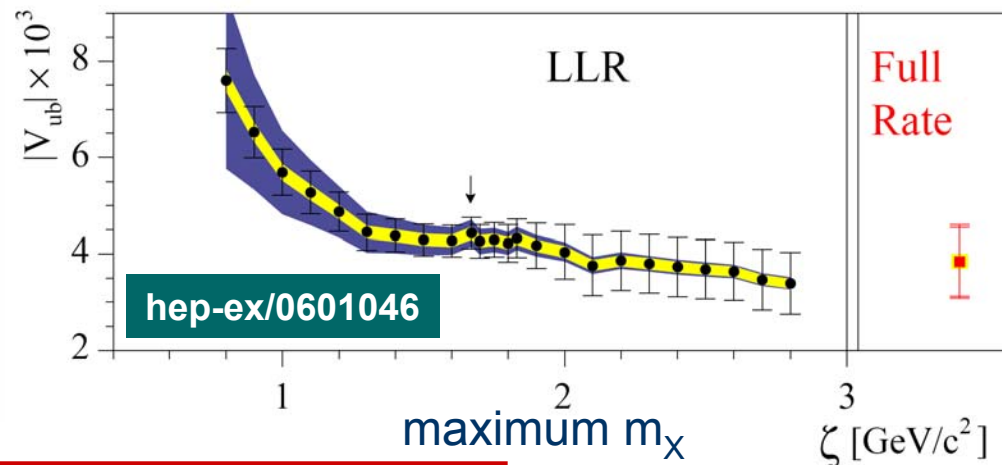
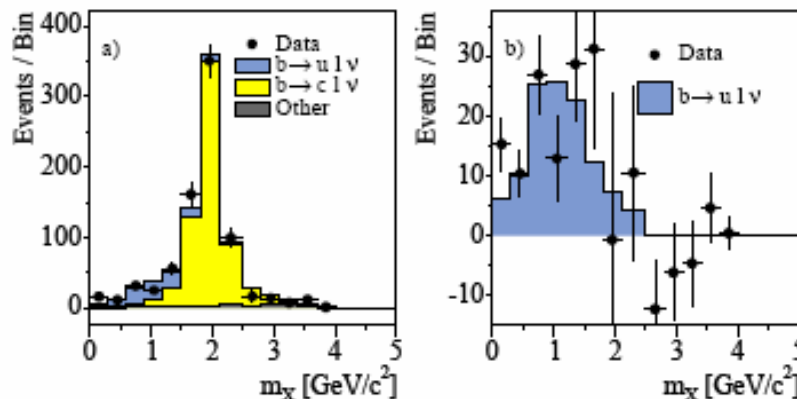
Relating  $b \rightarrow u \ell \nu$  to  $b \rightarrow s \gamma$  using weight functions:

*largely SF independent!*

$$\Gamma(B \rightarrow X_u \ell \nu) = \frac{|V_{ub}|^2}{|V_{ts}|^2} \int W(E_\gamma) \frac{d\Gamma(B \rightarrow X_s \gamma)}{dE_\gamma} dE_\gamma$$

Leibovich, Low, Rothstein  
hep-ph/0005124,0105066

Weight function



Standard local  
OPE for full rate:  
Uraltsev  
hep-ph/9905520  
Hoang, Ligeti,  
Manohar  
hep-ph/9811239

LLR :  $M_X < 1.67$  GeV:

$$|V_{ub}| = (4.43 \pm 0.38_{\text{stat}} \pm 0.25_{\text{syst}} \pm 0.29_{\text{theo}}) 10^{-3}$$

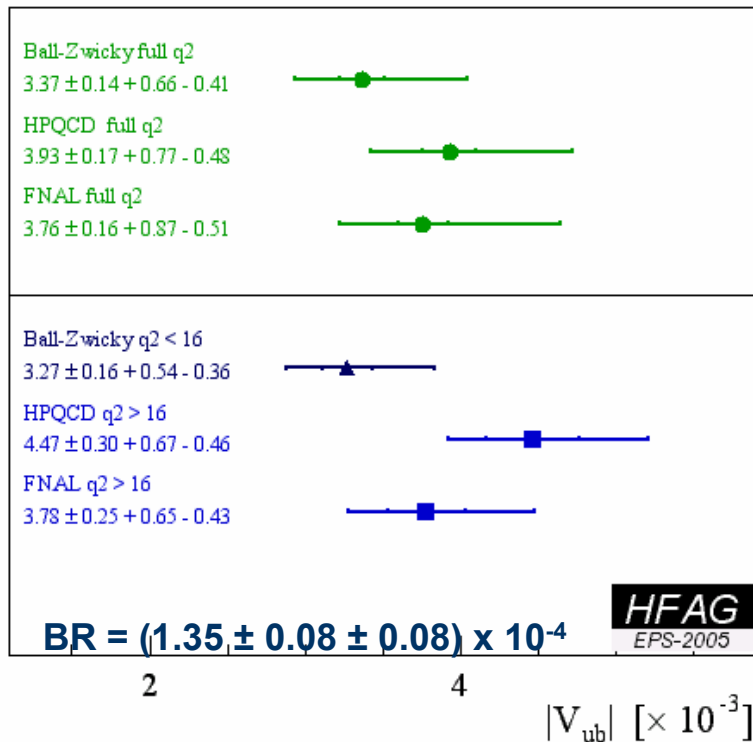
OPE:  $M_X < 2.50$  GeV:

$$|V_{ub}| = (3.84 \pm 0.70_{\text{stat}} \pm 0.30_{\text{syst}} \pm 0.10_{\text{theo}}) 10^{-3}$$

reduced theory error  
as no extrapolation to  
full rate necessary

# $|V_{ub}|$ Summary

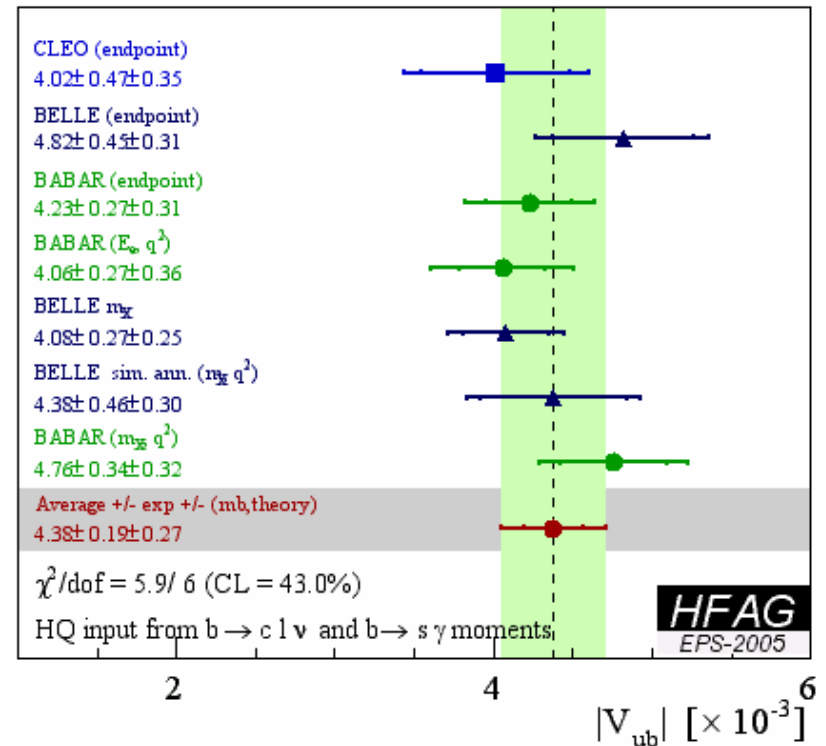
## Exclusive $|V_{ub}|$ :



4% exp., ~11% theory uncertainty

Errors on  $|V_{ub}|$  dominated  
 by FF normalization

## Inclusive $|V_{ub}|$ :



$|V_{ub}| = (4.38 \pm 0.19 \pm 0.27) \times 10^{-3}$   
 7.6 % total uncertainty!

Main improvement due to better knowledge  
 of “shape function” parameters

# Radiative B Decays: $b \rightarrow s, d \gamma$

- $b \rightarrow s, d$  transition is a Flavour Changing Neutral Current

- forbidden in the standard model at tree-level

- exists only at loop level

- heavy particles dominate in the loop

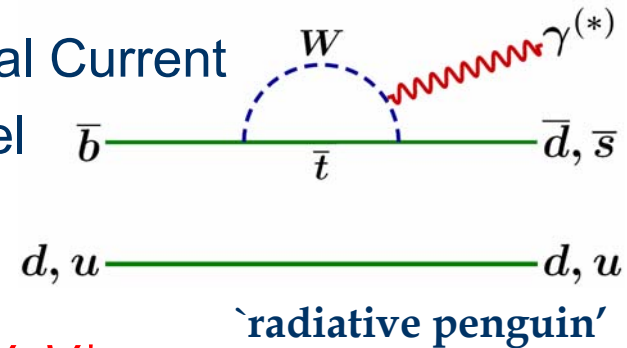
- in SM: sensitive to 'top' CKM parameters:  $V_{tb} V_{tq}^*$
  - sensitive to high virtual mass scale, e.g. from new physics

- We are unable to measure the parton level decay rate for  $b \rightarrow s \gamma$ , however:

$$\text{HQET} \Rightarrow \Gamma(B \rightarrow X_s \gamma) = \Gamma(b \rightarrow s \gamma) + \Delta^{\text{nonpert}}$$

Theoretical Framework: Operator Product Expansion  
separate weak scale from  $B$ -mass scale

- Theoretical uncertainty  $\sim 10\%$ , mainly from contribution of higher order diagrams in the expansion.



# $b \rightarrow s\gamma$ Spectra and Moments

Measure photon spectrum in  $b \rightarrow s\gamma$  decays:

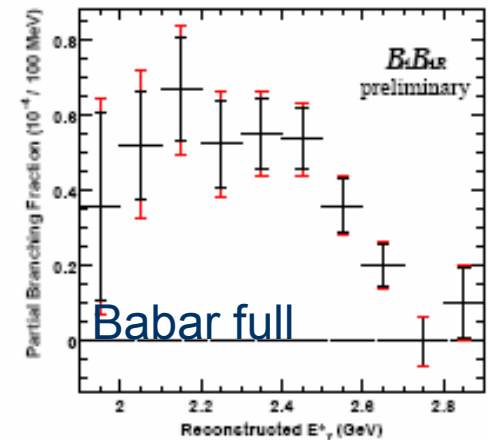
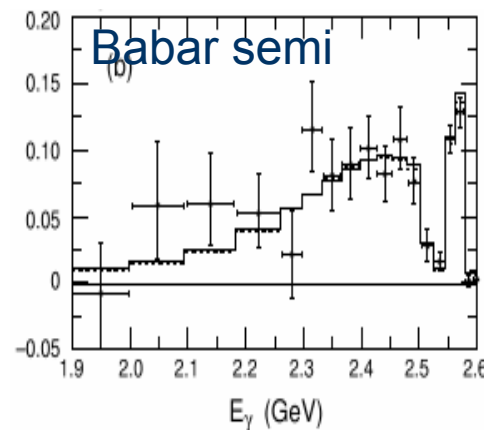
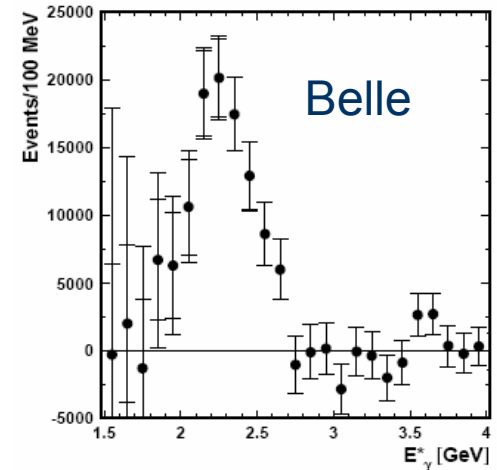
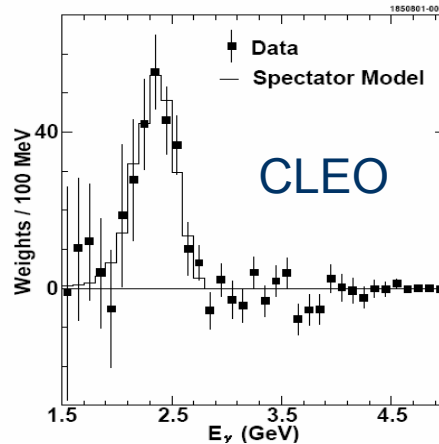
Two main approaches:

- Inclusive:
  - identify photon
- Semi-Inclusive:
  - reconstruct many exclusive final states (up to 38!)

Difficult measurement:  
Overwhelming background  
from  $\pi^0$ s for  $E_\gamma < 1.8$  GeV

Measurement of photon  
spectrum and its moments  
gives information about  
inner structure of B meson:

- $b$  quark mass
- Fermi momentum



# BR( $b \rightarrow s\gamma$ ) Average

- Experiments measure PBF's above different photon energies
- Need to be extrapolated to  $E_\gamma > 1.6$  GeV to compare with theory
- Extrapolation factors based on HQE fit to  $b \rightarrow clv$  and  $b \rightarrow s\gamma$  moments:

Standard Model Prediction \*

$$3.57 \pm 0.30 \times 10^{-4}$$

Nucl.Phys.B631:219-238,2002

CLEO PRL 87, 251807 (2001)

BELLE Phys.Lett. B 511, 151 (2001)

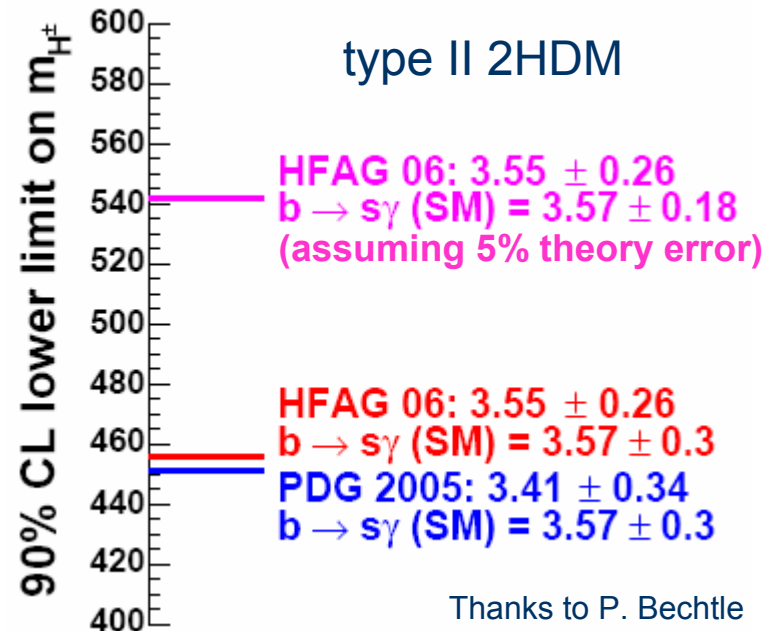
BELLE PRL.93:061803,(2004)

BABAR PRD 72, 052004 (2005)

BABAR hep-ex/0507001

New Average  
 $3.55 \pm 0.26 \times 10^{-4}$   
 HFAG prelim.

$$\text{BR}(b \rightarrow s\gamma)_{E_\gamma > 1.6 \text{ GeV}} \times 10^{-4}$$



## Outlook:

Exp. error will decrease with luminosity  
 Factor ~10 more data by 2008  
 Theo. uncertainty of 5% realistic with  
 NNLO calculation

\* Neubert & Hurth et al have slightly different theo. errors

# Fit to Moments of Inclusive Decay Distributions

**Heavy Quark Expansions** connect the inclusive decay width to  $|V_{cb}|$ :

$\Gamma_{SL}$  proportional to  $|V_{cb}|^2$ , but perturbative and non-perturbative corrections to free quark decay needed  $\rightarrow$  double expansion in  $\alpha_s$  and  $1/m_b$

$$\Gamma_{clv} = \frac{G_F m_b^5}{192\pi^3} |V_{cb}|^2 (1 + A_{ew}) A_{pert} A_{nonpert} \cong |V_{cb}|^2 f_{OPE}(m_b, m_c, a_i)$$

4 parameters at order  $\alpha_s^2$  and  $1/m_b^3$

Need to determine non-perturbative parameters!

$\rightarrow$  Use moments of inclusive distributions where same parameters appear:

$$\langle X^n \rangle (E_{cut}) = \frac{\int (X - X^0)^n \frac{d\Gamma}{dX} dX}{\int \frac{d\Gamma}{dX} dX} \bigg|_{E_l > E_{cut}} \cong f'_{OPE}(m_b, m_c, a_i)$$

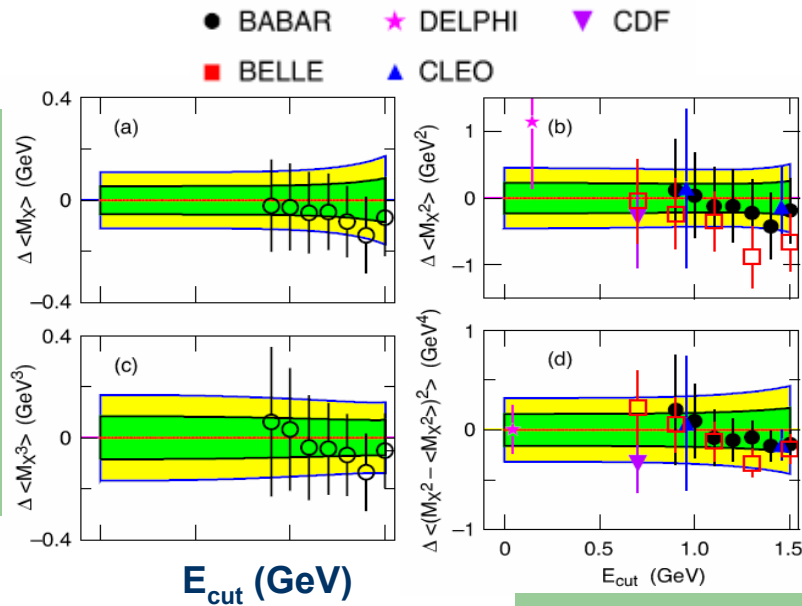
- Hadronic Mass distribution  $\langle M_X^n \rangle \rightarrow \langle M_X \rangle (m_b, m_c, \mu_\pi^2, \mu_G^2, \rho_D^3, \rho_{LS}^3, \alpha_s)$
- Lepton Energy spectrum  $\langle E_\ell^n \rangle \rightarrow \langle E_\ell \rangle (m_b, m_c, \mu_\pi^2, \mu_G^2, \rho_D^3, \rho_{LS}^3, \alpha_s)$
- Photon Energy spectrum  $\langle E_\gamma^n \rangle \rightarrow \langle E_\gamma \rangle (m_b, \mu_\pi^2, \mu_G^2, \rho_D^3, \rho_{LS}^3, \alpha_s)$  .

# Inclusive $|V_{cb}|$ - Fit to Moments

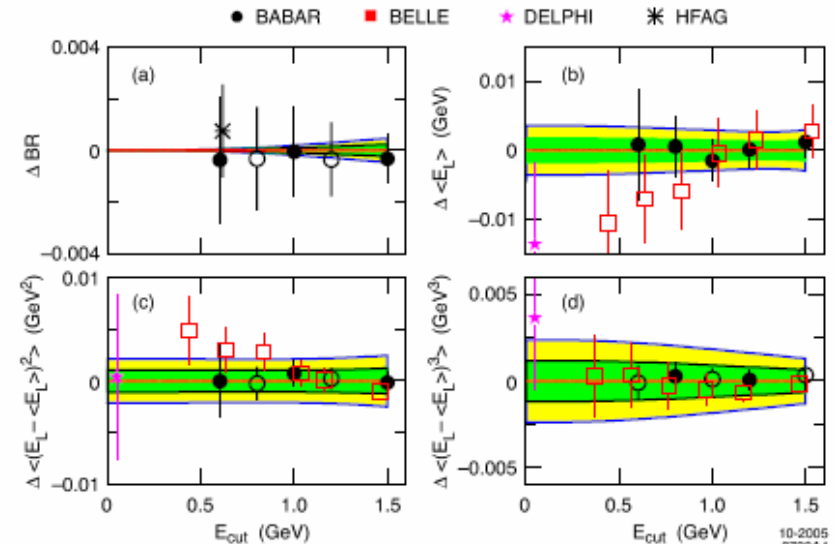
Based on calculations in kinetic scheme:

Benson, Bigi, Mannel & Uraltsev, hep-ph/0410080  
 Gambino & Uraltsev, hep-ph/0401063  
 Benson, Bigi & Uraltsev, hep-ph/0410080

Hadron Moments

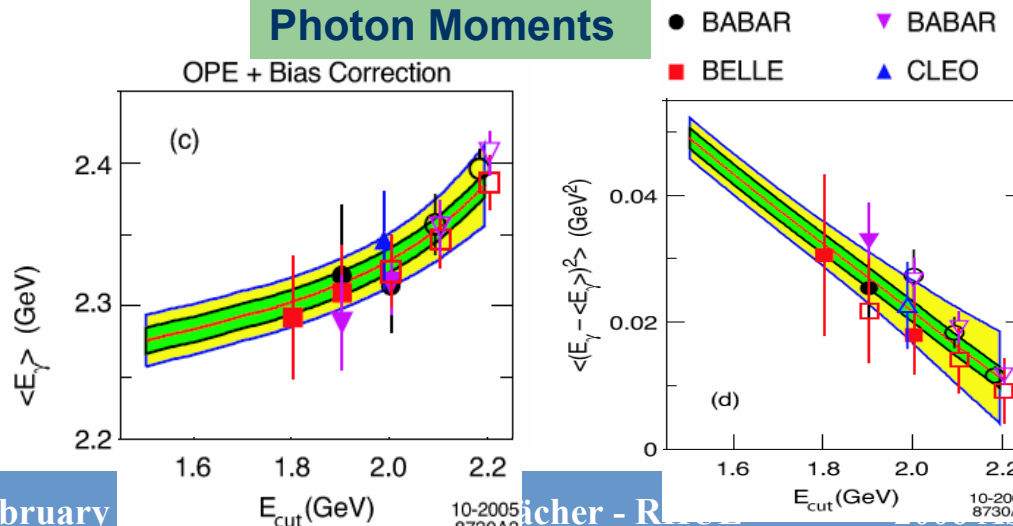


Lepton Moments



Photon Moments

Measurements highly correlated!



O. Buchmüller, H.F.  
 hep-ph/0507253

# Inclusive $|V_{cb}|$

New!

Result of fit to all  
moment measurements:

$|V_{cb}|$  @ 2%  
 $m_b < 1\%$   
 $m_c$  @ 5%

In  $\overline{MS}$  scheme:

$$\overline{m}_b(\overline{m}_b) = 4.20 \pm 0.04 \text{ GeV}$$

$$\overline{m}_c(\overline{m}_c) = 1.24 \pm 0.07 \text{ GeV}$$

$$\overline{m}_c(\mu)/\overline{m}_b(\mu) = 0.235 \pm 0.012$$

courtesy of N.Uraltsev

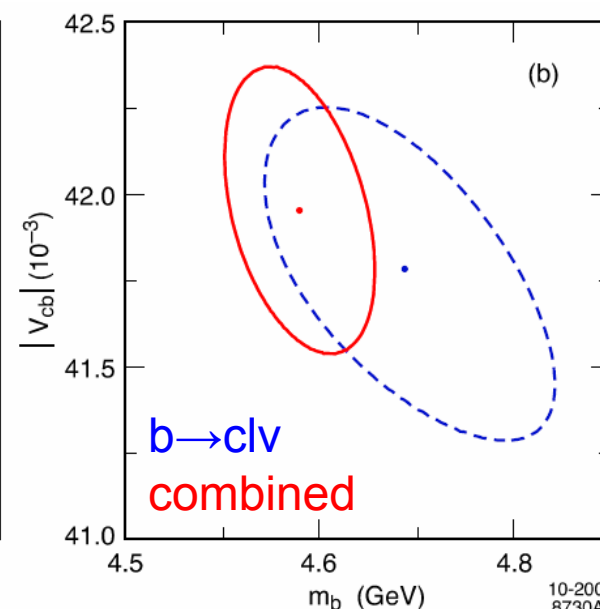
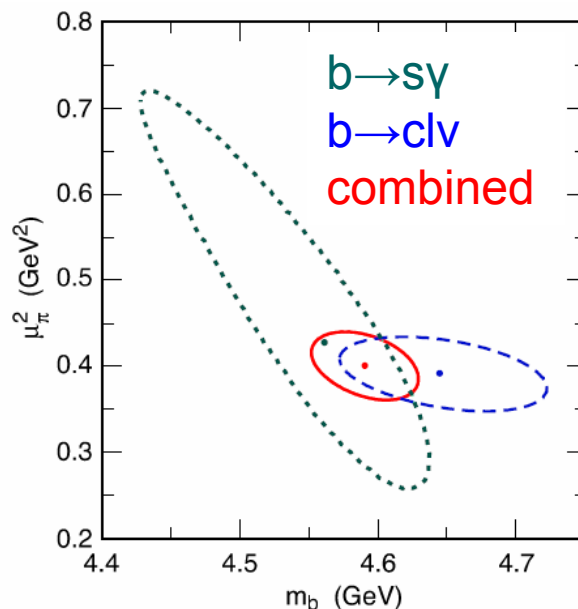
Good agreement with other  
similar analyses:

Bauer et al. [hep-ph/0408002](#)

DELPHI [hep-ex/0510024](#)

	exp	HQE	$\Gamma_{SL}$
$ V_{cb}  =$	$(41.96 \pm 0.23)$	$\pm 0.35$	$\pm 0.59) 10^{-3}$
$m_b =$	$4.590 \pm 0.025$	$\pm 0.030$	GeV
$m_c =$	$1.142 \pm 0.037$	$\pm 0.045$	GeV
$\mu_\pi^2 =$	$0.401 \pm 0.019$	$\pm 0.035$	GeV <sup>2</sup>
$\mu_G^2 =$	$0.297 \pm 0.024$	$\pm 0.046$	GeV <sup>2</sup>
$\rho_D^3 =$	$0.174 \pm 0.009$	$\pm 0.022$	GeV <sup>3</sup>
$\rho_{LS}^3 =$	$-0.183 \pm 0.054$	$\pm 0.071$	GeV <sup>3</sup>
$BR_{clv} =$	$10.71 \pm 0.10$	$\pm 0.08$	%

hep-ph/0507253



10-2005  
8730A1

# $b \rightarrow d\gamma$

## Motivation:

- $b \rightarrow d\gamma$  transition,  $\text{BF} \propto |V_{td} V_{tb}|^2$
- SM prediction:  $0.9 - 1.8 \times 10^{-6}$
- clean SM prediction for ratio of  $B \rightarrow \rho/\omega\gamma$  and  $B \rightarrow K^*\gamma$ :

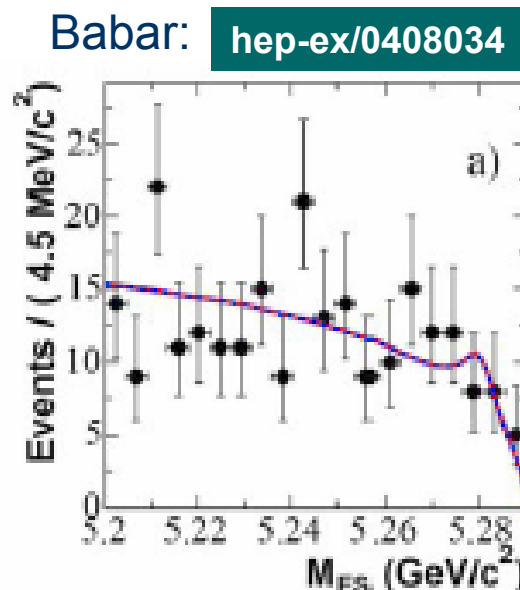
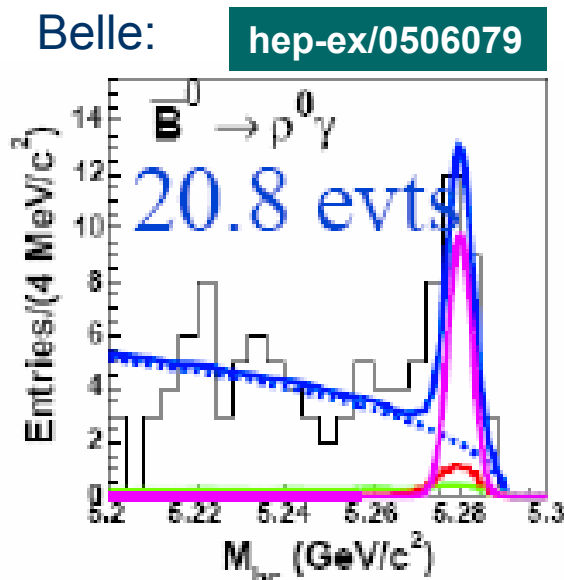
$$\frac{\overline{\mathcal{B}}[B \rightarrow (\rho/\omega)\gamma]}{\mathcal{B}(B \rightarrow K^*\gamma)} = \left| \frac{V_{td}}{V_{ts}} \right|^2 \left( \frac{1 - m_\rho^2/M_B^2}{1 - m_{K^*}^2/M_B^2} \right)^3 \zeta^2 [1 + \Delta R]$$

Ali and Parkhomenko,  
Eur.Phys.JC 23,89 (2002)  
Ali et al, PLB 595,323 (2004)

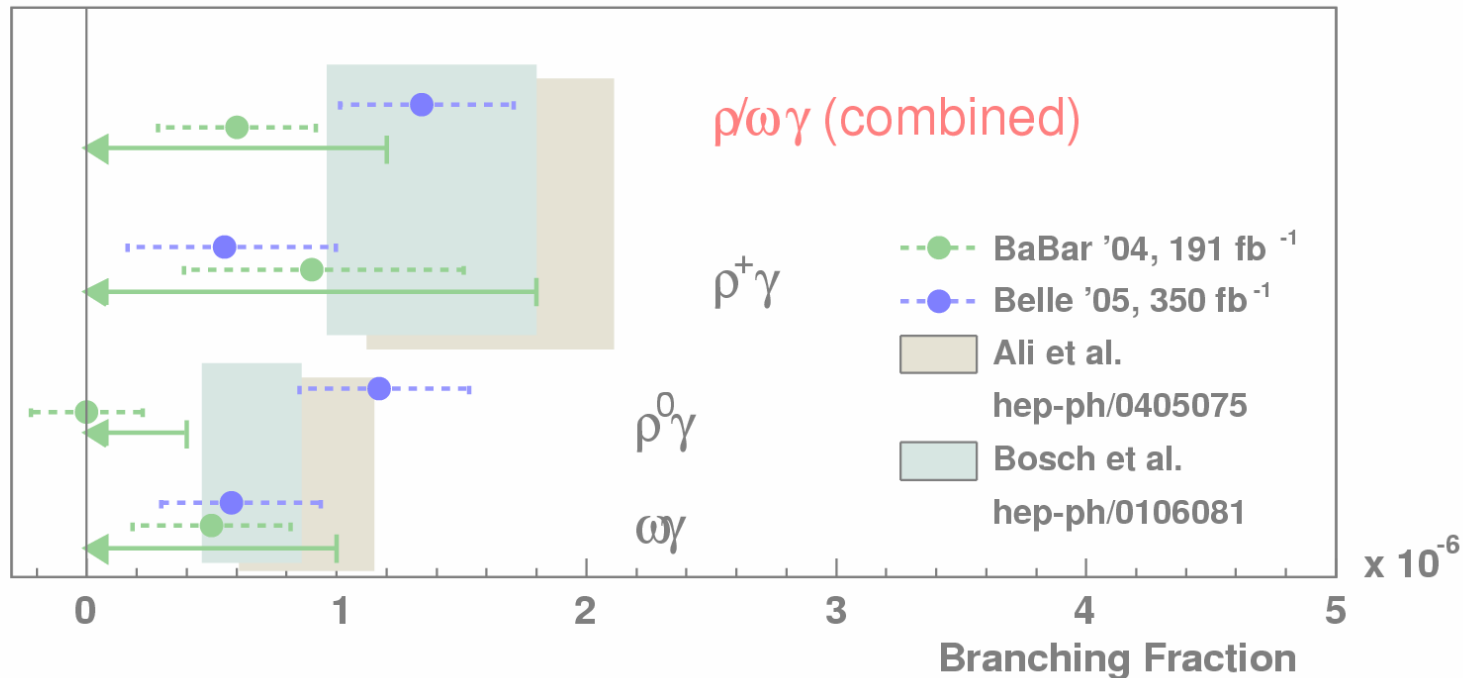
difference in dynamics  
(such as W-annihilation)  
 $\Delta R \approx 0.1 \pm 0.1$

form factor ratio  
 $\zeta^2 \approx 0.85 \pm 0.1$   
(largest uncertainty)

Average  
branching fractions



# $b \rightarrow d \gamma$



• BaBar and Belle are  $2.7\sigma$  apart in  $B^0 \rightarrow \rho^0 \gamma$

▪ BaBar low compared to theory prediction

## $B \rightarrow K^* \gamma$ :

Good agreement between Babar and Belle!

$$B(B^0 \rightarrow K^{*0} \gamma) = (40.1 \pm 2.0) \times 10^{-6}$$

$$B(B^+ \rightarrow K^{*+} \gamma) = (40.3 \pm 2.6) \times 10^{-6}$$

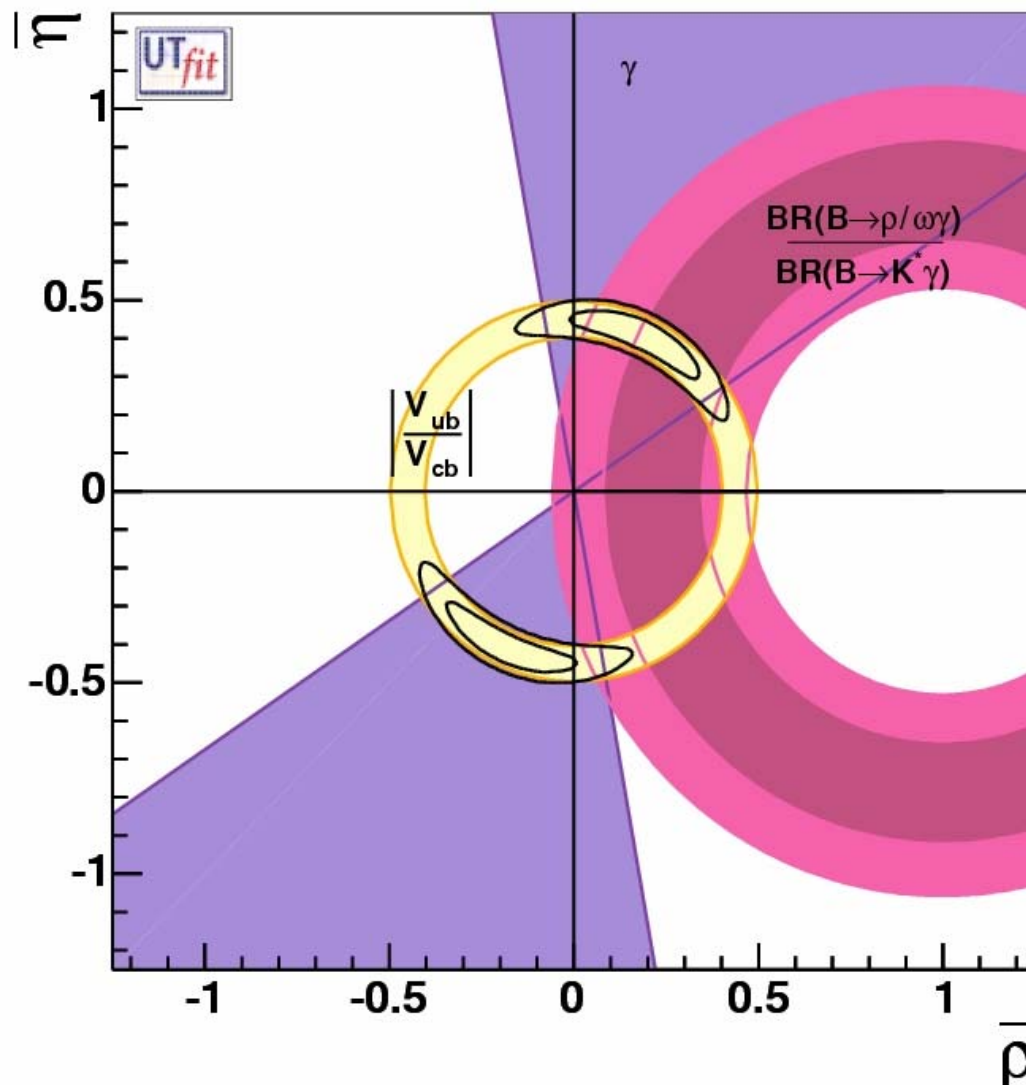
HFAG Summer 2005

# UT Constraints from Sides and Tree Processes

Based on:

$$\text{BR}(B^0 \rightarrow \rho/\omega \gamma) = (0.94 + 0.25 - 0.22) 10^{-6}$$

$$|V_{td}/V_{ts}| = 0.18 \pm 0.03$$

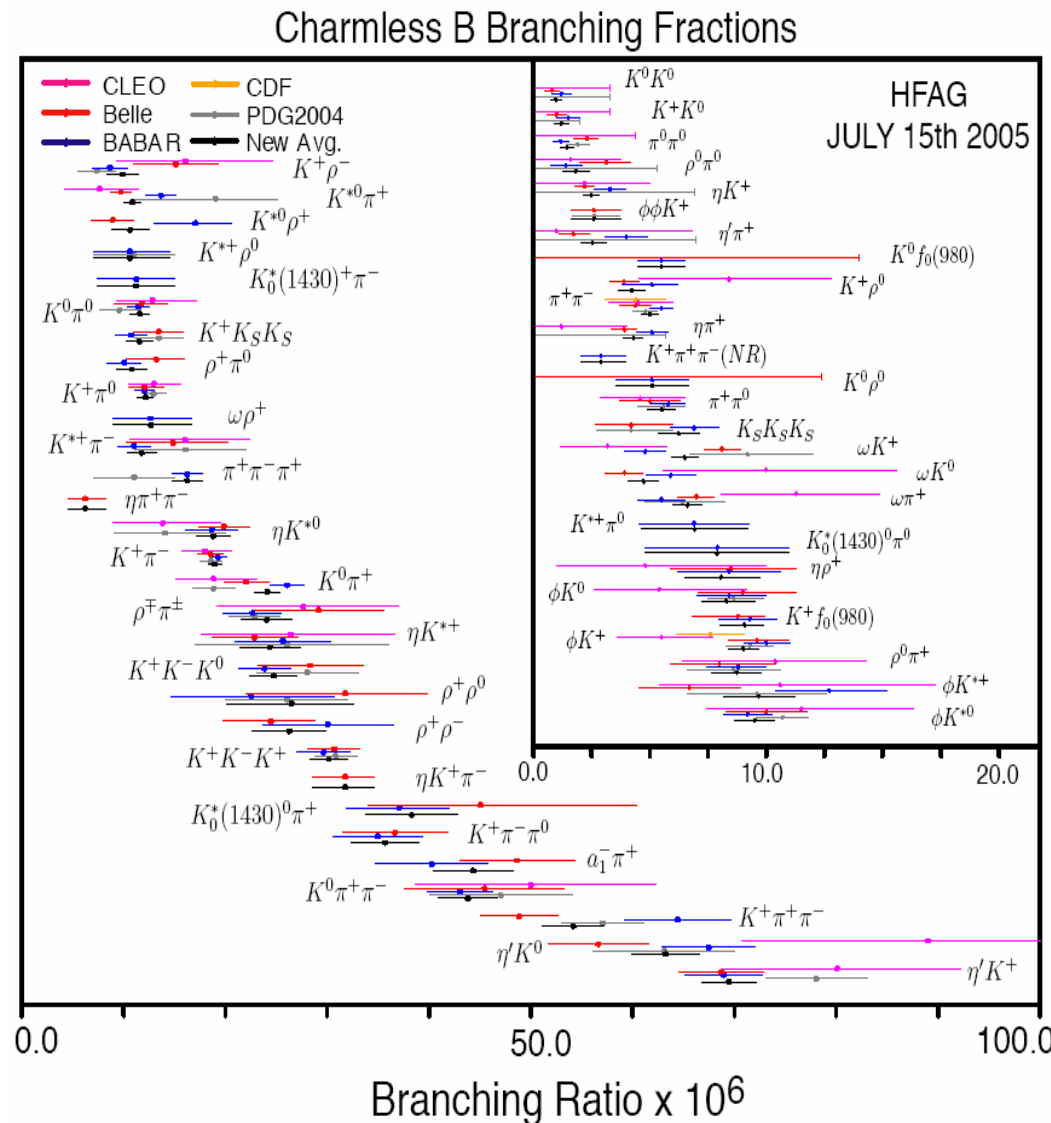


# Other Rare B Decays

- Charmless Hadronic B Decays
  - I will be selective and only pick 2 examples:
    - ❖ Bounds on  $\Delta S$  and  $\sin 2\beta$  from  $B \rightarrow \eta' K_s$
    - ❖  $B^+ \rightarrow K^+ \pi^- \pi^+$
- $B \rightarrow$  Charm Decays via W-exchange
  - $B \rightarrow D_s D_s$
- $B \rightarrow$  Charm Decays via Annihilation
  - $B \rightarrow D_s \varphi$
  - No decay that occurs through annihilation has been observed
- Decays are suppressed in the Standard Model
  - Standard Model BR of order  $10^{-5} - 10^{-7}$
- Potential for New Physics
  - Beyond SM contributions can lead to enhanced BR's

# Rare Charmless B Decays

- Too many decays to be discussed in detail...
- Rare Charmless  $B$  decays can be used to study
  - Interfering standard model amplitudes
  - Amplitudes of CKM parameters and angles
  - Effects of higher mass particles in loops
- Measurements are used to improve theoretical models



# Bounds on the tree contribution in $B \rightarrow \eta' K_S$

Difference in  $\sin(2\beta)$  from  $b \rightarrow c\bar{c}s$  and  $b \rightarrow q\bar{q}s$  penguin

$$B \rightarrow \psi K_S \quad \sin 2\beta = 0.69 \pm 0.03$$

$$B \rightarrow \eta' K_S \quad \sin 2\beta_{\text{eff}} = 0.50 \pm 0.09$$

It's possible to set theoretical bounds on this difference:

$$\Delta S_{\text{th}} = S(\eta' K_S) - \sin 2\beta < |\xi_{\eta' K_S}|$$

is a function of BF for Flavour SU(3) related decay modes:

$$|\xi_{\eta' K_S}| < \left| \frac{V_{us}}{V_{ud}} \right| \left[ 0.59 \sqrt{\frac{\mathcal{B}(\eta' \pi^0)}{\mathcal{B}(\eta' K^0)}} + 0.33 \sqrt{\frac{\mathcal{B}(\eta \pi^0)}{\mathcal{B}(\eta' K^0)}} + 0.14 \sqrt{\frac{\mathcal{B}(\pi^0 \pi^0)}{\mathcal{B}(\eta' K^0)}} \right. \\ \left. + 0.53 \sqrt{\frac{\mathcal{B}(\eta' \eta')}{\mathcal{B}(\eta' K^0)}} + 0.38 \sqrt{\frac{\mathcal{B}(\eta \eta)}{\mathcal{B}(\eta' K^0)}} + 0.96 \sqrt{\frac{\mathcal{B}(\eta \eta')}{\mathcal{B}(\eta' K^0)}} \right]$$

Will improve with more measurements!

Theory:  $\Delta S < 0.05$

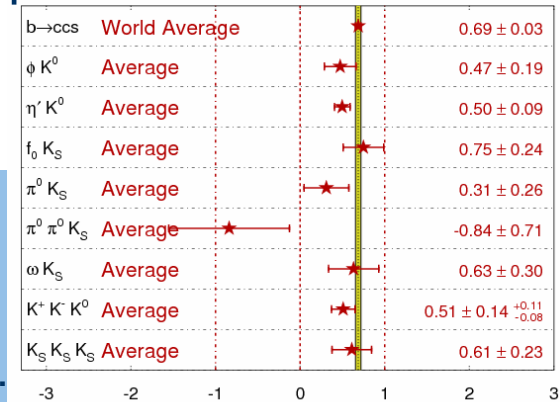
Experiment:  $\Delta S = 0.19 \pm 0.09$

If  $\Delta S \gg 0.1$

→ signature for new physics

Other approaches: Buchalla et al., Beneke

$\sin(2\beta^{\text{eff}})/\sin(2\phi_1^{\text{eff}})$  **HFAG**  
HEP 2005  
PRELIMINARY



hep-ph/0303171

HFAG Summer 2005

$\eta' \pi^0$	$< 3.7 \times 10^{-6}$	90% CL
$\eta \pi^0$	$< 2.5 \times 10^{-6}$	90% CL
$\pi^0 \pi^0$	$= 1.45 \pm 0.29 \times 10^{-6}$	
$\eta' \eta'$	$< 10 \times 10^{-6}$	90% CL
$\eta \eta$	$< 2.0 \times 10^{-6}$	90% CL
$\eta \eta'$	$< 4.6 \times 10^{-6}$	90% CL
$\eta' K^0$	$= 63.2 \pm 3.3 \times 10^{-6}$	

# Dalitz plot analysis of $B^+ \rightarrow K^+ \pi^- \pi^+$

$B^+ \rightarrow K^+ \pi^- \pi^+$  occurs via intermediate quasi two-body resonances (e.g.  $K^* \pi$ ,  $\rho K$ ) as well as non-resonant

Theoretical models predict BR and CP asymmetries for  $B \rightarrow K^* \pi$  and  $B \rightarrow \rho K$

General good agreement!

*Belle* finds  $3.9\sigma$  evidence for direct CP violation in  $B^+ \rightarrow \rho K^+$  from a phase and magnitude analysis

Babar finds  $2.4\sigma$  for  $A_{cp}$

(Distinguish  $A_{cp}$  from direct CP violation)

Babar :

Mode	$\mathcal{B}(B^+ \rightarrow \text{Mode})(10^{-6})$	$A_{CP} (\%)$
$K^+ \pi^- \pi^+$ Total	$64.1 \pm 2.4 \pm 4.0$	$-1.3 \pm 3.7 \pm 1.1$
$K^{*0}(892)\pi^+; K^{*0}(892) \rightarrow K^+ \pi^-$	$8.99 \pm 0.78 \pm 0.48^{+0.28}_{-0.39}$	$6.8 \pm 7.8 \pm 5.7^{+4.0}_{-3.5}$
$(K\pi)_0^{*0}\pi^+; (K\pi)_0^{*0} \rightarrow K^+ \pi^-$	$34.0 \pm 1.7 \pm 1.5^{+1.2}_{-1.6}$	$-6.4 \pm 3.2 \pm 2.0^{+1.1}_{-1.7}$
$\rho^0(770)K^+; \rho^0(770) \rightarrow \pi^+ \pi^-$	$5.07 \pm 0.75 \pm 0.35^{+0.42}_{-0.68}$	$32 \pm 13 \pm 6^{+8}_{-5}$
$f_0(980)K^+; f_0(980) \rightarrow \pi^+ \pi^-$	$9.47 \pm 0.97 \pm 0.46^{+0.42}_{-0.75}$	$8.8 \pm 9.5 \pm 2.6^{+9.3}_{-5.0}$
$\chi_{c0}K^+; \chi_{c0} \rightarrow \pi^+ \pi^-$	$0.66 \pm 0.22 \pm 0.07 \pm 0.03$	—
$K^+ \pi^- \pi^+$ nonresonant	$2.85 \pm 0.64 \pm 0.41^{+0.70}_{-0.34}$	—

Belle:

Mode	$\mathcal{B}(B^\pm \rightarrow R h^\pm \rightarrow K^\pm \pi^\pm \pi^\mp) \times 10^6$	$A_{CP} (\%)$
$K^\pm \pi^\pm \pi^\mp$ Charmless	$48.8 \pm 1.1 \pm 3.6$	$+4.9 \pm 2.6 \pm 2.0$
$K^*(892)[K^\pm \pi^\mp]\pi^\pm$	$6.45 \pm 0.43 \pm 0.48^{+0.25}_{-0.35}$	$-14.9 \pm 6.4 \pm 2.0^{+0.8}_{-0.8}$
$K_0^*(1430)[K^\pm \pi^\mp]\pi^\pm$	$32.0 \pm 1.0 \pm 2.4^{+1.1}_{-1.9}$	$+7.6 \pm 3.8 \pm 2.0^{+2.0}_{-0.9}$
$\rho(770)^0[\pi^+ \pi^-]K^\pm$	$3.89 \pm 0.47 \pm 0.29^{+0.32}_{-0.29}$	$+30 \pm 11 \pm 2.0^{+11}_{-4}$
$f_0(980)[\pi^+ \pi^-]K^\pm$	$8.78 \pm 0.82 \pm 0.65^{+0.59}_{-1.64}$	$-7.7 \pm 6.5 \pm 2.0^{+4.1}_{-1.6}$
$f_2(1270)[\pi^+ \pi^-]K^\pm$	$0.75 \pm 0.17 \pm 0.06^{+0.11}_{-0.18}$	$-59 \pm 22 \pm 2.0^{+3}_{-3}$
Non-resonant	—	—
$\chi_{c0}[\pi^+ \pi^-]K^\pm$	$0.56 \pm 0.06 \pm 0.04^{+0.12}_{-0.04}$	$-6.5 \pm 20 \pm 2.0^{+2.9}_{-1.4}$

hep-ex/0507004

hep-ex/0512066

First observation of  $B \rightarrow f_2 K$

First evidence of direct CP violation in a charged B decay

$$B^0 \rightarrow D_s^{(*)+} D_s^{(*)-}$$

Decay proceeds via W-exchange  
highly suppressed in SM

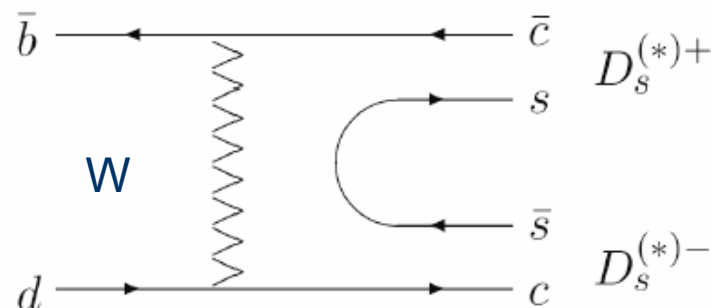
Difficult to calculate using factorisation  
approach as energy release only  $\sim 1$  GeV

Theoretical predictions:

- perturbative QCD (pQCD)  
[hep-ph/0308243](#)
- estimates of non-factorisable  
contributions (CL-GC) [hep-ph/0501031](#)
  - chiral loops and tree level amplitudes  
generated by soft gluon emission  
forming a gluon condensate

$B$ Decays	Branching Fraction ( $\times 10^{-5}$ )	
	pQCD [2]	CL-GC [3]
$B^0 \rightarrow D_s^- D_s^+$	$7.8 \pm_{1.6}^{2.0}$	25.0
$B^0 \rightarrow D_s^{*-} D_s^+$	$6.0 \pm_{1.1}^{1.6}$	33.0
$B^0 \rightarrow D_s^{*-} D_s^{*+}$	$8.5 \pm_{1.8}^{2.0}$	54.0

disfavoured



Babar ([hep-ex/0510051](#)) @ 90% C.L.

$$\begin{aligned} \mathcal{B}(B^0 \rightarrow D_s^- D_s^+) &< 1.0 \times 10^{-4}, \\ \mathcal{B}(B^0 \rightarrow D_s^{*-} D_s^+) &< 1.3 \times 10^{-4}, \\ \mathcal{B}(B^0 \rightarrow D_s^{*-} D_s^{*+}) &< 2.4 \times 10^{-4}. \end{aligned}$$

Belle ([hep-ex/0508040](#)) @ 90% C.L.

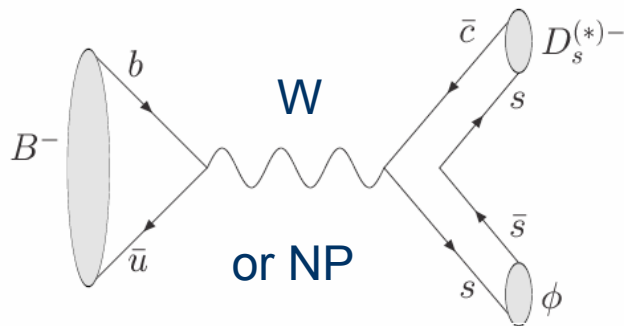
$$\mathcal{B}(B^0 \rightarrow D_s^- D_s^+) < 2.0 \times 10^{-4}$$

No signal observed and no  
evidence of significant W-exchange  
component in  $B^0 \rightarrow D^+ D^-$ , but:

Sensitivity to test SM prediction

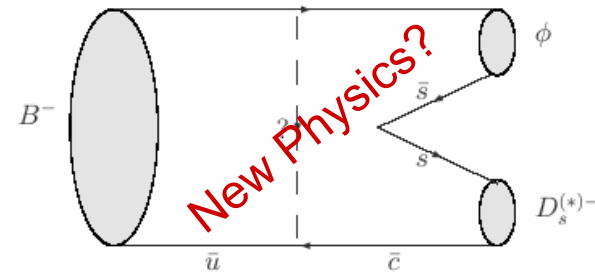
# $B \rightarrow D_s \phi$

Standard Model:

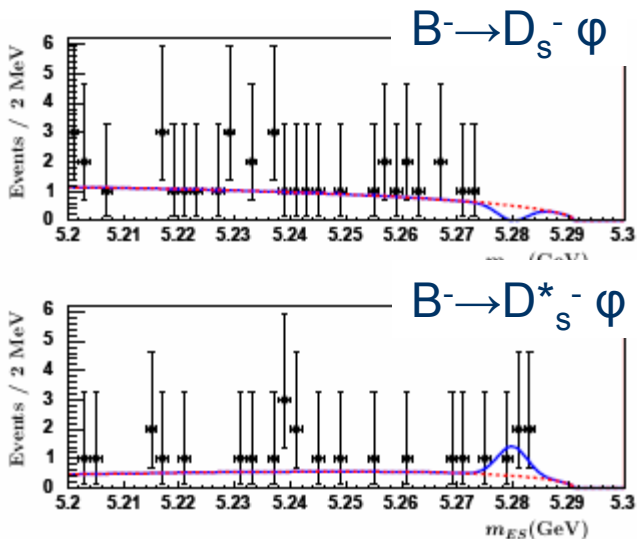


Highly suppressed in SM:  
 perturbative QCD:  $3 \times 10^{-7}$   
 QCD improved factorisation  $7 \times 10^{-7}$

New Physics: FCNC



Sensitivity to New Physics:  
 type II 2Higgs Doublet Model:  $8 \times 10^{-6}$   
 MSSM with R-parity violation:  $3 \times 10^{-4}$



Babar limit @ 90% C.L.  
 $BR(B^- \rightarrow D_s^- \phi) < 1.9 \times 10^{-6}$   
 $BR(B^- \rightarrow D_s^{*-} \phi) < 1.2 \times 10^{-5}$

Previous CLEO limit @ 90% C.L.

$BR(B^- \rightarrow D_s^- \phi) < 3 \times 10^{-4}$   
 $BR(B^- \rightarrow D_s^{*-} \phi) < 4 \times 10^{-4}$

Phys.Lett.B319:  
 365,1993

hep-ex/0512028

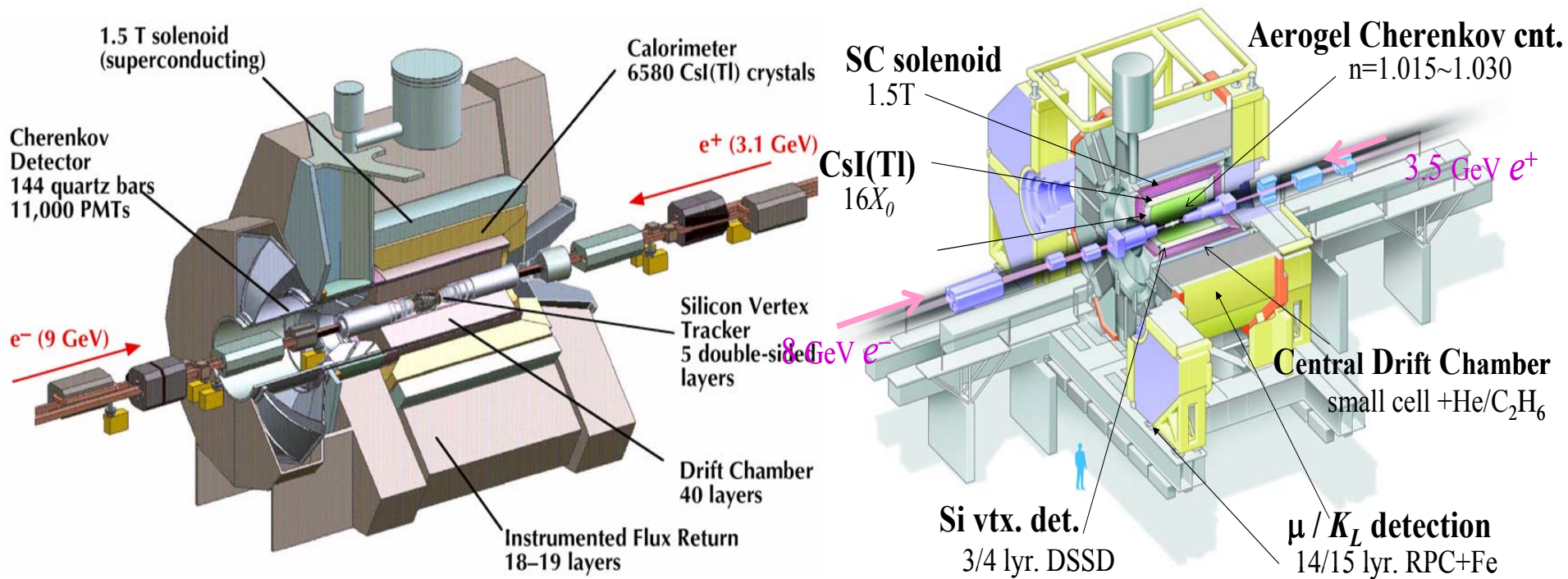
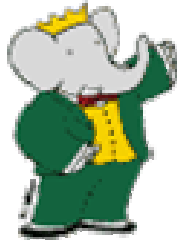
Measurement still one order of  
 magnitude away from SM prediction  
 but limits on NP possible.

# Conclusions

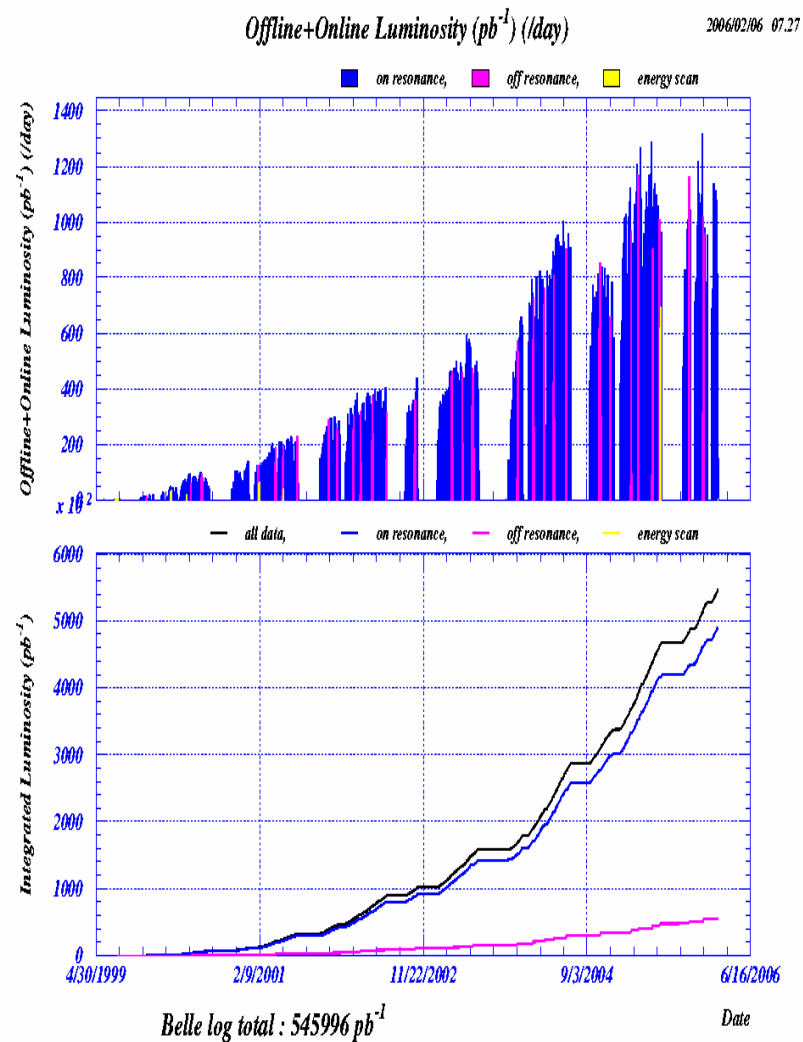
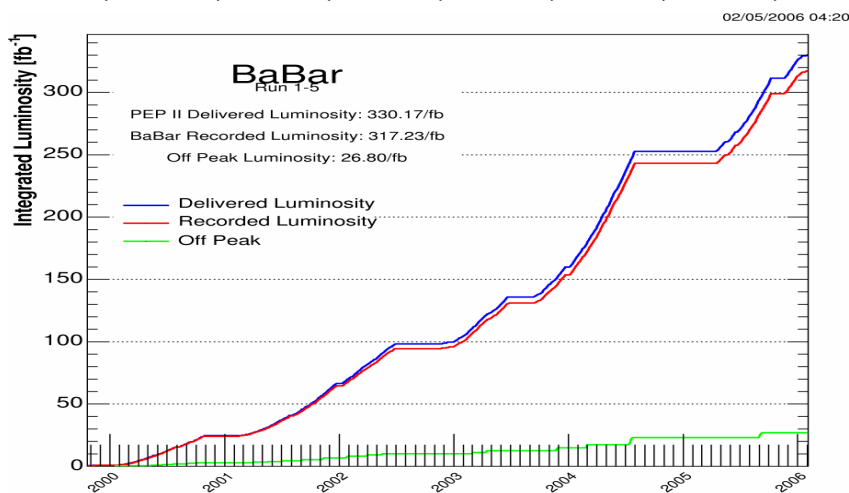
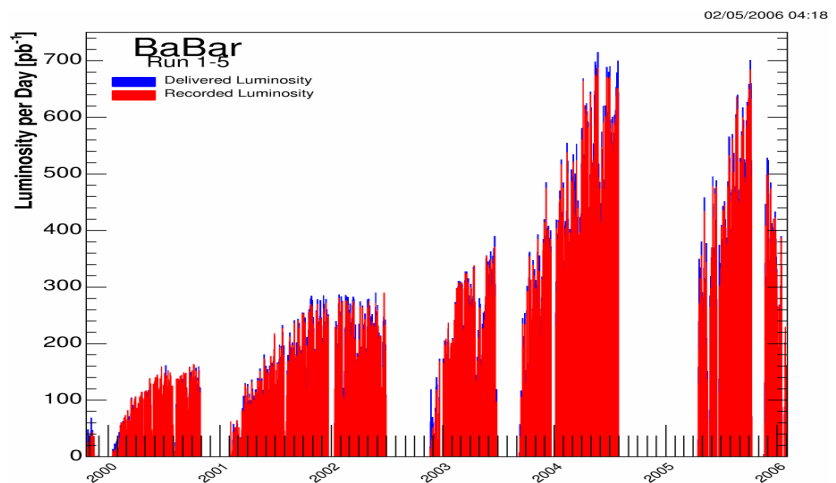
- Precision measurements of SM parameters from Semileptonic Decays:
  - $|V_{cb}|$  at 2% level
  - $|V_{ub}|$  at 8% probing consistency with  $\sin(2\beta)$  and hence SM
  - $m_b$  (<1%) and  $m_c$  (5%)
- Radiative B decays
  - $\text{BR}(B \rightarrow X_s \gamma)$  @ 7% - important constraint on many NP models
  - $b \rightarrow d \gamma$  constraining  $V_{td} V_{tb}^*$  – complementary to  $B_s$  mixing
- Wide variety of charmless hadronic B decays
  - evidence for direct CPV in  $B^+ \rightarrow \rho^0 K^+$
- First results from B decays via W-exchange & annihilation
  - sensitivity starting to test SM
- Many more results to come

# Backup Slides

# BaBar & Belle Detectors



# BFactory Performances



runinfo ver.1.55 Exo3 Run1 - Exo49 Run490 BELLE LEVEL latest: day is not 24 hours

# Fit to Moments of Inclusive Decay Distributions

The Operator Product Expansion separates perturbative from non-perturbative scales in a systematic way:

$$\Gamma_{SL}(B \rightarrow X_c l \nu) = \frac{G_F^2 m_b^5}{192 \pi^3} |V_{cb}|^2 (1 + A_{ew}) A_{pert}(r, \mu)$$

kinetic expec. value  $\rightarrow$  kinetic scheme  $r \equiv (m_c / m_b)^2$

$$\times \left[ z_0(r) \left( 1 - \frac{\mu_\pi^2 - \mu_G^2 + \frac{\rho_D^3 + \rho_{LS}^3}{m_b}}{2m_b^2} \right) - 2(1-r)^4 \frac{\mu_G^2 + \frac{\rho_D^3 + \rho_{LS}^3}{m_b}}{m_b^2} + d(r) \frac{\rho_D^3}{m_b^3} + O(1/m_b^4) \right]$$

chromomagnetic expec. value  $\mu_G^2$  Darwin term  $\rho_D^3 + \rho_{LS}^3$  spin-orbit  $d(r) \frac{\rho_D^3}{m_b^3}$

Benson, Bigi, Mannel & Uraltsev, hep-ph/0410080  
Gambino & Uraltsev, Eur.Phys.J. C34, 181 (2004)

Moments of hadronic mass, lepton energy and photon energy in  $b \rightarrow sg$  distribution depend on same heavy quark parameters:

$$\begin{aligned} \langle M_X^n \rangle &\rightarrow \langle M_X \rangle (m_b, m_c, \mu_\pi^2, \mu_G^2, \rho_D^3, \rho_{LS}^3, \alpha_s) \\ \langle E_\ell^n \rangle &\rightarrow \langle E_\ell \rangle (m_b, m_c, \mu_\pi^2, \mu_G^2, \rho_D^3, \rho_{LS}^3, \alpha_s) \\ \langle E_\gamma^n \rangle &\rightarrow \langle E_\gamma \rangle (m_b, \mu_\pi^2, \mu_G^2, \rho_D^3, \rho_{LS}^3, \alpha_s) \end{aligned}$$

$m_b$  and  $\mu_\pi^2$  are used to parameterise both  $B \rightarrow Xs \gamma$  and  $B \rightarrow Xu l \nu$  spectra

Many moment measurements ( $\sim 50$ ) allow to fit for all parameters up to  $1/m_b^3$

# $b \rightarrow sy$ Branching Fraction

- Partial branching fractions are measured above different photon energies
- Need to be extrapolated to  $E_\gamma > 1.6$  GeV to compare with theory
- Extrapolation factors based on HQE fit to  $clv$  and  $bsg$  moments

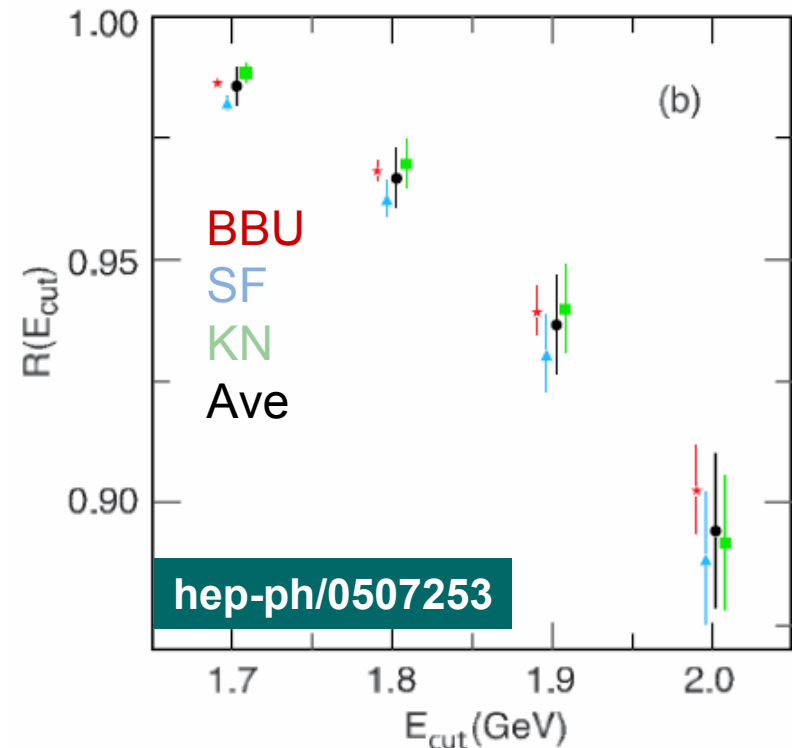
Mode	Reported $\mathcal{B}$	$E_{\min}$	$\mathcal{B}$ at $E_{\min}$
CLEO Inc. [3]	$321 \pm 43 \pm 27^{+18}_{-10}$	2.0	$306 \pm 41 \pm 26$
Belle Semi.[4]	$336 \pm 53 \pm 42^{+50}_{-54}$	2.24	—
Belle Inc.[5]	$355 \pm 32^{+30+11}_{-31-7}$	1.8	$351 \pm 32 \pm 29$
BABAR Semi.[6]	$335 \pm 19^{+56+4}_{-41-9}$	1.9	$327 \pm 18^{+55+4}_{-43-9}$
BABAR Inc.[7]	—	1.9	$367 \pm 29 \pm 34 \pm 29$

New HFAG Average:

$$\text{BR}(B \rightarrow X_s \gamma) = (3.55 \pm 0.24 \pm 0.10 \pm 0.03) \cdot 10^{-4}$$

7% uncertainty

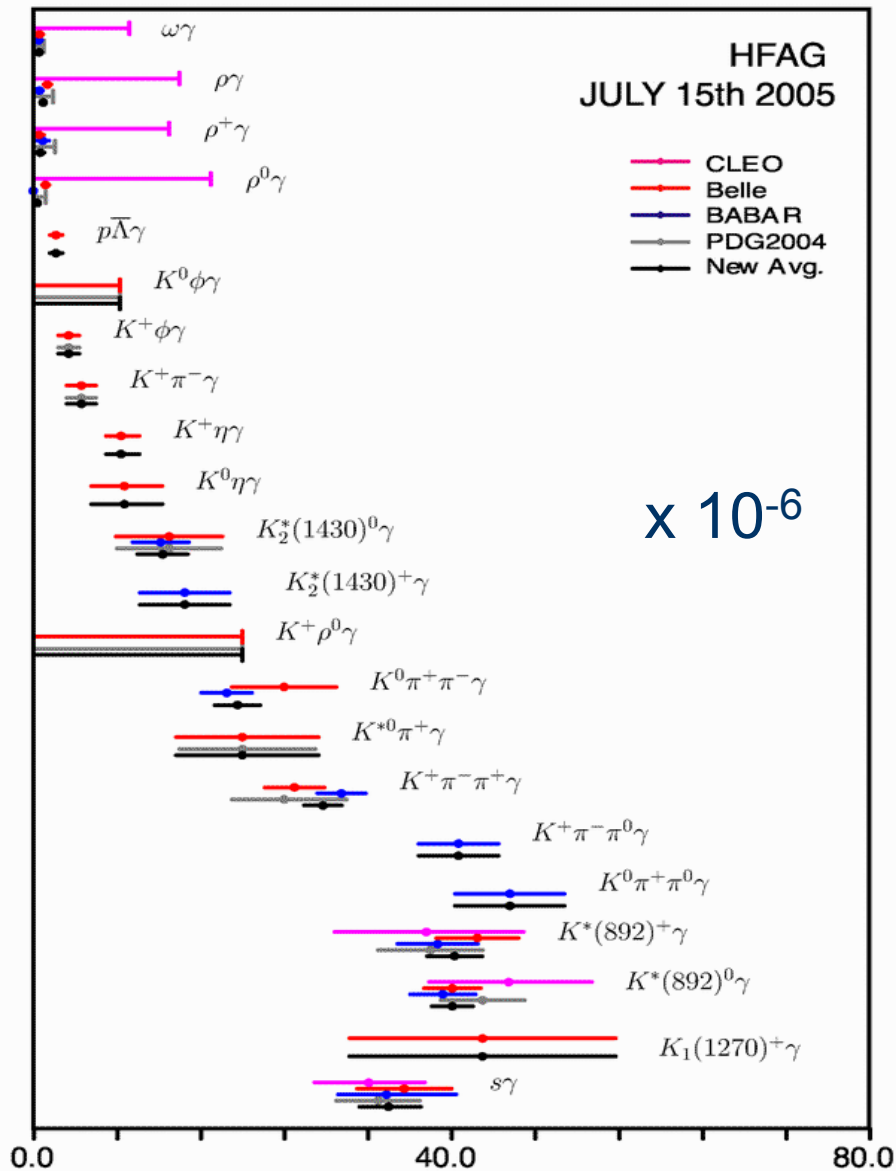
Extrapolation Factors for BF



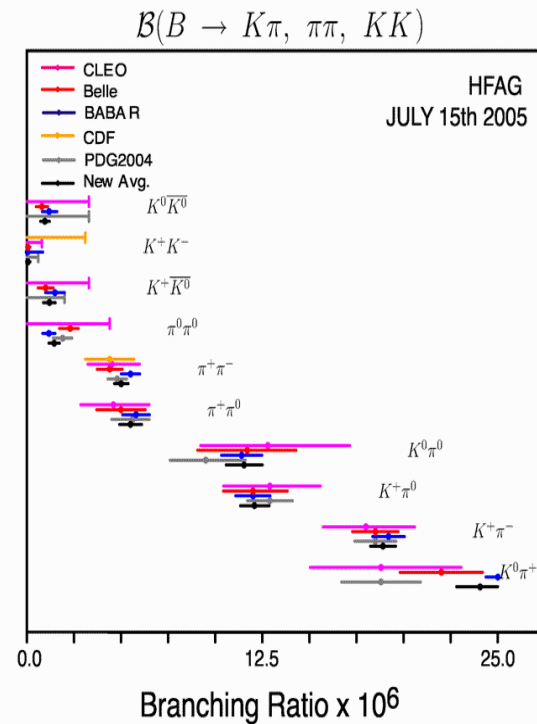
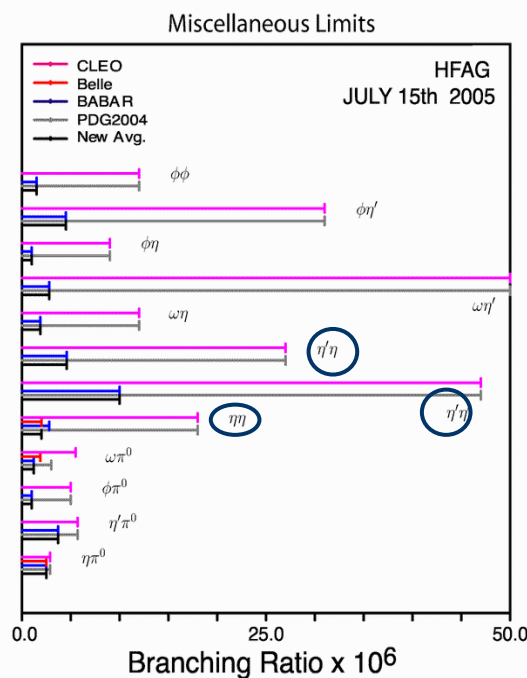
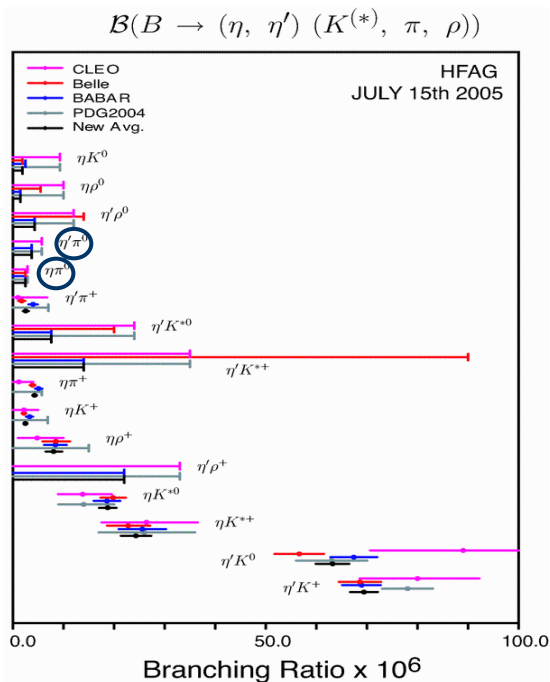
SM prediction:

$3.57 \pm 0.3 \times 10^{-4}$  Buras et al. (hep-ph/0203135)  
 $3.44 \pm 0.4 \times 10^{-4}$  Neubert (hep-ph/0408179)  
 $3.61 \pm 0.42 \times 10^{-4}$  Hurth et al. (hep-ph/0312260)

# Radiative B Decays

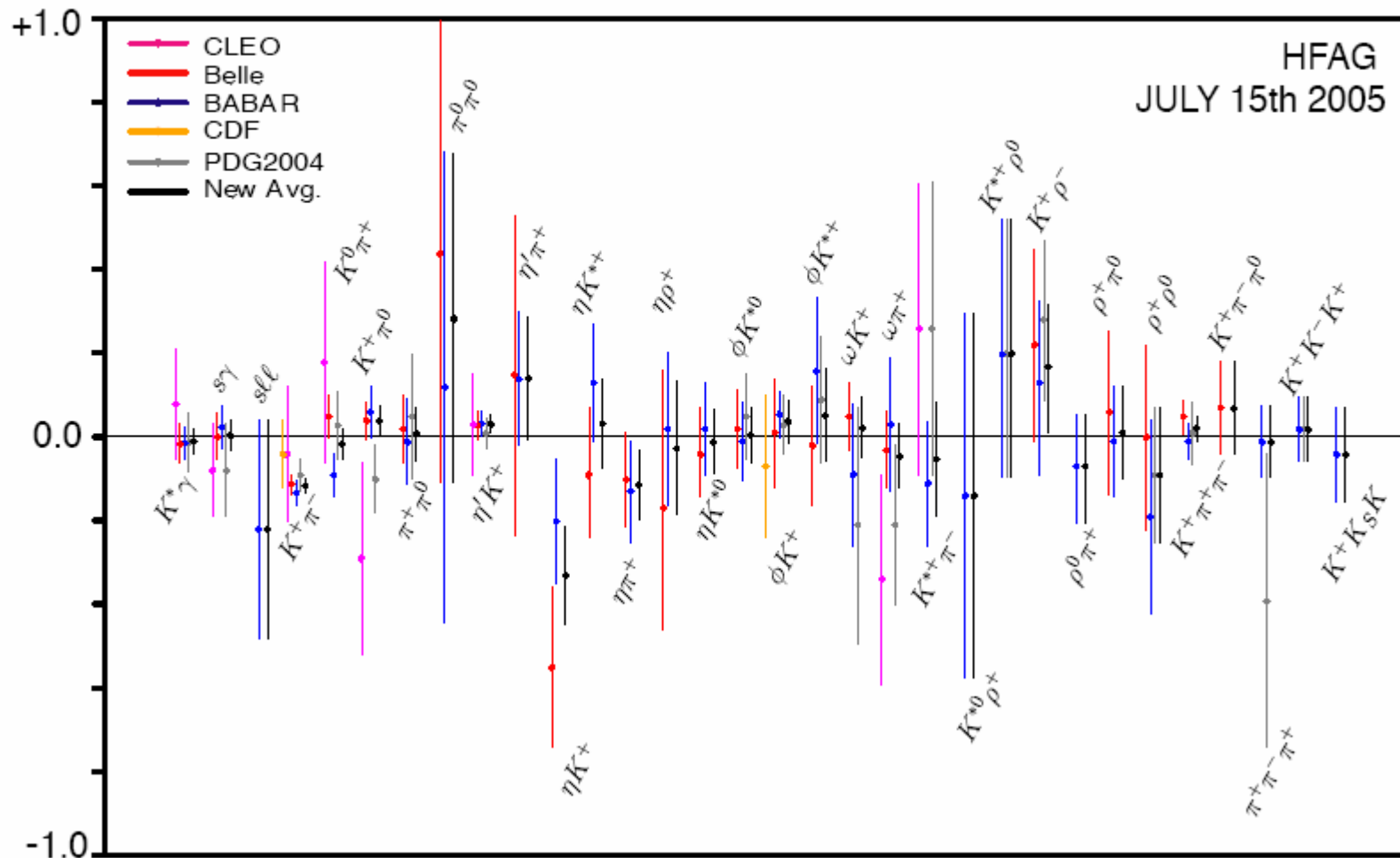


# Rare charmless hadronic B decays



# $A_{CP}$ in Rare Charmless B Decays

## CP Asymmetry in Charmless B Decays



# Dalitz plot analysis of $B^+ \rightarrow K^+ \pi^+ \pi^-$

Babar (hep-ex/0507004):

Mode	$\mathcal{B}(B^+ \rightarrow \text{Mode})(10^{-6})$	90% CL UL ( $10^{-6}$ )	$A_{CP}$ (%)
$K^+ \pi^- \pi^+$ Total	$64.1 \pm 2.4 \pm 4.0$	—	$-1.3 \pm 3.7 \pm 1.1$
$K^{*0}(892)\pi^+; K^{*0}(892) \rightarrow K^+ \pi^-$	$8.99 \pm 0.78 \pm 0.48^{+0.28}_{-0.39}$	—	$6.8 \pm 7.8 \pm 5.7^{+4.0}_{-3.5}$
$(K\pi)_0^0 \pi^+; (K\pi)_0^0 \rightarrow K^+ \pi^-$	$34.0 \pm 1.7 \pm 1.5^{+1.2}_{-1.6}$	—	$-6.4 \pm 3.2 \pm 2.0^{+1.1}_{-1.7}$
$\rho^0(770)K^+; \rho^0(770) \rightarrow \pi^+ \pi^-$	$5.07 \pm 0.75 \pm 0.35^{+0.42}_{-0.68}$	—	$32 \pm 13 \pm 6^{+8}_{-5}$
$f_0(980)K^+; f_0(980) \rightarrow \pi^+ \pi^-$	$9.47 \pm 0.97 \pm 0.46^{+0.42}_{-0.75}$	—	$8.8 \pm 9.5 \pm 2.6^{+9.3}_{-5.0}$
$\chi_{c0}K^+; \chi_{c0} \rightarrow \pi^+ \pi^-$	$0.66 \pm 0.22 \pm 0.07 \pm 0.03$	$< 1.1$	—
$K^+ \pi^- \pi^+$ nonresonant	$2.85 \pm 0.64 \pm 0.41^{+0.70}_{-0.34}$	$< 6.5$	—

Belle (hep-ex/0512066):

Mode	$\mathcal{B}(B^\pm \rightarrow Rh^\pm \rightarrow K^\pm \pi^\pm \pi^\mp) \times 10^6$	$\mathcal{B}(B^\pm \rightarrow Rh^\pm) \times 10^6$	$A_{CP}$ (%)
$K^\pm \pi^\pm \pi^\mp$ Charmless	$48.8 \pm 1.1 \pm 3.6$	—	$+4.9 \pm 2.6 \pm 2.0$
$K^*(892)[K^\pm \pi^\mp]\pi^\pm$	$6.45 \pm 0.43 \pm 0.48^{+0.25}_{-0.35}$	$9.67 \pm 0.64 \pm 0.72^{+0.37}_{-0.52}$	$-14.9 \pm 6.4 \pm 2.0^{+0.8}_{-0.8}$
$K_0^*(1430)[K^\pm \pi^\mp]\pi^\pm$	$32.0 \pm 1.0 \pm 2.4^{+1.1}_{-1.9}$	$51.6 \pm 1.7 \pm 6.8^{+1.8}_{-3.1}$	$+7.6 \pm 3.8 \pm 2.0^{+2.0}_{-0.9}$
$\rho(770)^0[\pi^+ \pi^-]K^\pm$	$3.89 \pm 0.47 \pm 0.29^{+0.32}_{-0.29}$	$3.89 \pm 0.47 \pm 0.29^{+0.32}_{-0.29}$	$+30 \pm 11 \pm 2.0^{+11}_{-4}$
$f_0(980)[\pi^+ \pi^-]K^\pm$	$8.78 \pm 0.82 \pm 0.65^{+0.55}_{-1.64}$	—	$-7.7 \pm 6.5 \pm 2.0^{+4.1}_{-1.6}$
$f_2(1270)[\pi^+ \pi^-]K^\pm$	$0.75 \pm 0.17 \pm 0.06^{+0.11}_{-0.18}$	$1.33 \pm 0.30 \pm 0.11^{+0.20}_{-0.32}$	$-59 \pm 22 \pm 2.0^{+3}_{-3}$
Non-resonant	—	$16.9 \pm 1.3 \pm 1.3^{+1.1}_{-0.9}$	—
$\chi_{c0}[\pi^+ \pi^-]K^\pm$	$0.56 \pm 0.06 \pm 0.04^{+0.12}_{-0.04}$	$112 \pm 12 \pm 18^{+24}_{-8}$	$-6.5 \pm 20 \pm 2.0^{+2.9}_{-1.4}$

Belle parameterises  $A_{cp} = -(2b \cos\phi)/(1+b^2)$

$b \neq 0$  is condition for DCPV!  
(even if  $A_{cp} = 0$ )

First evidence of direct CP violation in a charged B decay

